

BRANCH: MECHANICAL ENGINEERING

SEMESTER: 5<sup>TH</sup>

SUBJECT: HYDRAULIC MACHINE & INDUSTRIAL FLUID  
POWER

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## CHAPTER 1

### HYDRAULIC TURBINES.

- 1.1 Definition and classification of hydraulic turbines
- 1.2 Construction and working principle of impulse turbine.
- 1.3 Velocity diagram of moving blades, work done and derivation of various efficiencies of impulse turbine.
- 1.4 Velocity diagram of moving blades, work done and derivation of various efficiencies of Francis turbine.
- 1.5 Velocity diagram of moving blades, work done and derivation of various efficiencies of Kaplan turbine
- 1.6 Numerical on above
- 1.7 Distinguish between impulse turbine and reaction turbine.

#### Introduction-

- Hydraulic Machines are those machines which convert either hydraulic energy (energy possessed by water) into mechanical energy (which is further converted into electrical energy) or mechanical energy to hydraulic energy.
- Hydraulic energy is produced by the water which is stored in reservoirs and lakes at a high altitude (so that it has gravitational potential energy).
- The Hydraulic Machines which convert hydraulic energy to mechanical energy is called turbines while the hydraulic machines which convert mechanical energy into hydraulic energy is called pumps.
- Thus the study of Hydraulic machines consists of turbines and pumps.

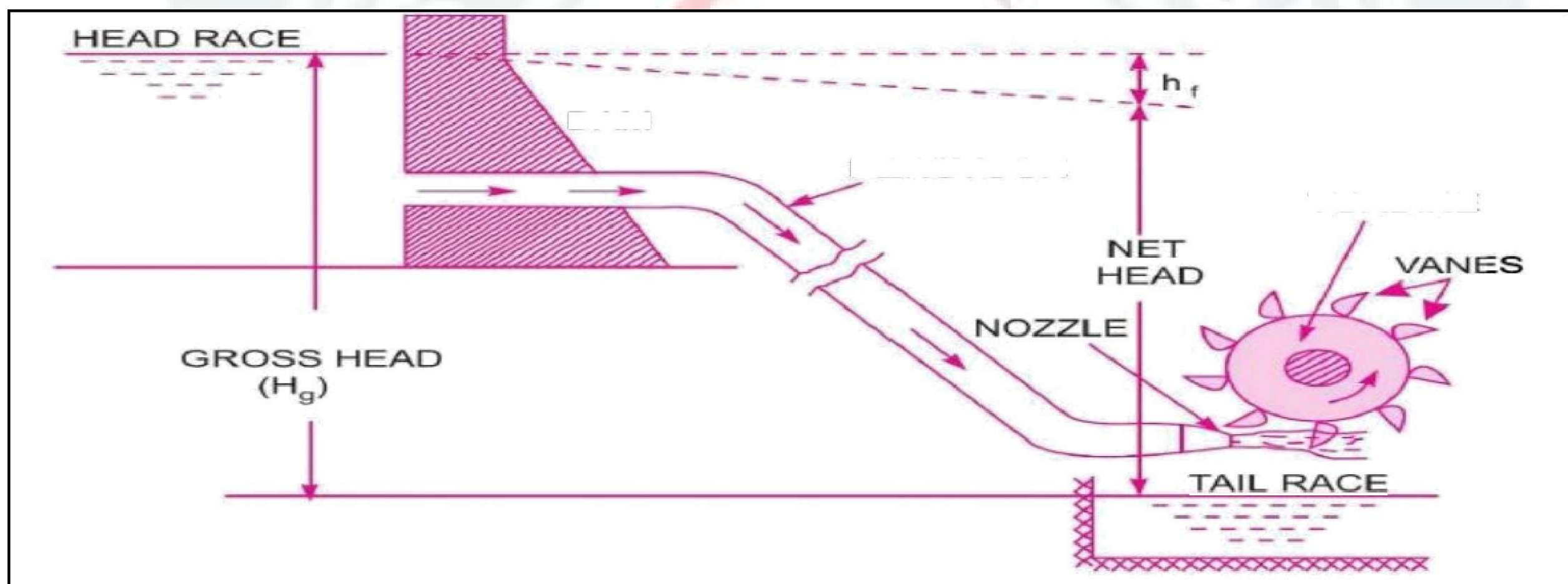
#### Turbines

- Turbines are defined as hydraulic machines which convert hydraulic energy into mechanical energy.
- This mechanical energy is used in running an electric generator which is directly coupled to the shaft of turbine. Thus the mechanical energy is converted into electrical energy.

- The electric power which is obtained from hydraulic energy is known as hydroelectric power.
- At present the generation of hydroelectric power is cheaper as compared to power generated by other sources like coal, oil etc.

### **General layout of a Hydroelectric Power plant**

- A dam constructed across a river to store water
- Pipes of large diameter called penstock, which carries water under pressure from the storage reservoir to turbine.
- Turbines having different types of vanes fitted to the wheels.
- Tail race, which is a channel which carries water away from the turbine after the water has worked on the turbine.
- The surface of water in the tail race channel is also called tail race.



### **Gross Head**

The difference between head race level and tail race level where no water is flowing is known as gross head ( $H_g$ )•

### **Net Head**

- It is defined as the head available at the inlet of turbine.
- When water flowing from head race to turbine a loss of head due to friction between the water and penstock occurs.



- » There are other losses due to bend pipe fittings, loss at entrance of penstock etc. which has smaller magnitude as compared to head loss due to friction ( $h_f$ )

- Net head ( $H$ ) =  $H_g - h_f$

$$h_f = \frac{4 \times f \times L \times V^2}{D \times 2 \times g}$$

Where  $V$  = Velocity of flow in penstock,  $L$  = length of penstock and  $D$  = Diameter of the penstock

due to the Classification:

It has been categorized into four parts such as:

1. According to the type of energy at Inlet:

- Impulse Turbine: The energy is in the form of kinetic. e.g.: Pelton wheel.
- Reaction Turbine: The energy is in the form of both Kinetic and Pressure. e.g.: Kaplan, Propeller, Francis turbine.

2. According to the direction of flow through Runner:

- Tangential flow: water flows in a direction tangential to the path of rotation, i.e. Perpendicular to both axial and radial directions.
- Radial flow: Water flows in the radial direction through the runner.
- Inward radial flow: If the water flows from outwards to inwards, radially.
- Outward radial flow: If the water flows from inwards to outwards, radially.
- Axial flow: Water flows parallel to the axis of the turbine. e.g.: Girard, Jonval, Kaplan turbine.
- Mixed flow: Water enters radially at the outer periphery and leaves axially. e.g.: Modern Francis turbine.

3. According to the head under which the turbine works:

- High head- The turbine capable of working under the high potential head of water above 300m (Impulse turbine. e.g.: Pelton turbine.)



- Medium head- The turbine is capable of working under a medium range of potential head about 60m to 300m (Reaction turbine. e.g.: Francis turbine.)
- Low head- The turbine is capable of working under a low range of potential head less than 60m (Reaction turbine. e.g: Kaplan turbine, propeller turbine.)

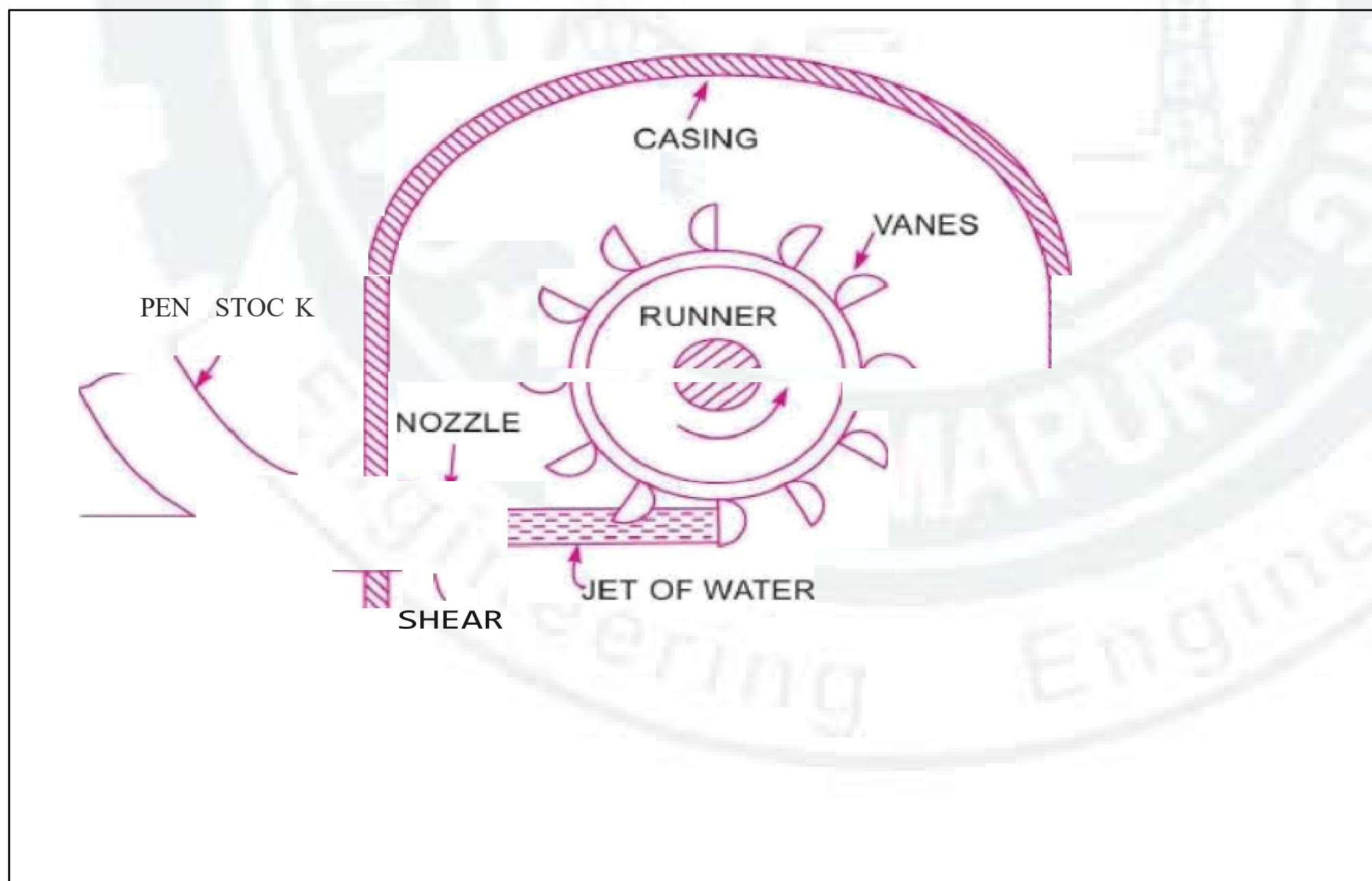
#### 4. According to the specific speed of the turbine:

- Low specific speed - (Impulse turbine. e.g.: Pelton wheel.)
- Medium-specific speed - (Reaction turbine. e.g.: Francis wheel.)
- High specific speed - (Reaction turbine. e.g.: Kaplan and Propeller turbine.)

#### Impulse Turbine-

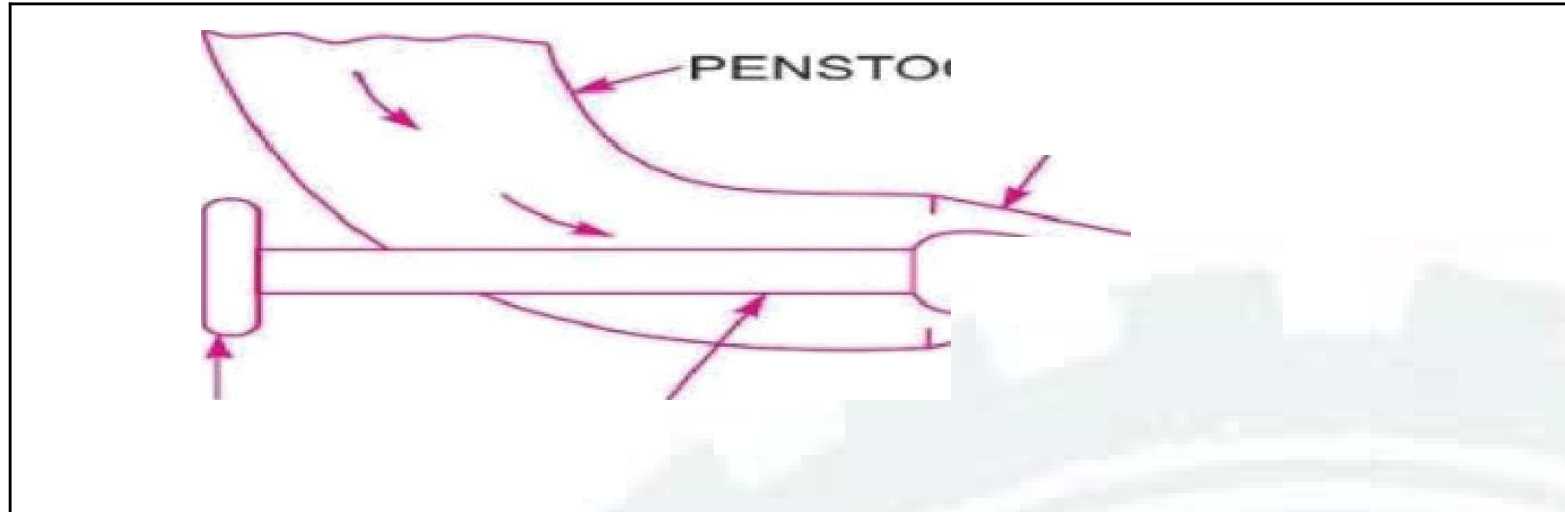
- Impulse turbine works on the basic principle of impulse.
- The water strikes the bucket along the tangent of the runner
- The energy available at the inlet is only kinetic energy
- The pressure at the inlet and outlet of turbine is atmospheric.
- This turbine is used for high heads.

#### Construction-



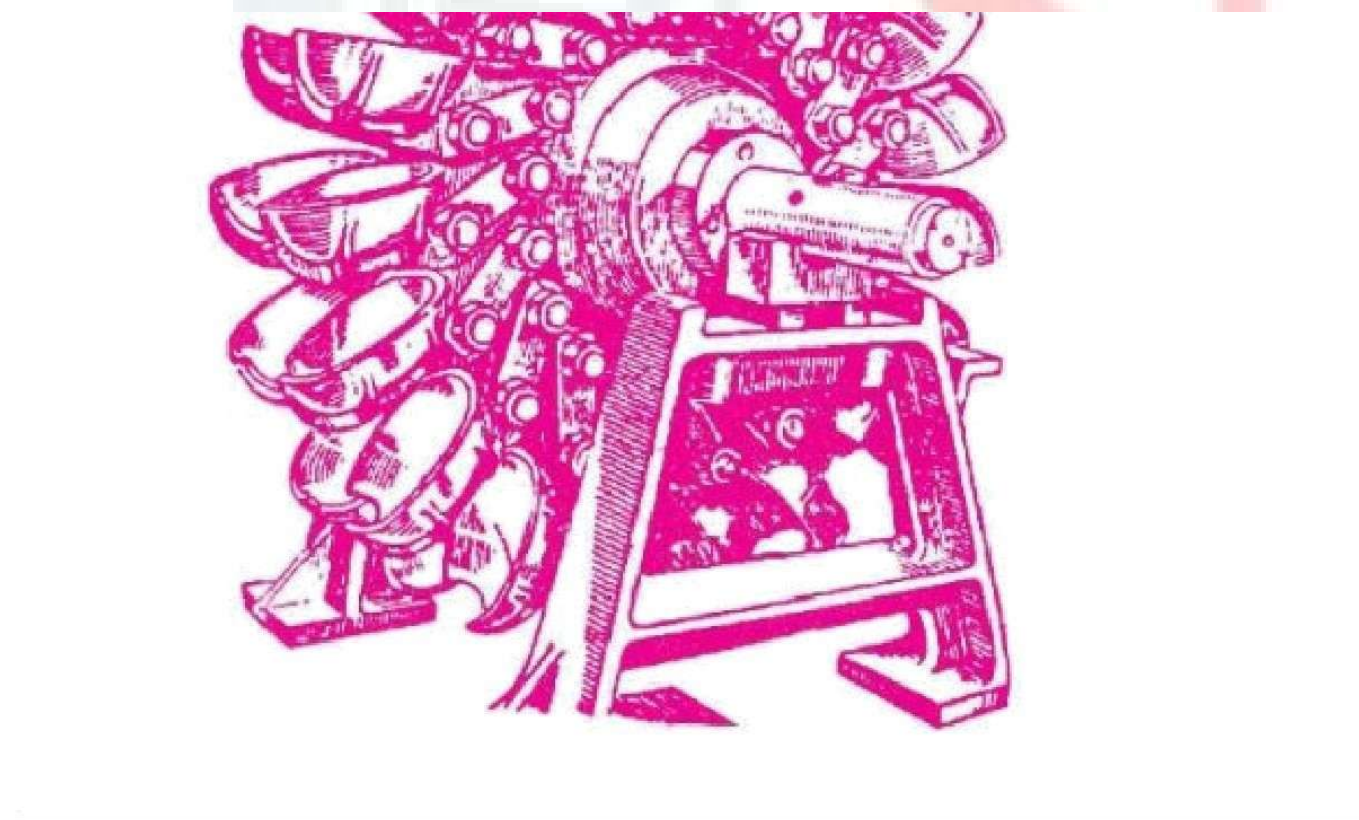
**Nozzle and Spear-** Nozzle directs the flow of water to the buckets, with an increased velocity coming from a high head.

Spear is a conical structure which is moved in and out of nozzle to regulate the flow of water striking the buckets



**Runner with Buckets** — It consists of circular disk where number of buckets evenly spaced are fixed.

The shape of bucket is double hemispherical up or bowl. Each bucket is divided into two symmetrical parts dividing by a wall is called splitter.



The jet of water strikes on the splitter. The splitter divide the jet into two equal part and the jet comes out at the outer edge of the bucket.

**Casing** - It is provided to prevent the splashing of water and to discharge water to the tail race. It also act as safeguard against accident.

**Braking Jet** - When the nozzle is completely closed by moving the spear in the forward direction the amount of water striking the runner is reduced to zero but the runner due to inertia continues revolving for long time.



In order to bring the runner to rest in a short time, a nozzle (brake) is provided which directs the jet of water on the back of bucket ; his jet of water is called breaking jet.

### Working Principle

- High pressure water flow form dam (high head) to nozzle (low head).
- This water flows through divergent nozzle where it's all pressure energy change into kinetic energy. It forms a water jet.
- The water jet strikes the blade at high speed which rotates the rotor.
- It transfers all kinetic energy of water to the rotor, which further use to rotate ie generator.
- After transferring energy, water flows to the tail race.
- This process continues continuously until sufficient power generates

### Different Efficiencies of Turbines-

Hydraulic Efficiency - It is defined as the ratio of power given by water to the **runner of a turbine to the power supplied by water** at the inlet of turbine.

$$\eta_h = \frac{\text{Power delivered to the runner}}{\text{Power supplied at inlet}} = \frac{R.P}{W.P}$$

Mechanical Efficiency — The ratio of power available at the shaft of turbine to the **power delivered by runner is defined as mechanical efficiency.**

$$\eta_m = \frac{\text{Power at the shaft of turbine}}{\text{Power delivered by water to the runner}} = \frac{S.P}{R.P}$$

Volumetric Efficiency = It is defined as the ratio of volume of water actually **striking the runner to the volume of water supplied to the turbine**

$$\eta_v = \frac{\text{Volume of water actually striking the runner}}{\text{Volume of water supplied to the turbine}}$$

Overall Efficiency - It is defined as the ratio of power available at the shaft of turbine to the Power supplied at inlet of turbine.



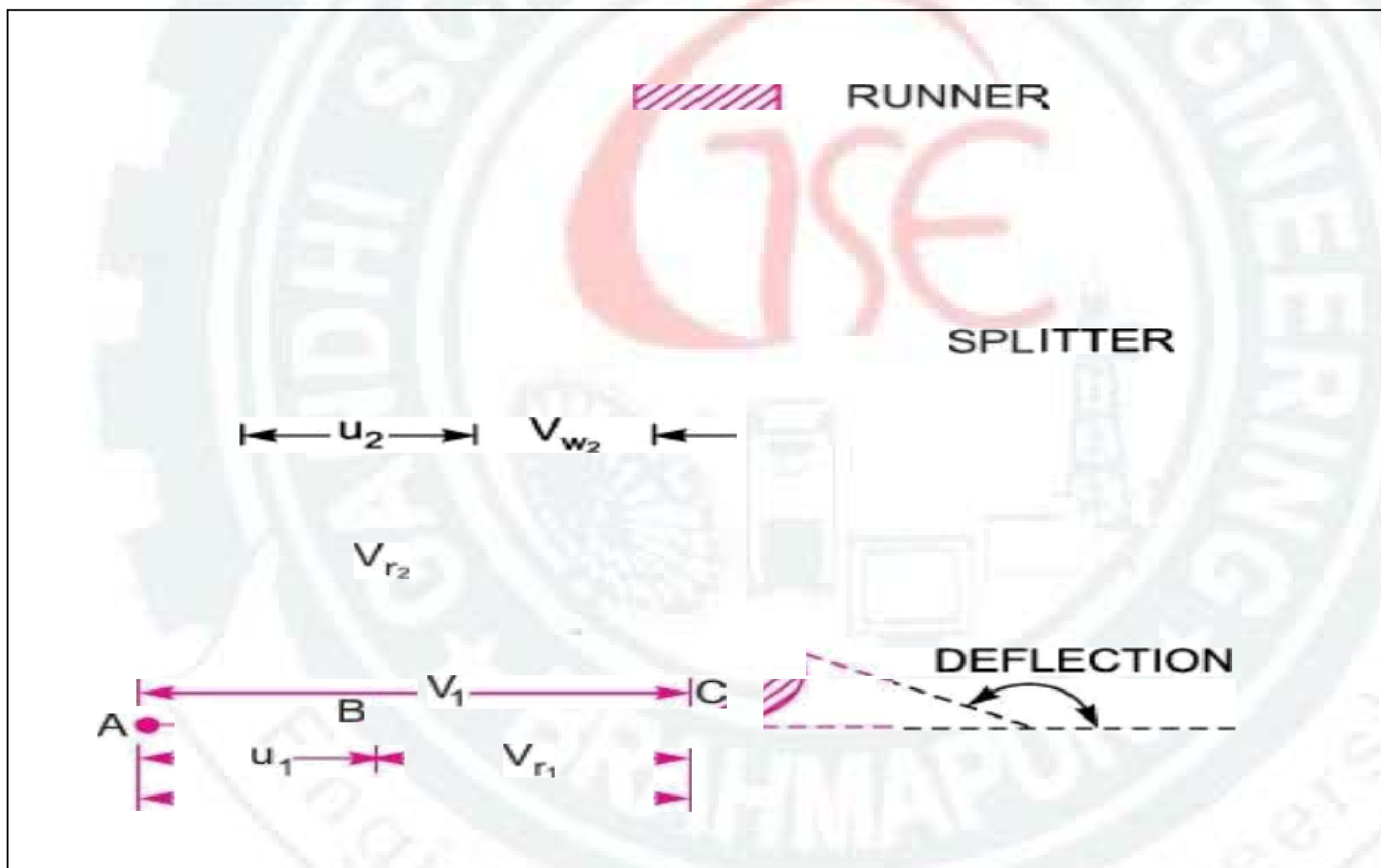
$$\eta_a = \frac{\text{Volume available at the shaft of the turbine}}{\text{Power supplied at the inlet of the turbine}} \times \frac{\text{Shaft power}}{\text{Water Power}} \times \frac{\text{S.P.}}{\text{W.P.}}$$

$$\frac{\text{S.P.} \times \text{R.P.} \times \text{S.P.} \times \text{R.P.}}{\text{W.P.} \times \text{R.P.} \times \text{R.P.} \times \text{W.P.}} \times \eta_m \times h$$

$$- \eta_n \times h$$

### Velocity Triangles Diagram For Pelton Wheel :

- The jet of water from the nozzle strikes the bucket at the splitter, which splits up the jet into two parts. These parts of the jet glide over the inner surfaces and come out at the outer edge.
- The splitter is the inlet tip and the outer edge of the bucket is the outlet tip of the bucket.
- The inlet velocity triangle is drawn at the splitter and the outer velocity triangle is drawn at the outer edge of the bucket.



Where,

$V_1$ —velocity of jet at inlet

$u_s$ - velocity of the vane/bucket at inlet

$m_l$  relative velocity of jet at inlet

$V_{o_l}$ —Velocity of whirl at inlet

$n$  = angle between the direction of the jet and the direction of motion of the

vane, guide blade angle (Here in this figure it is zero)

$\theta$  = angle made by  $r_1$  with the direction of motion of vane at the inlet, vane angle at inlet ( $=0$ )

$u_2$  = Velocity of jet at outlet of vane

$u_2$  = Velocity of vane at outlet

$V_r$  = relative velocity of jet at outlet

$V_w$  = velocity of whirl at outlet

$V_{f2}$  = velocity of flow at the outlet

$\phi$  = angle between  $u_2$  with the direction of motion of vane at the outlet

$\psi$  = angle made by  $v_r$  with the direction of motion of vane at the outlet, vane angle at outlet

$H' = H_i - h_f$

$$h_f = \frac{4 f_x L V^2}{D^5 \times 2 \times g} \quad (D = \text{Diameter of penstock})$$

$$\frac{H'}{H} = \frac{H_i - h_f}{H} \quad (H = \text{net head acting on turbine})$$

$$u_1 = u_2 = \frac{\pi D N}{60} \quad (D = \text{Diameter of wheel, } N = \text{speed of the wheel in rpm})$$

The velocity triangle at inlet will be a straight line where,

$$u_1 + V_{r1} = u_2$$

If the vane surface is assumed to be very smooth the loss of energy due to friction will be zero.

The water will glide over the surface of vane with a relative velocity  $V_{r1}$  and will come out of the vane with relative velocity  $V_{r2}$ , which means  $V_{r1} = V_{r2}$

From the velocity triangle at outlet,  $V_{r2} = V_{u2} \tan \phi$  and  $V_{p2} = V_{r2} \cos \phi$

The force exerted by the jet of water in the direction of motion

$$F_g = \frac{\text{Initial Momentum} - \text{Final Momentum}}{\text{Time}}$$

$$F_g = \rho a (u_1 - u_2) \quad (\text{Initial velocity} - \text{final velocity})$$

$$\frac{1}{t}(\text{Initial velocity} - \text{final velocity})$$

$$\frac{\rho V}{t}(V_{w1} + V_{w2}) = \frac{\rho a l}{t} (V_{w1} + V_{w2})$$

$$F = \rho a V_1 [V_{w1} + V_{w2}]$$

Net work done by the jet on the runner per second

$$= F \times u = \rho a V_1 [V_{w1} + V_{w2}] \times u$$

$$W = \rho a V_1 [V_{w1} + V_{w2}] \times u$$

The energy supplied to the jet at inlet is in the form of K.E and is equal to  $\frac{1}{2} \rho a V_1^3$

$$\text{Kinetic energy of jet per second} = \frac{1}{2} (\rho a V_1^3) \times 1$$

$$\text{Hydraulic efficiency, } q_h = \frac{\text{Work done per second}}{\text{K.E of jet per second}}$$

$$= \frac{\rho a V_1 [V_{w1} + V_{w2}] \times u}{\frac{1}{2} (\rho a V_1^3) \times 1} = \frac{2 [V_{w1} + V_{w2}] u}{V_1^2}$$

$$q_h = \frac{2 [V_{w1} + V_{w2}] u}{V_1^2}$$

### Design of Pelton Wheel:

- » Velocity of jet at inlet  $V_1 = C_v \sqrt{2gH}$  where  $C_v$  = coefficient of velocity 0.98-0.99
- » Velocity of wheel where  $u = p \sqrt{2gH}$  ... Where  $p$  is the speed ratio = 0.43-0.48

The angle of deflection is  $165^\circ$  unless mentioned.

- Pitch or mean diameter  $D$  can be expressed by,  $u = \pi D N / 60$
- Jet ratio  $M = D/d$  (12 in most cases/calculate),  $d$  = nozzle diameter



- Number of bucket on a runner  $Z = 15 + D/2d = 15 + 0.5 = 15.5$
- Number of Jets = obtained by dividing the total rate of flow through the turbine by the rate of flow through the single jet
- Size of Bucket: Axial Width, radial length, depth

### Numerical Problems

Q 1. A Pelton wheel has a mean bucket speed of 10 meter per sec with a jet of water flowing at the rate of 700 liters per sec under a head of 30 mt. the bucket deflect through an angle of 160 degree. Calculate the power given by water to the Runner and hydraulic efficiency of Turbine Assume Co-efficient of velocity as 0.98

Solution:

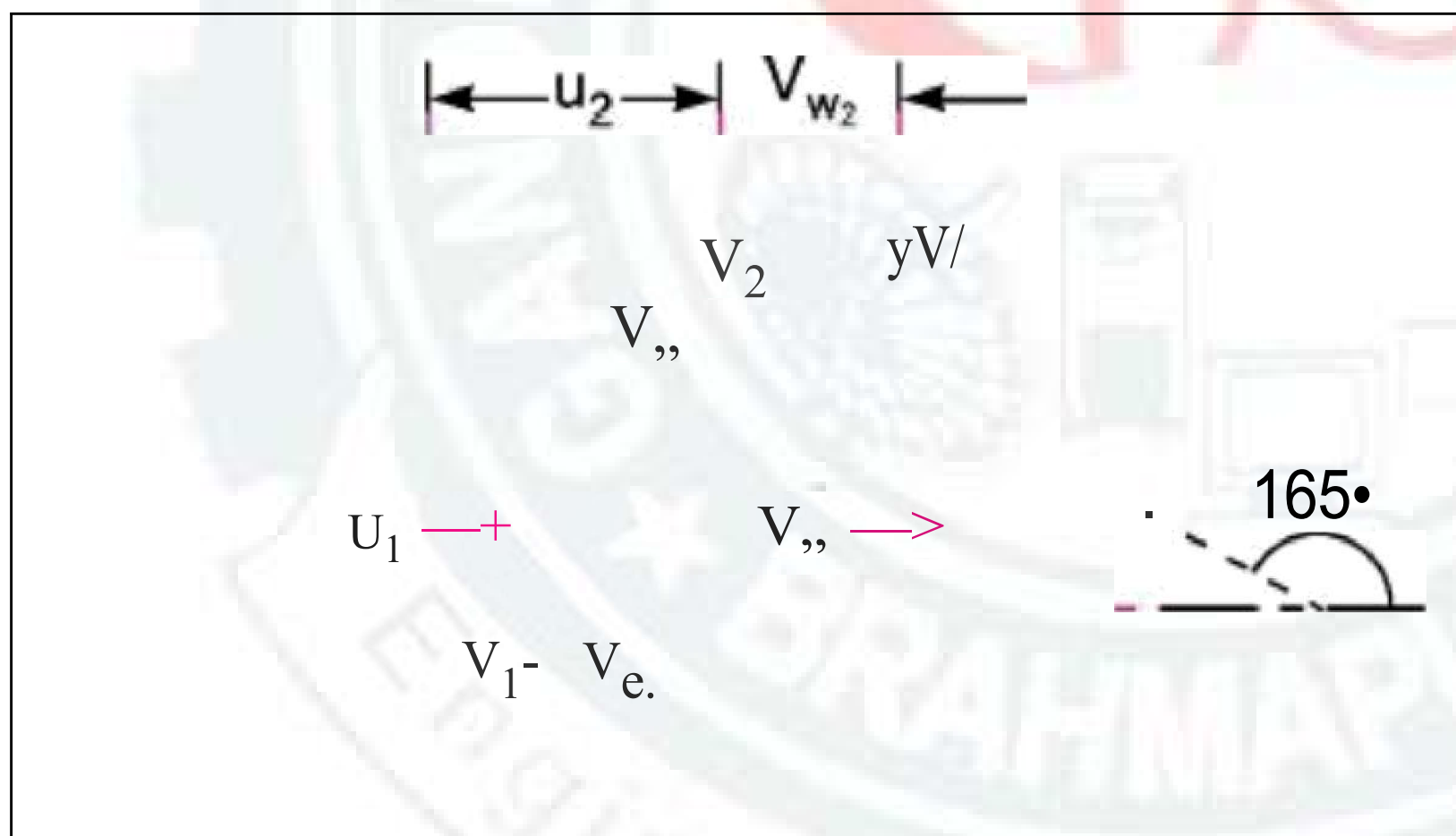
Given data:

speed of bucket,  $U = U_1 = U_2 = 10 \text{ m/sec}$   
 $Q = 700 \text{ litre/sec} = 700 \times 10^{-3} \text{ m}^3/\text{sec}$

$H = 30 \text{ m}$

angle deflected  $= 160^\circ$   $\theta = 180 - 160 = 20^\circ$

RP = ?  $h = ?$ ,  $C_v = 0.98$



From velocity triangle at inlet

velocity of jet  $= C_v \sqrt{2gH} = 0.98 \times \sqrt{2 \times 9.81 \times 30} = 23.77 \text{ m/sec}$

We have from velocity diagram at inlet  $V_1 = V_{p1} = 23.77 \text{ m/sec}$

$V_{G1} = V_{q1} - U = 23.77 - 10 = 13.77 \text{ m/sec}$

We have from velocity diagram at outlet  $t_r = t_2 = 13.77 \text{ Sec}$

$$V_{r2} = V_{r2} \cos 8 - U_2 = 13.77 \cos 20 - 10 = 2.94 \text{ m/sec}$$

Now work done by jet of water on Bucket or Runner Power

$$\begin{aligned} R.P &= \frac{\rho a V_1 (V_{r1} - V_{r2}) \times U}{1000} \text{ KW} \\ &= \frac{\rho Q (V_{p1} + V_{p2}) \times U}{1000} = \frac{1000 \times 0.7 (23.77 - 2.94) \times 10}{1000} \\ R.P &= 186.97 \text{ KW} \end{aligned}$$

The hydraulic efficiency of the turbine is given by

$$\begin{aligned} \eta_h &= \frac{(V_{r1} - V_{r2}) \times U}{\frac{V_1^2}{2}} = \frac{2(23.77 - 2.94) \times 10}{23.77^2} \\ \eta_h &= 0.9454 \text{ say } 94.54\% \end{aligned}$$

Q2. A Pelton wheel is to be designed for the following Specification:

Shaft power = 11772 KW; head = 380 m; speed = 750 RPM; overall efficiency = 86%, jet diameter not to exceed one-sixth of the wheel diameter. Determine:

- The wheel diameter
- Number of jet required
- Diameter of jet, take  $K_{gb} = 0.985$  and  $K_{v1} = 0.45$

Solution:

Given data:

$$S.P = 11772 \text{ KW}$$

$$H = 380 \text{ m,}$$

$$\eta_o = 86\%$$

$$D = \frac{D}{6}$$

$$D, d, Z = ?$$

We have overall efficiency of Pelton wheel Turbine

$$\eta_o = \frac{S.P}{W.P} = 0.86 \Rightarrow \frac{11772}{W.P} = 0.86$$

$$\therefore W.P = \frac{11772}{0.86} = 13688.37 \text{ KW}$$

$$\text{velocity of jet } V_j = C_{v1} \sqrt{2gH} = 0.985 \times \sqrt{2 \times 9.81 \times 380} = 85.1 \text{ m/sec}$$

• we have water power

$$W.P = \frac{\rho g Q H}{1000} = 13688.37$$

$$\Rightarrow Q = \frac{13688.37 \times 1000}{\rho g H} = \frac{13688.37 \times 1000}{1000 \times 9.81 \times 380} = 3.62 \text{ m}^3/\text{s}$$

We have speed ratio

$$K_1 = \frac{U_1}{\sqrt{2gH}} = 0.45$$

$$U_1 = U_2 = 0.45 \times \sqrt{2 \times 9.81 \times 380} = 38.85 \text{ m/s}$$

We have mean velocity of bucket

$$U = \frac{\pi D N}{60} = 38.85$$

$$\Rightarrow D = \frac{60 \times 38.85}{\pi \times 900} = 0.83 \text{ m} \dots \dots \text{Mean Diameter of Bucket}$$

Now we have dia. of jet

$$d = \frac{D}{\sqrt{K_1}} = \frac{0.83}{\sqrt{0.45}} = 0.1648 \text{ m}$$

$$\text{Discharge of water through single jet } Q = aV = \frac{\pi}{4} d^2 \times V = \frac{\pi}{4} \times 0.1648^2 \times 8505 = 1.0 \text{ m}^3/\text{s}$$

$$0.1648^2 = 1.0 \text{ m}^3/\text{s}$$

No of jet

$$n = \frac{\text{Total } Q}{Q_{\text{jet}}} = \frac{3.62}{0.81305} = 1.99 \text{ say } 2 \text{ nos.}$$

Q3. A Pelton wheel is having a mean Bucket diameter of 1 m and is running at 1000 R.P.M. the net head on the Pelton wheel is 700 m. if the side clearance angle is 15 degree and discharge through nozzle is 0.1 meter cube per sec find:  
I. Power available at the Nozzle ü. Hydraulic efficiency of the turbine

Solution:

Given data:

Diameter of wheel  $D = 1.0 \text{ m}$

speed of wheel  $N = 1000 \text{ r.p.m}$

clearance angle means vane angle at outlet  $\theta = 15^\circ$

$Q = 0.1 \text{ m}^3/\text{Sec}$  Net Head  $H = 700 \text{ m}$

Assume  $C_d$  as 0.98

From velocity triangle at inlet



$$C_d \sqrt{2gH} = C_d \sqrt{2 \times 9.81 \times 700} = 114.84 \text{ m/Sec}$$

We have from velocity diagram at inlet  $V_1 = V_{w1} = 114.84 \text{ m/Sec}$

Wheel velocity

$$U = v_{w1} = U_1 = \frac{\pi D N}{60} = \frac{\pi \times 1 \times 1000}{60} = 52.35 \text{ m/Sec}$$

Relative velocity at inlet  $v_{r1} = V_1 - U_1 = 114.84 - 52.35 = 62.49 \text{ m/Sec}$

We have from velocity diagram at outlet  $v_{r2} = v_{r1} = 62.49 \text{ m/Sec}$

$$V_{p2} = v_{r2} \cos \theta - U_2 = 62.49 \cos 15^\circ - 52.35 = 8.01 \text{ m/Sec}$$

1. Power available at nozzle (W.P):

we have water power

$$W.P = \frac{\rho g Q H}{1000} \text{ KW} = \frac{1000 \times 9.81 \times 0.1 \times 700}{1000} \text{ KW} = 686.70 \text{ KW}$$

2. The hydraulic efficiency of the turbine is given by

$$\eta_h = \frac{(V_{p1} + V_{p2}) \times U}{V_1^2} = \frac{2(114.84 + 8.01) \times 52.35}{114.84^2} = 0.9684 \text{ say } 97\%$$

$$\eta_h = 0.9684 \text{ say } 97\%$$

Q4. A 137 mm diameter jet of water issuing from a nozzle impinges on the Buckets of a Pelton wheel and the jet is deflected through an angle 165 degree by the buckets. The head available at the nozzle is 400 m assuming coefficient of velocity as 0.97, speed ratio as 0.46 and reduction in relative velocity while passing through buckets as 15% find:

i. the force exerted by the jet on Buckets in tangential direction

ii. The power developed

Solution:

Given Data:

Dia of jet  $d = 137 \text{ mm} = 0.137 \text{ m}$

angle  $\theta = 15^\circ$

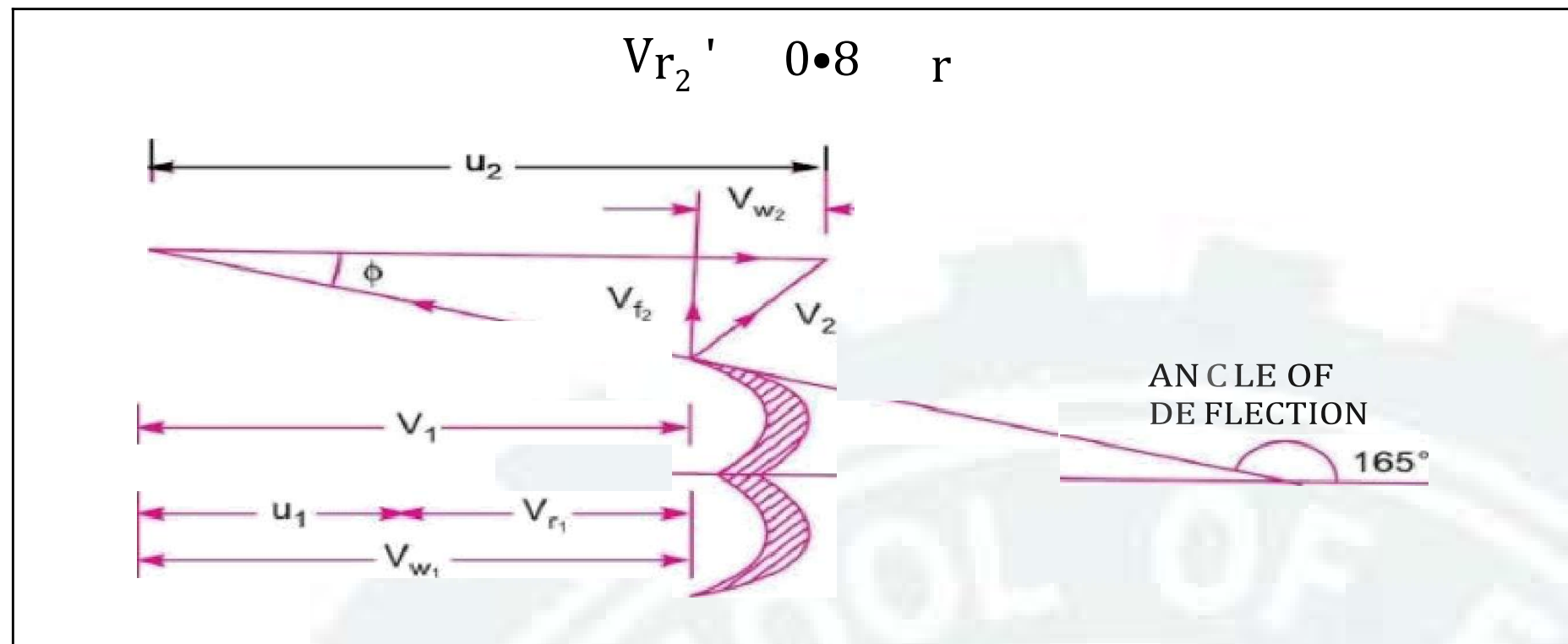
$H = 400 \text{ m}$

$C_v = 0.97$

speed ratio = 0.46

$$\text{area of jet } a = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 0.137^2 = 0.01474 \text{ m}^2$$

as per question relative velocity of water at outlet



From velocity triangle at inlet

$$\text{velocity of jet } V_1 = C_v \sqrt{2gH}$$

$$= 0.97 \times \sqrt{2 \times 9.81 \times 400} = 85.93 \text{ m/sec}$$

We have from velocity diagram at inlet

$$V_1 = V_{p_i} = 85.93 \text{ m/sec}$$

Now velocity of wheel

$$U = V_{p_i} \times \text{speed ratio} = 85.93 \times 0.46 = 40.75 \text{ m/sec}$$

$$\text{Relative velocity at inlet } V_{r_i} = V_{p_i} - U = 85.93 - 40.75 = 45.18 \text{ m/sec}$$

$$\text{We have from velocity diagram at outlet } V_{r_2} = 0.85 V_{r_i} = 38.40 \text{ m/sec}$$

$$V = U - V_{r_2} \cos 15^\circ = 40.75 - 38.40 \cos 15^\circ = 3.658 \text{ m/sec}$$

Now work done by jet of water on Bucket or Runner Power

$$RP = \frac{\rho a (V_{p_i} - V_{r_2} \cos 15^\circ) \times U}{1000} \dots \dots \text{negative sign since } U < V_{r_2}$$

$$= \frac{1000 \times 0.01474 \times 85.93(85.93 - 3.658) \times 40.75}{1000}$$

$$R.P = 4246.4 \text{ KW}$$

Force exerted by jet of water in tangential direction

$$F, = \rho a V (V_p - V_{p'}) = 1000 \times 0.01474 \times 85.93(85.93 - 3.658) \\ = 104206 \text{ N}$$

Q5. Two jets strike the buckets of a Pelton wheel, which is having shaft Power 15450 KW. The diameter of each jet is given as 200 mm. if the net head on the turbine is 400m find overall efficiency of the turbine. Take  $C_v = 1.0$ .

Ans.:

Given Data

$$\text{Shaft Power, } SP = 15450 \text{ KW}$$

$$\text{Diameter of jet, } d = 200 \text{ mm} = 0.2 \text{ m}$$

$$\text{Net head, } H = 400 \text{ m}$$

$$C_v = 1.0$$

$$\text{area of jet } a = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 0.2^2 = 0.0314 \text{ m}^2$$

From velocity triangle at inlet

$$\text{velocity of jet } V_1 = C_v \sqrt{2 \times g \times H} = 1.0 \times \sqrt{2 \times 9.81 \times 400} = 88.54 \frac{\text{m}}{\text{Sec}}$$

Total discharge of water from two nozzles at inlet of Turbine is given by

$$Q = 2 \times (a \times V_1) = 5.562 \text{ m}^3/\text{Sec}$$

Power available at inlet of Turbine

we have water power

$$W.P = \frac{\rho g Q H}{1000} \text{ KW} \\ = \frac{1000 \times 9.81 \times 5.562 \times 400}{1000} \text{ KW} = 21817.44 \text{ KW}$$

overall efficiency of Turbine

$$\eta = \frac{S.P}{W.P} = \frac{15450}{21817.44} = 0.708 \\ \text{to } \% \quad 0.708 = 70.8 \%$$



Q6. A Pelton wheel turbine is to be designed for a head of 60m when running at 200 rpm. The Pelton wheel develops 95.6475 KW shaft Power. The velocity of Buckets is 0.45 times the velocity of jet. Overall efficiency is 0.85 and coefficient of Velocity is equal to 0.98.

Solution:

Given Data:

Head  $H = 60$  m

Speed of wheel  $N = 200$  rpm

Shaft Power  $SP = 95.6475$  KW

overall efficiency  $\eta_o = 0.85$

$C_v = 0.98$

velocity of bucket  $U = 0.45 \times V$ ,

Design of Pelton wheel means we have to find the calculation of Values

- Diameter of jet (d),
- Diameter of Wheel (D),
- No of Bucket on Runner (Z),
- No of Jet Required (n)

$$\text{area of jet } a = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 0.2^2 = 0.0314 \text{ m}^2$$

From velocity triangle at inlet  
velocity of jet

$$V = C_v \sqrt{2gH} = 0.98 \times \sqrt{2 \times 9.81 \times 60} = 33.62 \frac{\text{m}}{\text{Sec}}$$

Now velocity of bucket

$$U = U_i = 0.45 \times V = 0.45 \times 33.62 = 15.13 \frac{\text{m}}{\text{Sec}}$$

$$\eta_o = \frac{W.P}{P_g} = 0.85 \quad \text{--- 088S}$$

$$W.P = \frac{95.6475}{0.85} = 112.52 \frac{\text{m}}{\text{Sec}}$$

We have Power available at inlet of Turbine

$$W.P = \frac{\rho g Q H}{1000} = 112.52 \text{ KW}$$

$$\frac{112.52 \times 1000}{1000 \times 9.81 \times 60} = 1.92 \text{ Sec}$$

1. Diameter of Jet (d)

Total discharge of water from nozzles at inlet of Turbine is given by

$$Q = (a \times V_j) = 0.1912 \text{ m}^3/\text{Sec}$$

$$a = \frac{0.1912}{33.62}$$

$$\frac{\pi}{4} \times d^2 = \frac{0.1912}{33.62}$$

$$d = \sqrt{\frac{0.1912 \times 4}{33.62 \times \pi}}$$

$$d = \sqrt{\left(\frac{0.1912 \times 4}{33.62 \times \pi}\right)} = 0.085 \text{ m say } 85 \text{ mm, } \text{m } d = 0.085 \text{ m say } 85 \text{ mm}$$

2. Diameter of Wheel

We have

$$U = 15.13 \text{ m/Sec}$$

$$\frac{U}{\pi D N} = 15.13$$

$$= \frac{60 \times 15.13}{\pi \times N} = \frac{60 \times 15.13}{\pi \times 200} = 1.44 \text{ m}$$

$$< D = 1.44 \text{ m}$$

3. No of Bucket  $D = 1.44$

$$Z = 15 + \frac{D}{2d} + \frac{D}{2 \times 0.085} = 23.5 \text{ say } 24 \text{ No.s}$$

4. Size of Bucket

$$\text{Width of Buckets} = 5 \times d = 5 \times 85 = 425 \text{ mm}$$

$$\text{Depth of Bucket} = 1.2 \times 85 = 102 \text{ mm}$$

Q7. Determine the power given by the jet of water to the runner of a Pelton wheel turbine which is having tangential velocity as 20 m/s. The net head on the Turbine is 50 m and discharge through the jet is 0.03 m<sup>3</sup>/Sec. The side clearance angle is 15 degree and take velocity coefficient as 0.975

Ans.:

Given data:

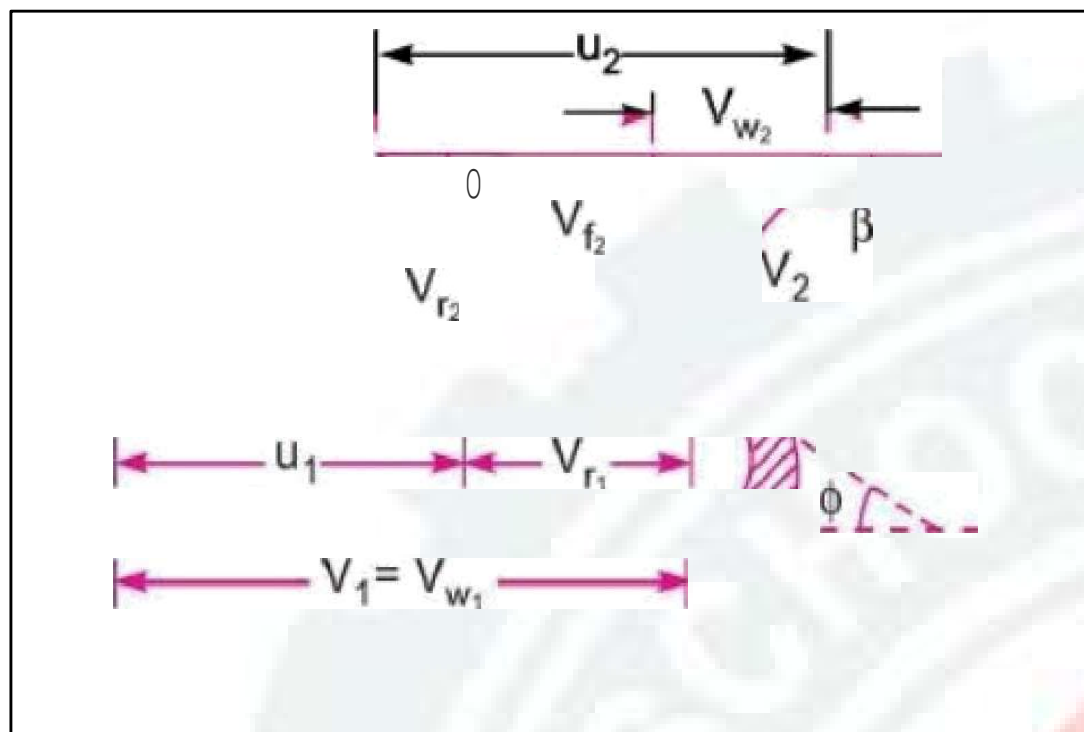
Velocity of Wheel,

$$U = U_1 = U_2 = 20 \frac{\text{m}}{\text{e}} \quad H = 50 \text{ m} \quad \phi = 0.03 \text{ m}^3/\text{Sec}$$

side clearance angle,  $Q = 15^\circ$

$$C_v = 0.975$$

R.P = ?



From velocity triangle at inlet

$$\text{velocity of jet} = C_v \sqrt{2gH}$$

$$= 0.975 \times \sqrt{2 \times 9.81 \times 50} = 30.54 \text{ m/Sec}$$

We have from velocity diagram at inlet

$$V_1 = V_{p1} = 30.54 \text{ m/Sec}$$

$$\text{Relative velocity at inlet } V_{r1} = V_1 - U_1$$

$$= 30.54 - 20 = 10.54 \text{ m/Sec}$$

We have from velocity diagram at outlet

$$V_{r2} = 10.54 \text{ m/Sec}$$

$$V_2 = U_2 - V_{r2} \cos \phi = 20 - 10.54 \cos 15^\circ = 9.82 \text{ m/Sec}$$

Now work done by jet of water on Bucket or Runner Power

$$\begin{aligned} \text{R.P} &= \frac{\rho Q (V_{p1} - V_{p2}) \times U}{1000} = \frac{\rho Q (V_{p1} - V_2) \times U}{1000} \quad (\text{negative sign since } U_2 \\ &> V_{r2} \cos \phi) = \frac{1000 \times 0.03 \times (30.54 - 9.82) \times 20}{1000} \end{aligned}$$



$$R.P = 124.32 \text{ KW}$$

### Reaction Turbine:

- In this type of Turbine the water at the inlet of the turbine possesses kinetic energy as well as Pressure energy
- As the water flows over the runner blades some part of pressure energy is changed into kinetic energy. Thus the water through runner is under pressure. The runner is completely enclosed in an airtight casing and casing and runner is always full of water.

### Types of Reaction Turbine:

#### » Radial Flow reaction Turbine

1. Inward Flow Reaction Turbine
2. Outward Flow Reaction Turbine

- Axial Flow Reaction Turbine
- Mixed flow reaction Turbine

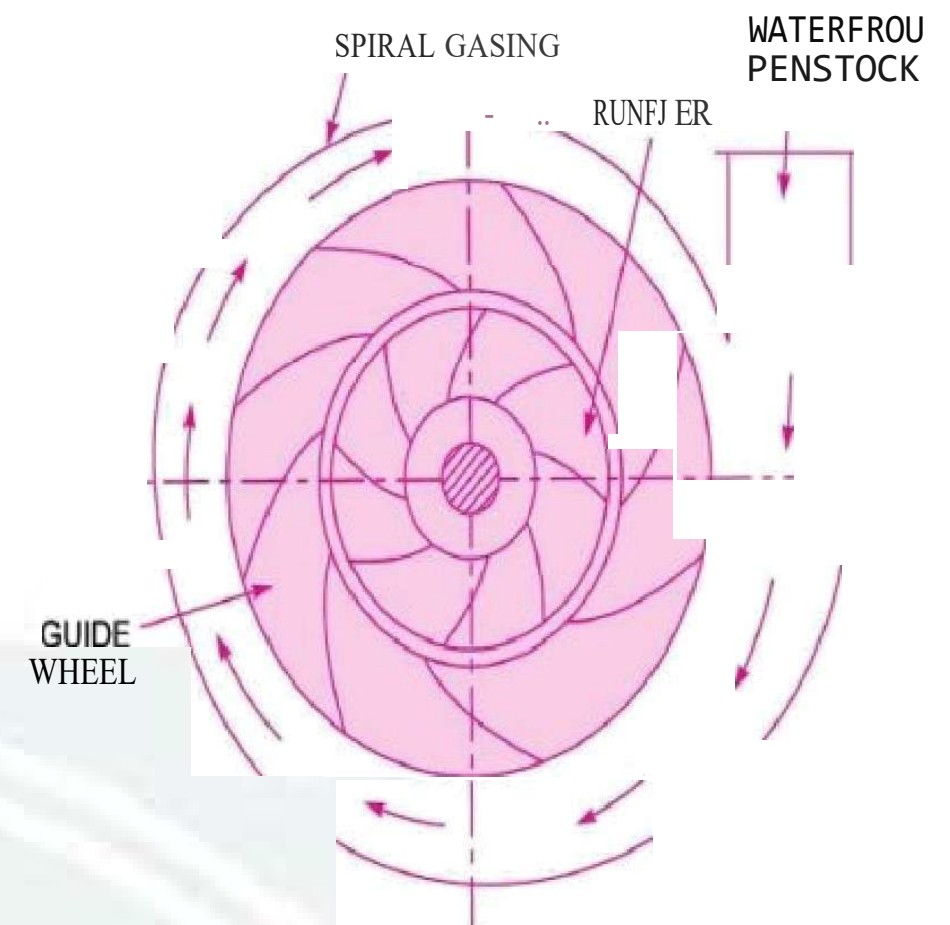
### Radial Flow Reaction Turbine:

- It is type of turbine in which the water flows in the radial direction. The water may flow from inwards to outwards or from outwards to inwards
- It is divided into two types
  1. Inward Flow Reaction Turbine
  2. Outward Flow Reaction Turbine
- o In inward flow reaction turbine ie flow of water takes place from outwards to inwards through the runner
- » In outward flow reaction turbine flow of water takes place from inwards to outwards through the runner

### Construction of Radial flow Turbine:

The following are the main parts of Radial flow turbine

- Casing
- Guide Mechanism
- Runner
- Draft Tube



### **Casing:**

- The water from penstock enters the casing which is of spiral shape in which area of section of casing goes on decreasing gradually.
- The casing completely surrounds the runner of the turbine.
- It is made spiral so that the water may enter the runner at constant velocity throughout circumference of the runner. It is made of concrete, Cast iron or plate steel.

### **Guide Mechanism:**

- It consists of a circular wheel all-round the runner of the turbine. The stationary guide vanes are fixed on the guide mechanism.
- The guide vanes allow the water to strike the vanes fixed on the runner without shock at inlet. Also by a suitable arrangement,
- The width between two adjacent vanes of guide mechanism can be altered so that the amount of water striking on runner can be varied.

### **Runner:**

- It is a circular wheel on which a series of radial curved vanes are fixed.
- The surface of vanes are made smooth.

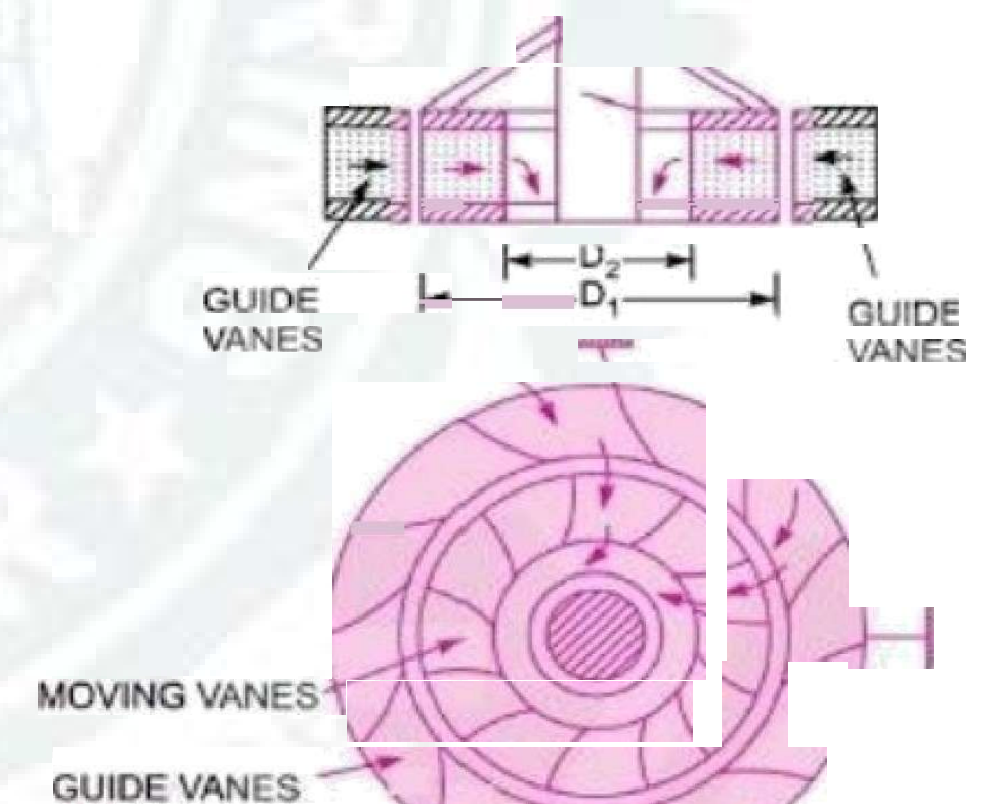
- The radial curved vanes are so shaped that water enters and leaves the runner without shock.
- The runner are made of cast steel, cast Iron or stainless steel. They are keyed to shaft

### Draft tube:

- The pressure at the exit of the runner of a reaction turbine is generally less than atmospheric pressure.
- The water at exit cannot be directly discharged to the tail race.
- A tube or pipe of gradually increasing area is used for discharging of water from exit of the turbine to the tail race.
- The tube of increasing area is called draft tube

### Inward Flow reaction Turbine:

- In an inward flow reaction turbine in which the water from casing enters the stationary guiding wheel.
- The guiding wheel consists of guide vanes which direct the water to enter the runner which consists of the moving vanes.
- The water flows over the moving vanes in the inward radial direction and is discharged at the inner diameter of the runner.
- The outer diameter of the runner is the inlet and inner diameter is the outlet.



### Velocity triangles and Work done by water on the runner:



(Inward radial Flow turbine Velocity triangle Diagram)

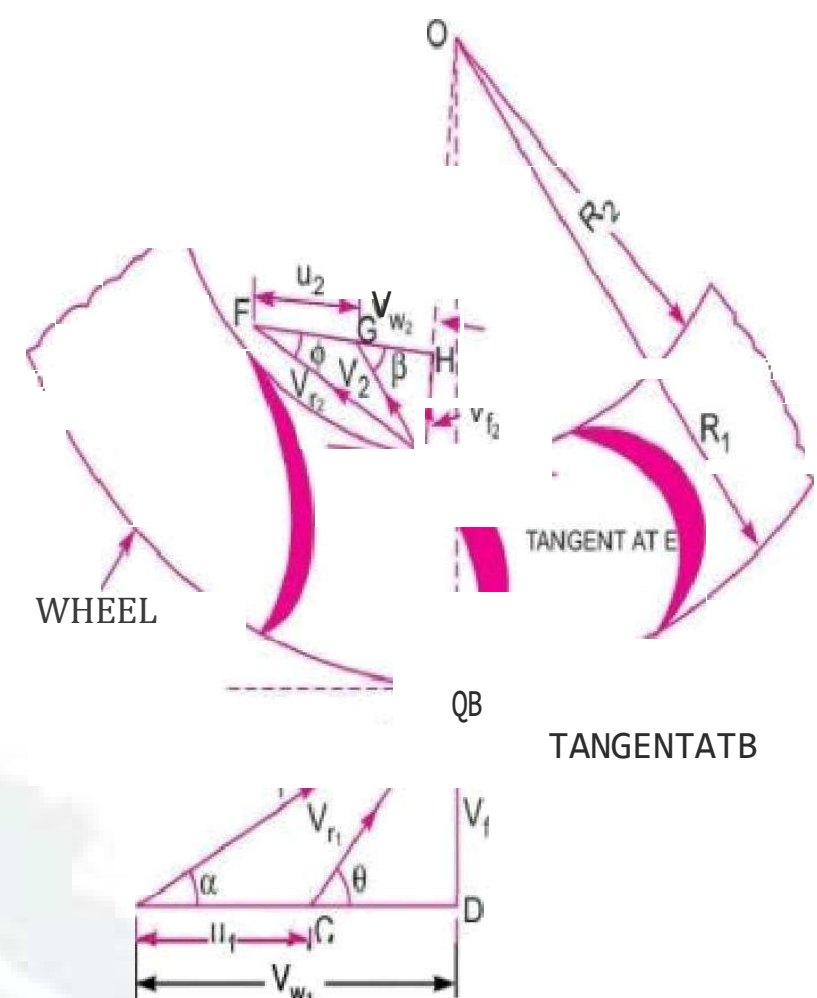
$r_1$  = Radius of wheel at inlet of vane

$r_2$  — Radius of wheel at outlet of vane

$\omega$  = Angular speed of the wheel

$$u_1 = \omega r_1, u_2 = \omega r_2$$

$$U_1 = \frac{\pi D_1 N}{60} \quad U_2 = \frac{\pi D_2 N}{60}$$



where  $D_1, D_2$  internal and outer diameter of runner respectively

$U_1, U_2$  = Tangential velocity of wheel at inlet and outlet respectively

$V_{w1}$  and  $V_{w2}$  — velocity of whirl at inlet and outlet respectively

The mass of water striking per second for a series of vane = the mass of water coming out from nozzle per second

=  $\rho a V_1$  ( $a$  = area of jet,  $V_1$  — velocity of jet)

Momentum of water striking the vane in the tangential direction per second at inlet

Mass of water per second  $\times$  component of  $V_1$  in the tangential direction

$\rho a V_1 \times V_1 \cos \alpha$  (component of  $V_1$  in the tangential direction =  $V_1 \cos \alpha = V_{w1}$ )

Momentum of water at outlet per second

= Mass of water per second  $\times$  component of  $V_2$  in the tangential direction

$\rho a V_2 \times V_2 \cos \beta$  (component of  $V_2$  in the tangential direction =  $V_2 \cos \beta = V_{w2}$ )

-ve sign is taken as the velocity  $V_2$  at outlet in opposite direction.

Angular momentum per second at inlet =

Momentum at inlet x radius at inlet =  $\rho a_1 V_1 \times r_1$

Angular momentum per second at outlet =  $\rho a_2 V_2 \times r_2$

Torque exerted by water on wheel =  $T$  Rate of change of angular momentum.

$T = [\text{Initial angular momentum per second} - \text{Final angular momentum per second}]$

$$\rho a_1 V_1 \times r_1 - \rho a_2 V_2 \times r_2$$

$$= \rho a_1 V_1 r_1 - \rho a_2 V_2 r_2$$

$$= \rho a V_1 (r_1 V_1 + r_2 V_2)$$

Work done per second on wheel = Torque x Angular velocity =  $T \omega$

$$= \rho a V_1 (r_1 V_1 + r_2 V_2) \omega$$

$$= \rho a V_1 (r_1 V_1 + r_2 V_2) \omega$$

The general expression for the work done per second is

$$W = \rho Q (V_{w1} r_1 + V_{w2} r_2) \omega$$

+ve sign will be taken if angle  $\phi$  is an Acute and  
if angle  $\phi$  is obtuse then -ve sign will be taken  
if  $\phi = 90^\circ$  then  $V_{w2} = 0$

$$\text{Water power (WP)} = \rho Q g H$$

$$\text{Runner Power (RP)} = \rho Q (V_{w1} r_1 + V_{w2} r_2) \omega / 1000$$

$$\text{Hydraulic efficiency} = \frac{V_{w1} r_1 + V_{w2} r_2}{g H}$$

Speed Ratio:

It is defined as  $\frac{U_1}{\sqrt{2 g H}}$

Flow Ratio:

It is ratio of the velocity of flow at inlet ( $V_{f1}$ ) to the velocity given 2 is known as flow ratio

$$\text{flow ratio} = \frac{V_{f1}}{\sqrt{2gH}}$$

Discharge through Turbine:

Discharge of water flows over the runner blades

$$Q = \pi D_1 B_1 V_{f1} + \pi D_2 B_2 V_{f2}$$

Where

$D_1, D_2$  — dia meter of blade at inlet and outlet respectively

$B_1, B_2$  — width of blade at inlet and outlet of runner respectively

$V_{f1}, V_{f2}$  — velocity of flow at inlet and outlet respectively

Head of turbine:

The head of turbine is algebraic sum of Pressure head and Kinetic Head. It is given by „K”

$$H = \frac{V_{f1}^2}{2g} + \frac{V_{f2}^2}{2g}$$

Q. In an inward flow reaction turbine has external and internal diameters as 0.9 m and 0.45 m respectively. The turbine is running at 200 r. p.m. and width of turbine at inlet is 200 mm. the velocity of flow through the runner is constant and is equal to 1.8 m/s. The guide blades make an angle of  $10^\circ$  to the tangent of wheel and discharge at the outlet of turbine is radial. Draw the inlet and outlet velocity triangles and determine

1. The absolute velocity of water at inlet of Runner
2. The velocity of whirl at inlet
3. The relative velocity at inlet
4. Runner blade angle
5. Width of runner at outlet
6. Mass of water flowing through runner per Sec.
7. Head at inlet of the turbine
8. Power developed and hydraulic efficiency

Solution:

Given data:

External diameter,  $D_1 = 0.9$  m

internal diameter  $D_2 = 0.45$  m  $N = 200$  Rpm

Flow velocity  $V_{f1} = V_{f2} = 1.8$  m/s

Guide blade angle  $\alpha = 10^\circ$



Discharge at outlet is Radial,  $V_{p_2} = 0$ ,  $\phi = 90^\circ$

tangential velocity of blade at inlet and outlet

$$U_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 0.45 \times 200}{60} = 9.424 \text{ m/sec}$$

$$U_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times 0.9 \times 200}{60} = 4.712 \text{ m/sec}$$

1. Absolute velocity at inlet of Runner ( $V_1$ ):

From inlet velocity triangle at inlet

$$\sin \alpha = \frac{V_{f1}}{V_1} \Rightarrow V_1 = \frac{V_{f1}}{\sin \alpha} = \frac{1.8}{\sin 10^\circ} = 10.365 \text{ m/sec}$$

$$V_1 = 10.365 \text{ m/sec}$$

2. Velocity of Whirl at inlet ( $V_{w1}$ ):

From inlet velocity triangle at inlet

$$\tan \alpha = \frac{V_{f1}}{V_{w1}} \Rightarrow V_{w1} = \frac{V_{f1}}{\tan \alpha} = \frac{1.8}{\tan 10^\circ}$$

$$V_{w1} = 10.207 \text{ m/sec}$$

3. The Relative velocity at inlet ( $V_{r1}$ ):

From inlet velocity triangle we have

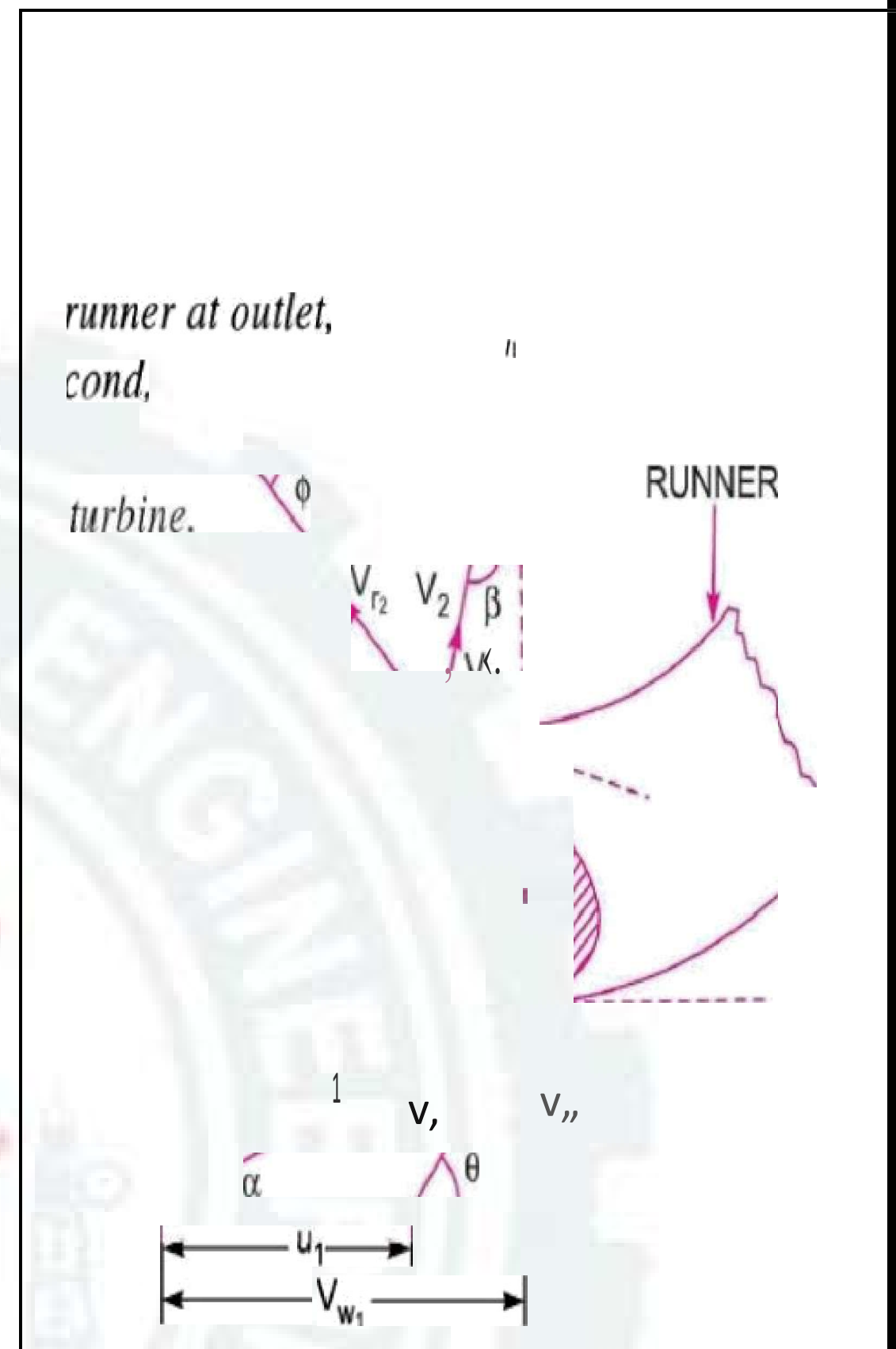
$$V_{r1} = \sqrt{V_{f1}^2 - (V_{w1} - U_1)^2}$$

$$= \sqrt{1.8^2 - (10.207 - 9.424)^2}$$

$$= \sqrt{3.24 - 0.598} = 1.65 \text{ m/sec}$$

$$= 1.65 \text{ m/sec}$$

$$= 1.65 \text{ m/sec}$$



$$1.8^2 (10.207^2 + 9.424^2)$$

$$3.24 - F_0 613 \quad 1.963 \quad /5_e$$

4. Runner blade angle ( $\theta$ ,  $Q$ )

From inlet velocity triangle

$$\tan \theta = \frac{V_{p_{off}}}{V_U} = \frac{1.8}{10.207^2 + 9.424^2} \quad \text{ZZ98}$$

$$\theta = \tan^{-1} 2.298 = 66.48^\circ$$

from outlet velocity triangle, we have

$$\tan \theta = \frac{f_{\theta}}{U} = \frac{1.8}{4.712}$$

$$\theta = \tan^{-1} \frac{1.8}{4.712} = 20.9^\circ$$

5. width of runner at outlet (02):

We have from continuity equation

$$Q = D_1 B_1 V_{f1} = D_2 B_2 V_{f2}$$

$$< D_1 B_1 = D_2 B_2 \quad \frac{D_1 B_1}{D_2} = B_2$$

$$\Rightarrow B_2 = \frac{0.90 \times 0.20}{0.45} = 0.40 \text{ m} = 400 \text{ mm}$$

$$\Rightarrow B_2 = 400 \text{ mm}$$

6. Mass of water flowing through runner per sec:  
we have

$$Q = n D_1 B_1 V_{f1} = n \times 0.9 \times 0.20 \times 1.8 = 1.0178 \text{ m}^3/\text{sec}$$

Now mass of water per sec

$$\frac{\text{Mass}}{\text{sec}} = \rho \times Q = 1000 \times 1.0178 = 1017.8 \text{ kg/sec}$$

6. Head of water at inlet of turbine:

We have already

$$H = \frac{V_{w1}^2}{2g} - \frac{V_{w2}^2}{2g} + \frac{1}{g} (V_{p1} U_1 - V_{p2} U_2) + \frac{V_{f1}^2}{2g} - \frac{V_{f2}^2}{2g}$$

$$= \frac{10.207^2}{2 \times 9.81} - \frac{1.8^2}{2 \times 9.81} + \frac{1}{9.81} (10.207 \times 9.424 - 1.8 \times 1.8) + \frac{1.8^2}{2 \times 9.81} - \frac{9.424^2}{2 \times 9.81}$$

$$= 9.97 \text{ m}$$

7. Power developed (RP):

Runner power

$$R P = \frac{1}{1000} \rho Q (V_{p1} U_1 - V_{p2} U_2) = \frac{1000 \times 1.0178 \times (10.207 \times 9.424 - 1.8 \times 1.8)}{1000}$$

$$R P = 97.9 \text{ KW}$$

8. Hydraulic Efficiency:

We have

$$\eta_h = \frac{V_{p1} U_1}{g H} = \frac{10.207 \times 9.424}{9.81 \times 9.97} = 0.9834 \text{ say } 98.34 \%$$

$$\eta_h = 98.34 \%$$

Q. A reaction turbine works at 450 rpm under a head of 120 m. its diameter at inlet is 120 cm and the flow area is 0.4 m<sup>2</sup> the angle made by absolute



velocity and relative velocity at inlet are  $20^\circ$  and  $60^\circ$  respectively with the tangential velocity :Determine

1. The volume flow rate
2. Power developed
3. Hydraulic efficiency

Assume whirl at outlet to be zero.

Solution:

Given data

internal diameter  $D_1 = 120\text{cm} = 1.2\text{ m}$

$N = 450\text{ Rpm}$  flow area  $= 0.4\text{ m}^2$

$H = 120\text{ m}$

$\beta = 60^\circ$        $\alpha = 20^\circ$

whirl at outlet to be zero,  $V_{p_2} = 0$ ,  $\beta = 90^\circ$

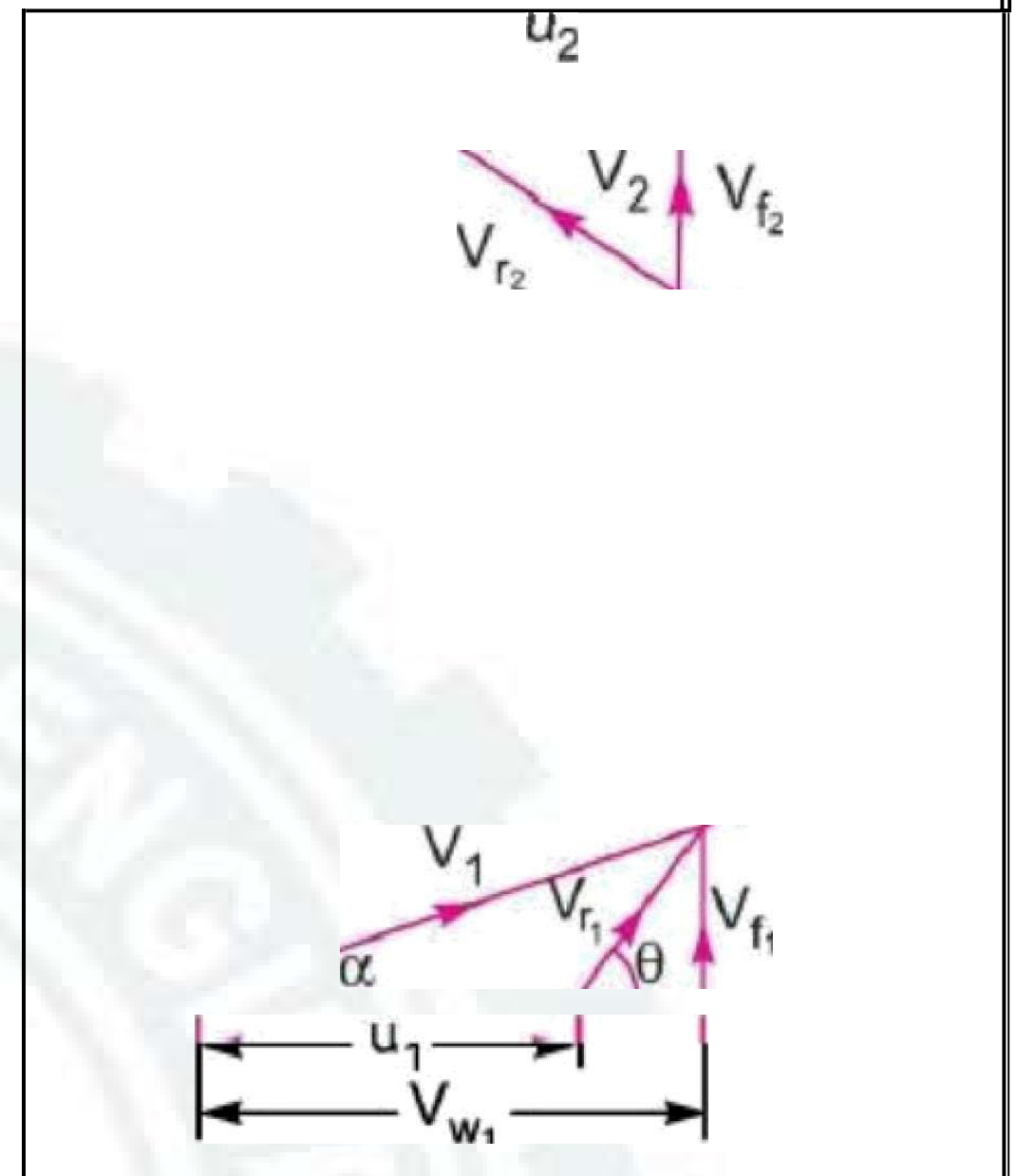
tangential velocity of blade at inlet and out let

$$U_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 1.2 \times 450}{60} = 28.27 \text{ /sec}$$

Velocity of Whirl at inlet ( $V_{w_1}$ ):

From inlet velocity triangle at inlet

$$\begin{aligned} &= \frac{V_{f_1}}{\sin \alpha} \\ &= \frac{V_{f_1}}{\sin 20^\circ} \\ &= \frac{V_{f_1}}{0.342} \\ &= \frac{V_{f_1}}{0.342} \\ &= \frac{V_{f_1}}{0.342} \\ &= \frac{V_{f_1}}{0.342} \\ &= \frac{V_{f_1}}{0.342} \\ &= \frac{V_{f_1}}{0.342} \end{aligned}$$



$$\tan \alpha = \frac{V_{w1}}{V_p} \tan 20^\circ = \frac{V_f}{U}$$

$$V_{w1} = 0.364 V_1$$

From inlet velocity triangle

$$\tan 8^\circ = \frac{V_{f1}}{U}$$

$$V_{f1} = U \times \tan 60^\circ = 0.364 V_p$$

$$V_{f1} = \frac{28.27 \times \tan 60^\circ}{48.96} = 0.364 V_p$$

$$(1.732 \times 0.364) = 35.79 \text{ m/sec}$$

Now flow velocity at inlet

$$V_{f1} = 0.364 V_p = 0.364 \times 35.79$$

$$V_{f1} = 13.027 \text{ m/sec}$$

1. volume flow rate :

We have from continuity equation

$$Q = D_1 B_1 V_{f1} = 0.4 \times 13.027 = 5.2 \frac{\text{m}^3}{\text{Sec}}$$

Power developed (RP):

$$R P = \frac{\text{Runner power}}{1000} = \frac{V_{w1} \cdot U_1}{1000} = \frac{1000 \times 5.211 \times 35.79 \times 28.27}{1000}$$

$$R P = 5272.402 \text{ KW}$$

Hydraulic Efficiency:

We have

$$\eta_h = \frac{V_{w1} \cdot U_1}{gH} = \frac{35.79 \times 29.27}{9.81 \times 120} = 0.8595 \text{ say } 85.95\%$$

Francis Turbine:

- It is inward reaction turbine having radial discharge at outlet.
- It is a medium head turbine in which the head of water is in between 50 to 250 m
- It is named after J B Francis a American Engineer.
- In modern Francis Turbine the water enters the runner of turbine in the radial direction at outlet and leaves through in the axial direction at the inlet of Runner.
- Thus it is a mixed flow reaction turbine.
- The constructional features of turbine is as like in case of Reaction Turbine.
- The velocity triangle diagram at inlet and outlet of the turbine are drawn in the same way that of inward flow reaction turbine.



As in the case of Francis turbine the discharge is radial at outlet hence whirl



Velocity at outlet is zero

As in case of Francis turbine the discharge is radial at outlet the velocity of whirl at outlet will be zero.  $V_{w,2} = 0$

Some Important Notes:

1. Discharge at Outlet is Radial

$$V_{p_2} = 0, \beta = 90^\circ$$

2. Work done by water on runner per Sec

$$R.P = \frac{\text{Work Done}}{\text{Sec}} = \frac{P \cdot W_{w,u}}{1000} \text{ KW}$$

3. Work done per Second per unit Weight of water Striking per Sec

$$\frac{\text{Work Done}}{\text{Sec}} \text{ J Unit Weight J Sec} = \frac{W_{w,u}}{g}$$

4. Hydraulic Efficiency

$$\eta_h = \frac{V_{w,u} U_i}{gH}$$

5. The flow ratio is given as

$$\text{Flow ratio} = \frac{f}{2H}, \text{ it varies from } 0.15 - 0.30$$

6. The Speed ratio

$$\text{Speed ratio} = \frac{U_i}{2H}, \text{ it varies from } 0.6 - 0.9$$

7. The ratio of width to its diameter is given by

$n = p$  —, the value of  $n$  varies 0.10 – 0.40

Q. A Francis turbine with an overall efficiency of 75% is required to produce 148.25 KW power. It is working under a head of 7.62 m. the peripheral velocity =  $0.26 \sqrt{2gxH}$  and the radial velocity of flow is  $0.96 \sqrt{2gxH}$ . The wheel runs at 150 r.p.m. and the hydraulic losses in the turbine is 22% of available energy. Assume radial Discharge, Determine:

- The Guide blade angle
- The Wheel vane angle at inlet
- Diameter of wheel at inlet
- Width of the wheel at inlet

Solution:

Given Data:

overall efficiency,  $\eta_o = \% = 0.75$

Shaft Power = 148.25 KW

$H = 7.62$  m

Peripheral Velocity,  $U_1 = 0.26 \sqrt{2gxH}$

Flow velocity  $v_f = 0.96 \sqrt{2gxH}$

speed of wheel,  $N = 150$  r. p. m

Hydraulic loss = 22% of Head( $H$ )

Discharge radial at outlet,  $V_{r2} = 0, \phi = 90^\circ$

Now we have

$$\text{Peripheral Velocity, } U_1 = 0.26 \sqrt{2gxH} = 0.26 \sqrt{2 \times 9.81 \times 7.62} = 3.179 \text{ /sec}$$

$$\text{Flow velocity } v_f = 0.96 \sqrt{2gxH} = 0.96 \sqrt{2 \times 9.81 \times 7.62} = 11.738 \text{ **/sec}$$

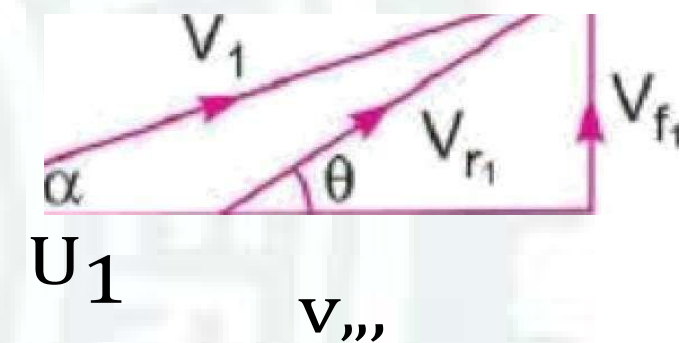
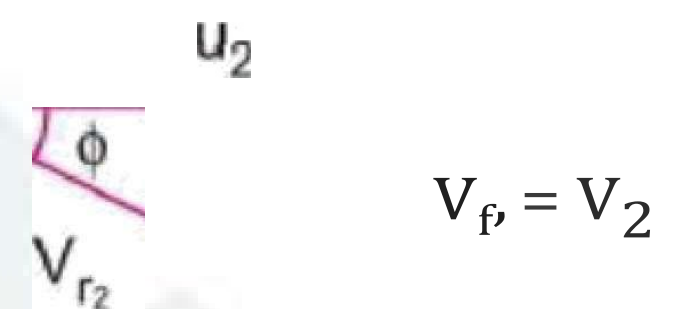
Hydraulic efficiency of turbine is given by

$$\eta_h = \frac{\text{Total head available} - \text{Hydraulic loss}}{\text{Head at inlet}} = \frac{H - 0.22H}{H} =$$

$$\eta_h = 0.78$$

- Guide Blade angle:

We know that



$$\eta_h = \frac{gH}{V_p} = \frac{gH \times \eta_h}{U_i} = \frac{9.81 \times 7.62 \times 0.78}{3.179} = 18.34 \text{ m/sec}$$

$$U_i = 18.34 \text{ m/sec}$$

from inlet velocity triangle

$$\tan \alpha = \frac{V_f}{V_{w1}} = \frac{11.738}{18.34} = 0.64$$

$$\alpha = \tan^{-1} 0.64 = 32.61^\circ$$

- ii. The wheel vane angle at inlet:  
we have from inlet velocity Triangle

$$\tan \beta = \frac{V_f}{U_i} = \frac{11.738}{18.34 - 3.179} = 0.774$$

$$\beta = \tan^{-1} 0.774 = 37.74^\circ$$

- iii. Diameter of Wheel at inlet ( $D_1$ ):  
We have peripheral Velocity

$$U_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 2 \times 250}{60} = 3.179 \text{ m/sec}$$

$$D_1 = \frac{60 \times U_1}{\pi N} = \frac{60 \times 3.179}{\pi \times 150} = 0.4047 \text{ m}$$

- iv. Width of the wheel at inlet ( $B_1$ ):

$$\eta_o = 5\% = 0.05 = \frac{W.P}{P}$$

$$W.P = \frac{\rho g Q H}{1000} = \frac{148.25}{0.75}$$



$$\Rightarrow Q = \frac{148.25 \times 1000}{0.75 \times 1000 \times 9.81 \times 7.62} = 2.644 \text{ sec}$$

$$Q' = 2.644 \text{ Sec}$$

we have discharge of water

$$Q = n D B_i \cdot M_{fg} = 2.644$$

$$\Rightarrow B_1 = \frac{2.644}{n D_1 f} = \frac{2.644}{n \times 0.4047 \times 11.738} = 0.177 \text{ m}$$

$$B_y = 0.177 \text{ m}$$

Q. The following data is given for a francis turbine. The Net head  $H = 60 \text{ m}$  speed  $N = 700 \text{ rpm}$ : shaft power =  $294.3 \text{ KW}$ : overall efficiency is  $84\%$  , Hydraulic efficiency is  $93\%$ : flow ratio is  $0.20$  breadth ratio  $n$  is  $0.1$ : Outer diameter of the runner is two times inner diameter of runner . the thickness of vanes occupy  $5\%$  of circumferential area of the runner , velocity of flow is constant at inlet and out let and discharge is radial at outlet determine:

- Guide blade angle
- Runner vane angle at inlet and outlet
- Diameters of runner in inlet

Solution:

Given Data:

Net head  $H = 60 \text{ m}$

speed  $N = 700 \text{ rpm}$

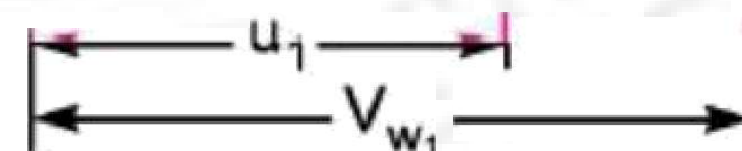
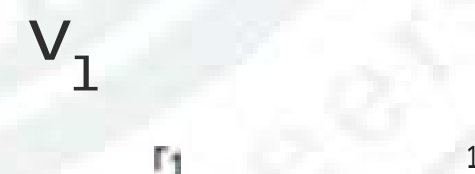
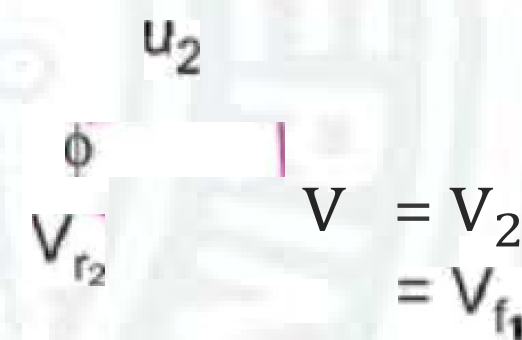
shaft power =  $294.3 \text{ KW}$ :

overall efficiency,  $\eta = 84\%$ ,

Hydraulic efficiency,  
 $\eta_h = 93\%$ :

flow ratio =  $0.20$

breadth ratio  $n = 0.1$  Outer diameter of the runner



is two times inner diameter of runner,  $D_o = 2D_i$

Flow velocity  $V_f =$  ft

Discharge Radial at outlet  $V_{r2} = 0$ ,  $V_f = v$ ,

Flow Velocity of Water:

We have flow ratio  $= \frac{V_f}{2 \times g \times H} = 0.20$

$$V_f = 0.20 \times 2 \times 9.81 \times 0 = 6.82 \text{ m/sec}$$

Discharge of water: We have overall efficiency

$$\eta_o = \frac{\text{S.P.}}{\text{W.P.}} = 84\%$$

$$\text{W.P.} = \frac{\text{S.P.}}{\eta_o} = \frac{294.3}{0.84} = 350.357 \text{ KW}$$

$$Q = \frac{\text{W.P.}}{\rho g H} = \frac{350.357 \times 1000}{1000 \times 9.81 \times 60} = 0.5952 \text{ m}^3/\text{sec}$$

$$Q = 0.5952 \text{ m}^3/\text{sec}$$

Diameter of Wheel :

we have discharge of water

$Q = \text{Actual area of flow} \times \text{Velocity of flow}$

$$Q = 0.95 \pi D_i \times B \times V_f = 0.5952$$

$$0.95 \pi D_i \times 0.1 \times V_f = 0.5952$$

$$\frac{0.5952}{0.95 \times \pi \times 0.1 \times V_f} = V_f^2$$

$$D_i = \sqrt{\left( \frac{0.5952}{0.95 \times \pi \times 0.1 \times V_f} \right)} = 0.54 \text{ m}$$

$$D_o = 2 D_i = 1.08 \text{ m}$$

$$\text{now width of blade } B = 0.1 \times 0.54 = 0.054 \text{ m}$$

Tangential velocity of runner at inlet

$$U_1 = \frac{D_o \times N}{60} = \frac{1.08 \times 700}{60} = 12.6 \text{ m/sec}$$

We have know

$$\tilde{N}_h = \frac{V_{w_1} \cdot U_1}{gH} \Rightarrow V_{w_1} = \frac{gH \times \eta_h}{U_1} = \frac{9.81 \times 60 \times 0.93}{19.79} = 27.66 \text{ m/sec}$$

$V_{p_1} = 27.66 \text{ m/sec}$  ... .. velocity of whirl at inlet  
from inlet velocity triangle

$$\tan \alpha = \frac{V_{f_1}}{V_{w_1}} = \frac{6.862}{27.66} = 0.248$$

$$\alpha = \tan^{-1} 0.248 = 13.928^\circ$$

v. The wheel vane angle at inlet:

We have from inlet velocity Triangle

$$\tan \theta = \frac{V_{f_1}}{V_{w_1} - U_1} = \frac{6.862}{27.66 - 19.79} = 0.872$$

$$\theta = \tan^{-1} 0.872 = 41.09^\circ$$

now from velocity triangle at outlet

$$U_2 = \frac{\pi D_2 N}{60} = \frac{\pi (0.54 \times 700)}{60} = 9.896 \text{ m/sec}$$

$$\tan Q = \frac{V_{f_2}}{U_2}$$

$$\therefore Q = \tan^{-1} \frac{6.862}{9.896} = 3.66^\circ$$

$$Q = 34.74^\circ$$

Axial Flow Reaction Turbine:

- If the water flows parallel to the axis of the rotation of the shaft, the turbine is known as axial flow Turbine.
- At the inlet of the turbine the Sum of pressure Energy and Kinetic energy is present and during the flow of water through runner a part of Pressure energy is converted into Kinetic energy, the turbine is called reaction turbine.
- For axial flow turbine the shaft of turbine is vertical. the lower end of the shaft is made larger which is known as hub or boss
- The vanes are fixed on the hub and hence hub acts as a runner for the axial flow turbine.



- The following are the important types of axial flow turbine.

1. Propeller Turbine
2. Kaplan Turbine

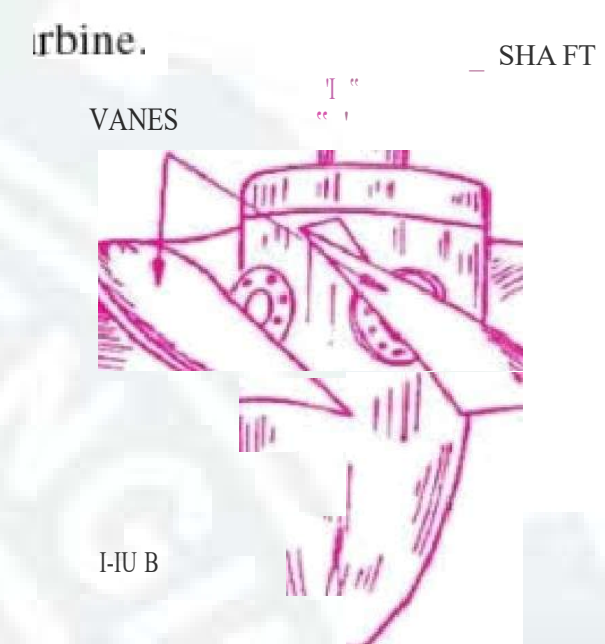
### Kaplan Turbine:

- It is named after the Austrian Engineer V Kaplan
- It is a Low Head Turbine i.e. Head available at inlet is below 50 m
- It is suitable where a large Quantity of water at low head available.
- It is type of axial flow turbine in which the vanes on the hub are adjustable.

### Construction & Working Principle

It consists of following Parts

1. Scroll Casing
2. Guide Vanes Mechanism
3. Hub with vanes or runner of the Turbine
4. Draft Tube



### Scroll Casing:

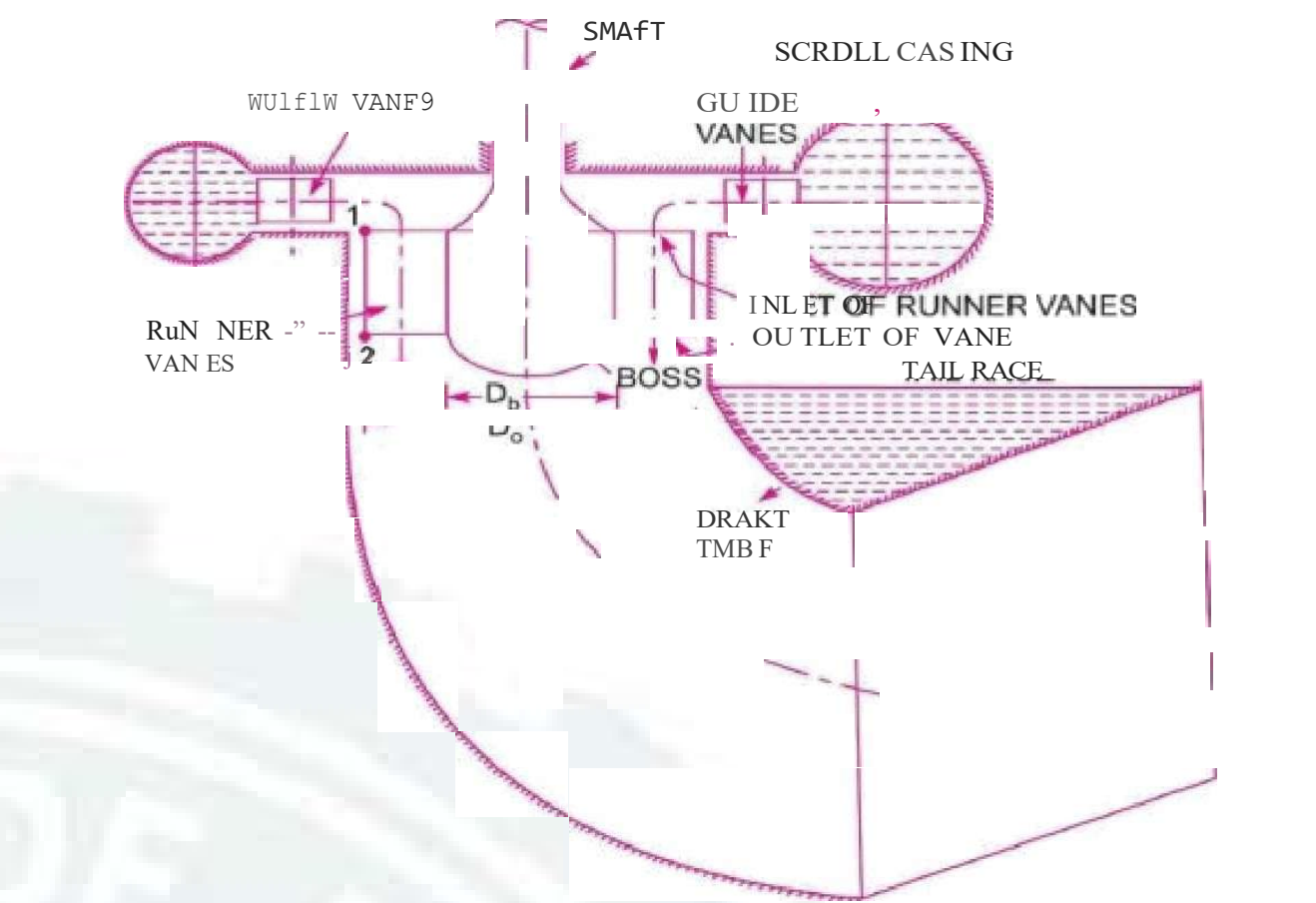
- It is a spiral type of casing that has decreasing cross section area. The water from the penstocks enters the scroll casing and then moves to the guide vanes where the water turns through  $90^\circ$  and flows axially through the runner.
- Runner: Runner Blades are the blades that are rotated by the flow of water. In Kaplan turbines, runner blades has twist along its length and are adjustable to an optimum angle for maximum power output.

### Draft Tube:

- A tube or pipe of gradually increasing area is used for discharging water from the exit of turbine to the tail race. This tube of increasing area is called Draft Tube.

### Working Principle:

- The water coming from the pen-stock is made to enter the scroll casing. The scroll casing is made in the required shape that the flow pressure is not lost.
- The guide vanes direct the water to the runner blades. The vanes are adjustable and can adjust itself according to the requirement of flow rate.
- The water takes a 90 degree turn, so the direction of the water is axial to that of runner blades. The runner blades start to rotate as the water strikes due to reaction force of the water.
- The rotation of the turbine is used to rotate the shaft of generator for electricity production.



Important points:

From velocity triangle (Inlet and Outlet)

$$V_2 = V_{fg} \cdot r, = 0$$

1. The peripheral velocity in inlet and outlet

$$U_1 = U_2 = \frac{nD}{60}$$

2. Velocity of flow at inlet and outlet are equal

$$V_{f1} = V_{f2}$$

3. Area of flow at inlet equal to area of flow at outlet

$$= \frac{\pi}{4} (D_o^2 - D_b^2) \times V_{f1}$$

4. Discharge of water

$$Q = \frac{\pi}{4} (D_o^2 - D_b^2) \times V_{f1}$$

5. Hydraulic Efficiency

$$\eta_h = \frac{U}{gH}$$

Q. A Kaplan Turbine working under a head of 20 m develops 11772 KW shaft Power. The outer diameter of the runner is 3.5 m and hub diameter is 1.75m. The Guide blade angle at the extreme edge of the runner is 35degree. The hydraulic and overall efficiencies of the turbines are 88% and 84% respectively. If the velocity of wheel is zero at outlet Determine:

- Runner vane angles at inlet and outlet at the extreme edge of the turbine
- Speed of the Turbine

Given Data:

Net head  $H = 20$  m

shaft power = 11772 KW:

overall efficiency,  $\eta_o = 84\%$ ,

Hydraulic efficiency,  $\eta_h = 88\%$ :

flow ratio = 0.20

breadth ratio  $n = 0.1$

Outer diameter of the runner  $D = 3.5$  m

Inner diameter of runner,  $D_h = 1.75$  m

Guide blade angle  $\alpha = 35^\circ$

Flow velocity  $V_f = V_f$

Discharge Radial at outlet,  $V_{r2} = 0$ ,  $V_{f2} = v_2$

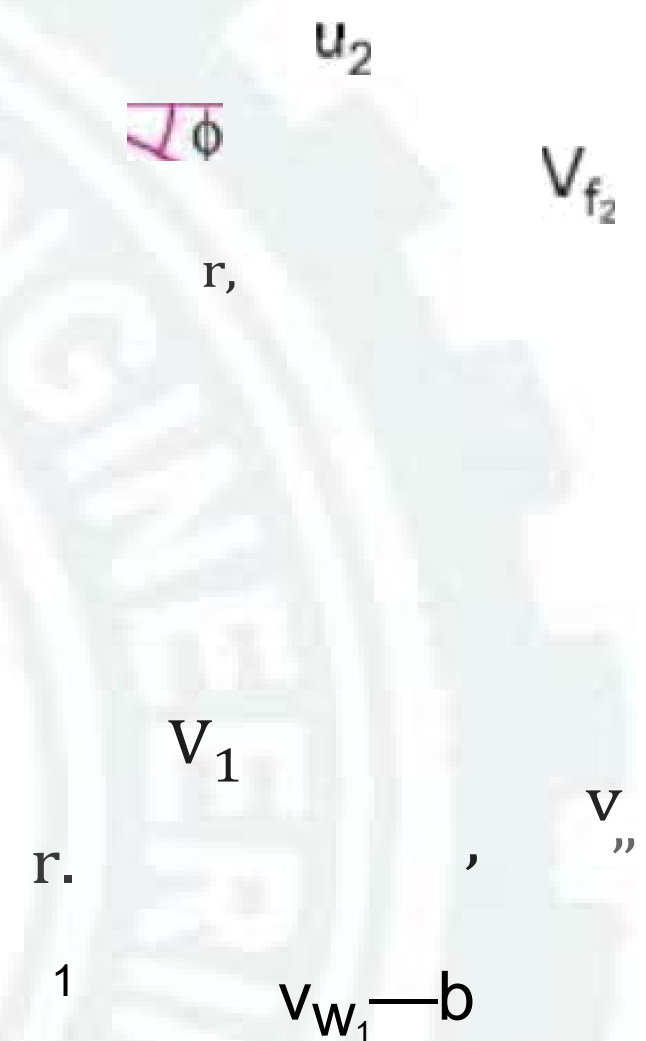
Flow Velocity of Water:

Discharge of water:

We have overall efficiency

$$\eta_o = \frac{S.P.}{W.P.} = 84\%$$

$$W.P. = \frac{S.P.}{\eta_o} = \frac{11772}{0.84} = 1401428 \text{ KW}$$





$$W.P = \frac{\rho g Q H}{1000} = 14014.28$$

$$Q = \frac{1000 \times 14014.28}{\rho g H} = \frac{1000 \times 14014.28}{1000 \times 9.81 \times 20} = 71.428, \text{ }^3 \text{ Sec}$$

$$Q = 71.428, \text{ }^3 \text{ Sec}$$

Diameter of Wheel :

we have discharge of water  $Q = \text{Actual area of flow} \times \text{Velocity of flow}$

$$Q = \left( \frac{D_o^2 - D_b^2}{4} \right) \times V_f = 71.428$$

$$V_f = \frac{71.428}{\left( \frac{D_o^2 - D_b^2}{4} \right)} = \frac{71.428}{\left( \frac{3.5^2 - 1.75^2}{4} \right)} = 9.9 \text{ m/sec}$$

from inlet velocity triangle

$$\tan \phi = \frac{V_f}{V_{w1}} = \frac{6.862}{27.6} = 0.2486$$

$$\phi = \tan^{-1}(0.2486) = 14.14^\circ$$

We have known that Hydraulic efficiency

$$\eta_h = \frac{V_{w1} \cdot U_1}{gH}$$

$$\Rightarrow U_1 = \frac{gH \times \eta_h}{V_{w1}} = \frac{9.81 \times 20 \times 0.88}{14.14} = 12.21 \text{ m/sec}$$

Speed of Runner:

Tangential velocity of runner at inlet

$$U_1 = 12.21 \text{ m/sec}$$

$$N = \frac{60 \times U_1}{\pi \times D \times \sin \phi} = 63 \text{ R.P.M}$$

- vi. The wheel vane angle at inlet:  
We have from inlet velocity Triangle

$$\tan \theta = \frac{V_f}{U_1 - U_2} = \frac{9.9}{14.14 - 12.21} = 5.13$$

$$\theta = \tan^{-1} 5.13 = 78.97^\circ$$

now from velocity triangle at outlet

For Kaplan Turbine, Tangential Velocity at inlet and outlet,  $U_2 = U_1 = 12.21 \text{ sec}$

$$\tan Q = \frac{V_{fg}}{U_2} \Rightarrow Q = \tan^{-1} \frac{V_{fg}}{U_2} = \tan^{-1} \frac{9.9}{12.21} = 39.035^\circ$$

$$Q = 39.035^\circ$$

Q. The hub diameter of a Kaplan turbine working under a head of 12 m is 0.35 times the diameter of the runner. The turbine is running at 100 rpm. If the vane angle of the extreme edge of the runner at outlet is 15 degree. And flow ratio 0.6

Find.

- Diameter of Runner
- Diameter of Boss
- Discharge through the runner

The velocity of whirl at outlet is given as zero.

Solution:

Given Data:

Net head  $H = 12 \text{ m}$

speed  $N = 100 \text{ rpm}$

$Q = 15$

flow ratio = 0.20

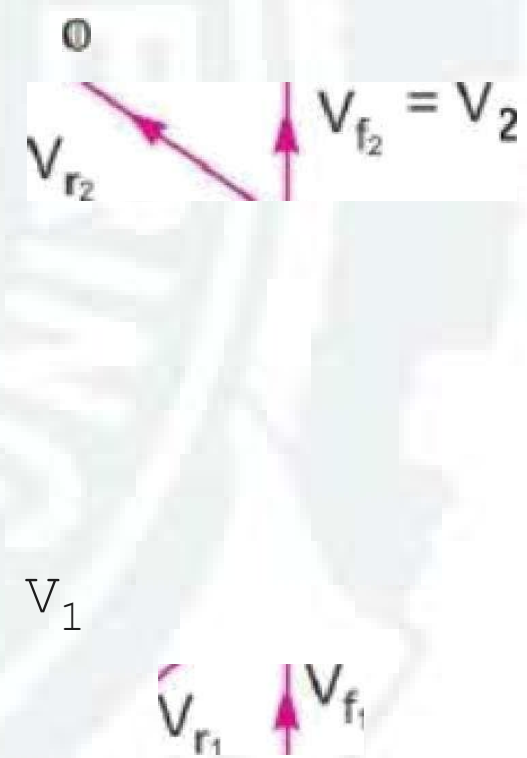
$D_b = 0.3 D_o$

Outer diameter of the runner is two times inner diameter of runner,  $D_o = 2 D_b$

Flow velocity  $V_{f1} = V_f$

Discharge Radial at outlet  $V_{p,0}, V_{f2} = v_2$

Flow Velocity of Water



$$\text{We have flow ratio} = \frac{V_{ft}}{\sqrt{2 \times g \times H}} = 0.6$$

$$V_{ft} = 0.6 \sqrt{2 \times 9.81 \times 12} = 9.2 \text{ m/sec}$$

now from velocity triangle at outlet

$$\tan \alpha = \frac{V_{f2}}{U_2}$$

$$\Rightarrow U_2 = \frac{V_{f2}}{\tan \alpha} = \frac{9.2}{\tan 15^\circ} = 34.55 \text{ m/sec}$$

$$V_{w1} = V_{w2} = 34.55 \text{ m/sec}$$

$$\text{we have tangential velocity, } U_2 = \frac{\pi D N}{60}$$

$$D_o = \frac{U_2 \times 60}{\pi \times 100} = \frac{34.55 \times 60}{\pi \times 100} = 6.55 \text{ m}$$

$$D_o = 6.55 \text{ m} \dots \dots \dots \text{Diameter of Runner}$$

$$\text{We have from above data } D_b = 0.35 \times D = 0.35 \times 6.35 = 2.3 \text{ m}$$

$$D_b = 2.3 \text{ m} \dots \dots \dots \text{Diameter of Boss}$$

we have discharge of water = Actual area of flow  $\times$  Velocity of flow

$$Q = \frac{\pi}{4} (D_o^2 - D_b^2) V_{f2} = \frac{\pi}{4} (6.55^2 - 2.3^2) \times 9.2 = 271.77 \text{ m}^3/\text{sec}$$

Impulse Turbine	Reaction Turbine
1. Energy available at inlet is Kinetic Energy	1. Energy available at inlet is sum of Kinetic Energy and Pressure energy
2. It is high head turbine	2. it may be Medium or low head Turbine
3. The flow of water is in a tangential direction upon the runner blades	3. It is Radial flow, Axial flow or mix flow type turbine
4. It produces more mechanical energy	4. It produces quietly less than impulse turbine.
5. The striking of water produces shock in blades of Runner	5. The flow of water is smooth on the curved blades
6. The turbine does not run full and air has a free access to the bucket	



7. No use of Draft tube

8. Flow regulation is done by means of Needle valve fitted in to Nozzle

9. Example : Pelton Wheel

6. Water completely fills at the passage between blade and wheel

7. Draft tube is used to drag the water at outlet of Runner

8. Flow regulation is carried out by means of Guide vane Mechanism ,Scroll Casing

9. Example: Francis Turbine, Kaplan Turbine



# Chapter 2

## Syllabus

### CENTRIFUGAL PUMPS

2.1 Construction and working principle of centrifugal pumps

2.2 work done and derivation of various efficiencies of centrifugal pumps.

2.3 Numerical on above



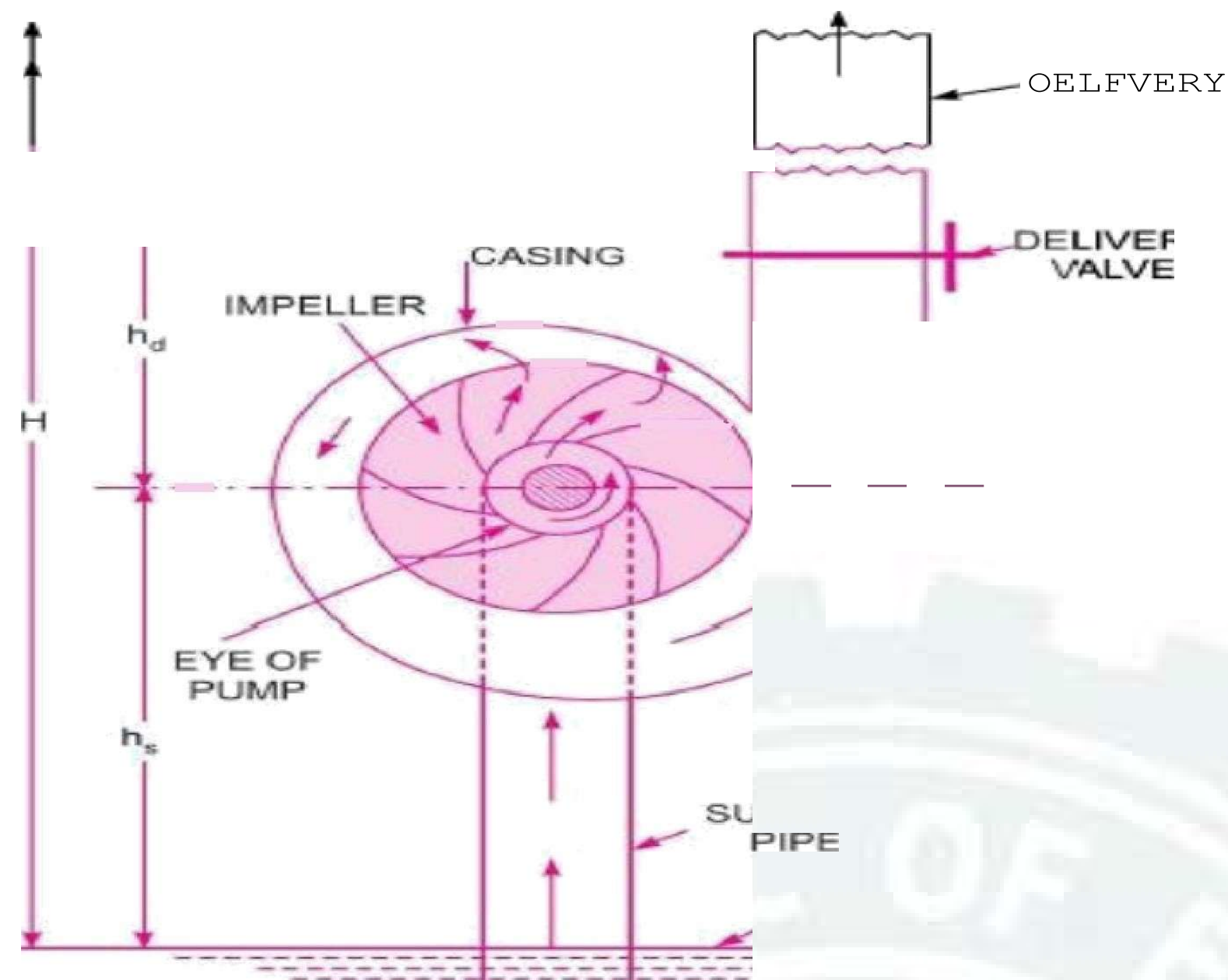
## introduction-

- s The hydraulic machines which convert the mechanical energy into hydraulic energy are called as pump.
- Pump is a device which transmits a fluid under pressure from one location to other location
- It converts Mechanical energy into Hydraulic energy.
- It is driven by Prime Mover like motor, Diesel engine etc.
- The hydraulic energy is in the form of pressure energy.
- [Centrifugal Force- Centrifugal force is the tendency of an object moving in a circle to travel away from the center of the circle.]
- It acts as a reverse of an inward radial flow reaction turbine
- e The flow in the centrifugal pump will be radially outward direction.
- It works on the principle of Force Vertex which means a certain mass of liquid is rotated by an external torque, thus the rise in pressure head of rotating liquid takes place.
- Due to high Pressure head the liquid can be delivered to a high level

## Construction –

- Main parts are
- Impeller
- Casing
- Suction pipe with a foot valve and a strainer
- Delivery pipe





### Impeller —

- The rotating part of centrifugal pump is called impeller.
- It consists of a series of backward curved vanes.
- The impeller is mounted on a shaft which is connected to the shaft of an electric motor

### Casing —

- It is similar to the casing of reaction Turbine
- It is an air tight passage surrounding the impeller of the pump.
- It is designed in such a way that the area of flow of water is gradually increases so that kinetic energy of water discharge at the outlet of impeller is converted into Pressure energy before the water leaves the casing and enters the delivery pipe
- 3 types of casing there volute casing, vortex casing, casing with guide blades.

## Suction pipe with a foot valve and a strainer—

- A pipe whose one end is connected to the inlet of the pump and other end dips into water in a sump is known as suction pipe.
- The suction of water is carried out in this pipe
- A foot valve is a Non Return Valve or one way type of Valve which allow the flow of water in one direction i.e. flow water from Sump to the Casing only
- Foot Valve is attached at the lower end of Suction Pipe
- A strainer is also fitted at the lower end of the Suction Pipe.
- It prevents the entry of foreign bodies in to the suction pipe.

## De l i e P i e

- A pipe whose one end is connected to the outlet of casing of pump and other end delivers the water at required height is known as delivery pipe.
- The diameter of delivery pipe should be less than the diameter of Suction Pipe

## Working

- The first step in the operation of a centrifugal pump is priming.
- It works on the principle that when a certain mass of fluid is rotated by an external source, it is thrown away from the center of axis of rotation and a centrifugal head is impressed which enables it to rise to a higher level.
- The delivery valve is closed and the pump is primed that is, suction pipe, casing and portion of delivery pipe up to delivery valve are completely filled with the liquid (to be pumped) so that no air pocket is left.

- Keeping the delivery valve closed the electric motor is started to rotate the impeller.
- The rotation of impeller causes strong action or vacuum just at the eye of casing.
- The speed of the impeller is gradually increased till the impeller rotates at its normal speed and normal energy required for pumping the liquid.
- After the impeller attains the normal speed the delivery valve is opened when the liquid is continuously sucked up the suction pipe, it passes through the eye of casing and enters the impeller at its center.
- This liquid is impelled out by the rotating vanes and it comes out at the outlet tips of the vanes into the casing.
- Due to impeller action the pressure head as well as velocity head of the liquid head are increased.
- From casing, the liquid passes into pipe and is lifted to the required height discharged from the outlet / upper end of the delivery pipe.
- So long as motion is given to the impeller and there is supply of liquid to be lifted, the process of lifting the liquid to the required height remains continuous
- When pump is to be stopped the delivery valve should be first closed, otherwise there may be some backflow from the reservoir.

Work done by the centrifugal pump

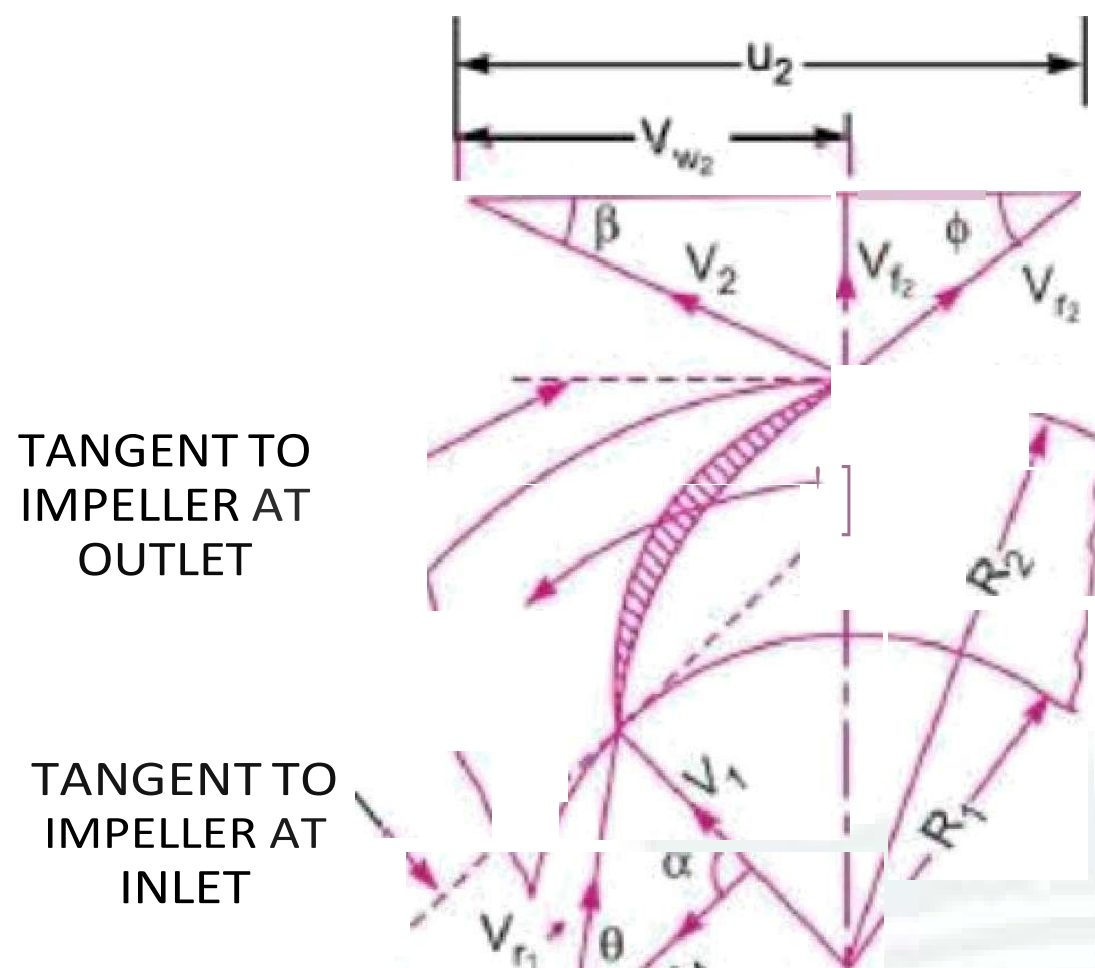
- The water enters the impeller radially at inlet for best efficiency of the pump.



- Absolute velocity of water at inlet makes an angle of 90 degree with the direction of motion of the impeller at inlet.
- Angle  $\alpha = 90^\circ$ , and  $F_{r1} = 0$
- $N$  = Speed of the impeller in rpm
- $D_1$  = Diameter of impeller at inlet
- $u_1$  = Tangential velocity of impeller at inlet

$$p_1 - p_2 = \frac{\rho \pi D_1^3 N^2}{60^2}$$

- $D_1$  -- Diameter of impeller at inlet
- $D_2$  = Diameter of impeller at outlet.
- $u_2$  = Tangential velocity of impeller at outlet
- $u_2 = \frac{\pi D_2 N}{60}$
- $V_1$  = Absolute velocity of water at inlet
- $V_{r1}$  = Relative velocity of water at inlet
- $\alpha =$  Angle made by absolute velocity  $V_1$  at inlet with the direction of motion of blade.
- $\beta =$  Angle made by relative velocity  $V_{r1}$  at inlet with the direction of motion of blade.
- $V_2$ ,  $V_{r2}$  and  $g$  are corresponding values at outlet.



- A centrifugal pump is the reverse of a radially inward flow reaction turbine.
- In case of radially inward flow reaction turbine the work done is  
 $W = \rho Q [V_{w1} u_1 - V_{w2} u_2]$   
 Work done by the impeller = -(work done in case of turbine)  
 $= -\rho Q [V_{w1} u_1 - V_{w2} u_2] = \rho Q [V_{w2} u_2 - V_{w1} u_1]$
- $W = \rho g [V_{w2} u_2 - V_{w1} u_1] \quad (V_{w1} = 0, \alpha = 90^\circ)$
- Work done by impeller on the water per second per unit weight =  
 $\frac{W}{\rho g} = \frac{\rho Q [V_{w2} u_2 - V_{w1} u_1]}{\rho g} = \frac{Q}{g} [V_{w2} u_2 - V_{w1} u_1]$   
 Where  $W$  = Weight of water =  $\rho \times g \times Q$   
 $Q$  = Area  $\times$  Velocity of flow =  $\pi D_1 B_1 \times V_{f1} = \pi D_2 B_2 \times V_{f2}$   
 Where  $B_1$  and  $B_2$  = width of impeller at inlet and outlet are  
 $V_{f1}$  and  $V_{f2}$  are velocity of flow at inlet and outlet.

### Heads of Pump:

There are four types of head

1. Suction Head
2. Delivery Head
3. Manometric Head

#### 4. Static Head

Suction Head: it is the vertical height of the center line of the centrifugal pump above the water surface in the tank or pump from which water is to be lifted.

It is denoted by symbol 'h<sub>s</sub>'

Delivery Head

The Vertical distance between the center line of the pump and the water surface in the tank to which water is delivered is known as delivery head.

It is denoted by symbol 'h<sub>d</sub>'

Static Head:

The sum of suction and delivery head is known as static head.

It is denoted by symbol 'H<sub>s</sub>'.

Manometric Head:

It is defined as the head against which a centrifugal pump has to work

It is denoted by the symbol 'H<sub>m</sub>'.

Efficiencies of centrifugal pump —

- Mechanical Efficiency:

It is the ratio of power available at the impeller to the power supplied to the impeller. It is denoted by 'η<sub>mech</sub>'

$$\eta_{mech} = \frac{\text{power available at impeller}}{\text{power supplied to impeller}} = \frac{pQ(Vp_2 \cdot U_2)}{\text{Shaft power}}$$

$$\eta_{mech} = \frac{q(v \cdot 2 U_z)}{\text{shaft power}}$$



- Manometric Efficiency:

It is the ratio of output power of the pump to power available at the impeller.

It is denoted by symbol ' $\eta_{man}$ '

$$\eta_{man} = \frac{\text{output power of impeller}}{\text{power available at impeller}} = \frac{\text{WaterPower}}{gq(v_{p_z} \cdot U_2)}$$

$$\eta_{man} = \frac{pgQH_g - \frac{gH_g}{V_2 U_2}}{p_o(\dots)}$$

a Overall Efficiency:

It is the ratio of the output power of pump to the input power of pump.

It is denoted by symbol ' $\eta_o$ '

$$\eta_o = \frac{\text{output power of impeller}}{\text{power available at inlet of impeller}} = \frac{\text{WaterPower}}{\text{Shaft power}}$$

$$\eta_{man} = \frac{pgQH_p}{p}$$

## Numerical

**Problem 19.1** The internal and external diameters of the impeller of a centrifugal pump are 200 mm and 400 mm respectively. The pump is running at 1200 r.p.m. The vane angles of the impeller at inlet and outlet are  $20^\circ$  and  $30^\circ$  respectively. The water enters the impeller radially and velocity of flow is constant. Determine the work done by the impeller per unit weight of water.

**Solution.** Given :

Internal diameter of impeller,  $D_1 = 200 \text{ mm} = 0.20 \text{ m}$

External diameter of impeller,  $D_2 = 400 \text{ mm} = 0.40 \text{ m}$

Speed,  $N = 1200 \text{ r.p.m.}$

Vane angle at inlet,  $\theta = 20^\circ$

Vane angle at outlet,  $\phi = 30^\circ$

Water enters radially\* means,  $\alpha = 90^\circ$  and  $U_{r1} = 0$

Velocity of flow,  $V = V_z$

Tangential velocity of impeller at inlet and outlet are.

$$u_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 0.20 \times 1200}{60} = 12.56 \text{ m/s}$$

and

$$u_2 = \frac{\pi \times 0.40 \times 1200}{60} = 25.13 \text{ m/s}$$

$$\text{From inlet velocity triangle, } \tan \theta = \frac{V_{f1}}{u_1} = \frac{V_{f1}}{12.56}$$

$$V_{f1} = 12.56 \tan 20^\circ = 12.56 \times \tan 20^\circ = 4.57 \text{ m/s}$$

$$V_{f2} = V_{f1} = 4.57 \text{ m/s}$$

$$\text{From outlet velocity triangle, } \tan \phi = \frac{V_{f2}}{u_2 - V_{w2}}$$

or

$$25.13 - V_{w2} = \frac{4.57}{\tan 30^\circ} = 4.57 \times \sqrt{3} = 7.915$$

$$V_{w2} = 25.13 - 7.915 = 17.215 \text{ m/s}$$

The work done by impeller per kg of water per second is given by equation (19.11) as

$$W = \frac{1}{g} V_{w2} u_2 = \frac{17.215 \times 25.13}{9.81} = 44.1 \text{ J/kg} = 44.1 \text{ m} \text{ Ans.}$$

**Problem 19.2** A centrifugal pump is to discharge 0.118 m<sup>3</sup>/s at a speed of 1450 r.p.m. against a head of 25 m. The impeller diameter is 250 mm, its width at outlet is 50 mm and manometric efficiency is 75%. Determine the vane angle at the outer periphery of the impeller.

**Solution.** Given :

Discharge,  $Q = 0.118 \text{ m}^3/\text{s}$

Speed,  $N = 1450 \text{ r.p.m.}$

Head,  $H = 25 \text{ m}$

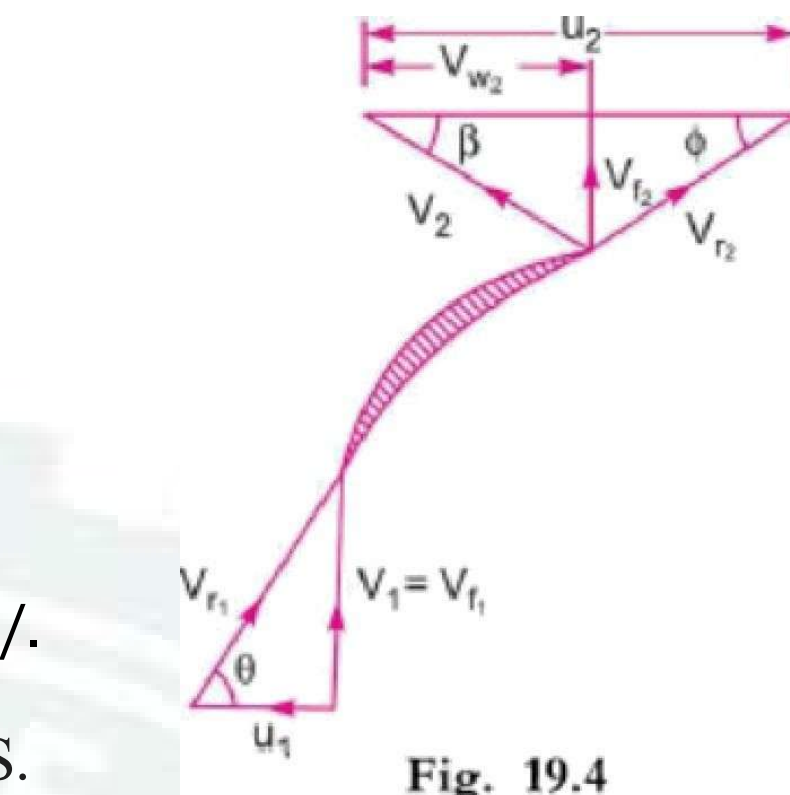
Diameter at outlet,  $D_2 = 250 \text{ mm} = 0.25 \text{ m}$

Width at outlet,  $b_2 = 50 \text{ mm} = 0.05 \text{ m}$

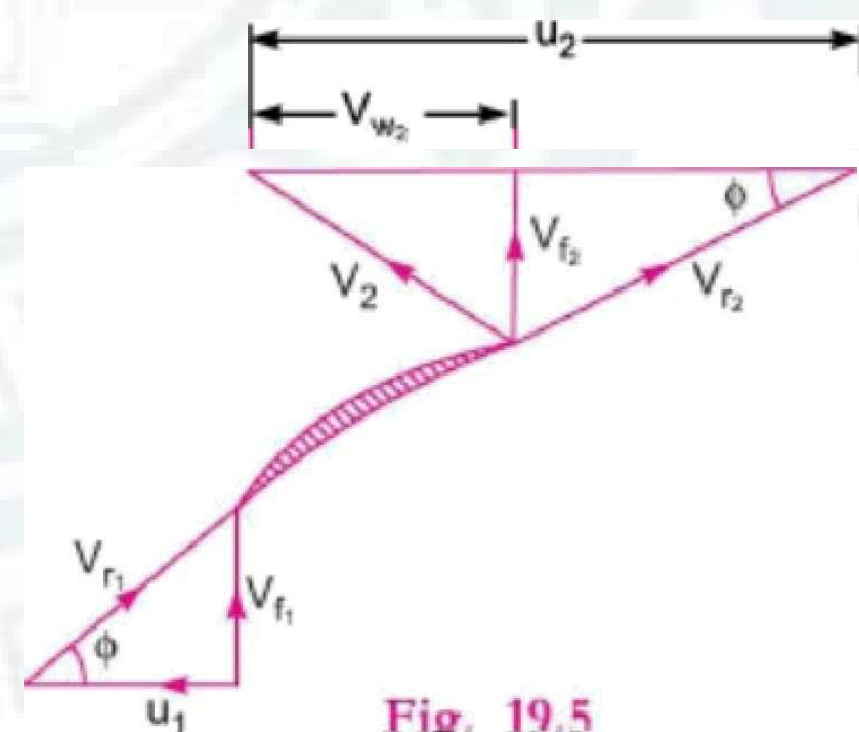
Manometric efficiency,  $\eta_m = 75\% = 0.75$

Let vane angle at outlet =  $\phi$

Tangential velocity of impeller at outlet,



**Fig. 19.4**



**Fig. 19.5**

Discharge is given by

$$Q = \pi D_2 B_2 \times V_{f2}$$

$$V_{f2} = \frac{Q}{\pi D_2 B_2} = \frac{0.118}{\pi \times 0.23 \times 0.05} = 16.3 \text{ m/s}$$

Using equation (19.8),

$$\phi = \frac{g H_m}{V_{f2}^2} = \frac{9.81 \times 25}{16.3^2} = 0.91$$

∴

$$V_{f2} = \frac{9.81 \times 25}{0.91} = 27.1 \text{ m/s}$$

From outlet velocity triangle, we have

$$\tan \phi = \frac{V_{f2}}{V_{w2}} = \frac{27.1}{16.3} = 1.66$$

∴

$$\phi = \tan^{-1} 1.66 = 59.74^\circ \text{ or } 59^\circ 44'. \text{ Ans.}$$

**Problem 19.3** A centrifugal pump delivers water against a net head of 14.5 metres and a design speed of 1000 r.p.m. The vanes are curved back to an angle of  $30^\circ$  with the periphery. The impeller diameter is 300 mm and outlet width is 50 mm. Determine the discharge of the pump if manometric efficiency is 95%.

**Solution:** Given:

Net head,

$$H_m = 14.5 \text{ m}$$

Speed,

$$N = 1000 \text{ r.p.m.}$$

Vane angle at outlet,

$$\phi = 30^\circ$$

Impeller diameter means the diameter of the impeller at outlet

Diameter,

$$D_2 = 300 \text{ mm} = 0.3 \text{ m}$$

Outlet width,

$$B_2 = 50 \text{ mm} = 0.05 \text{ m}$$

Manometric efficiency,  $\eta_{gm} = 95\% = 0.95$

Tangential velocity of impeller at outlet,

$$V_{w2} = \frac{\pi D_2 N}{60} = \frac{\pi \times 0.3 \times 1000}{60} = 15.7 \text{ m/s}$$

$$\text{Now using equation (19.8), } \phi = \frac{g H_m}{V_{w2}^2} = \frac{9.81 \times 14.5}{15.7^2} = 0.38$$

∴

$$V_{f2} = \frac{V_{w2} \tan \phi}{\tan 30^\circ} = \frac{15.7 \times 0.38}{0.577} = 10.3 \text{ m/s}$$

Refer to Fig. 19.5. From outlet velocity triangle, we have

$$\tan \phi = \frac{V_{f2}}{V_{w2} - V_{f2}} \text{ or } \tan 30^\circ = \frac{10.3}{15.7 - 10.3} = 1.9$$

∴

$$V_{f2} = 15.7 - 10.3 = 5.4 \text{ m/s}$$

Discharge,

$$Q = \pi D_2 B_2 \times V_{f2}$$

$$= \pi \times 0.3 \times 0.05 \times 5.4 = 0.254 \text{ m}^3/\text{s} \text{ Ans.}$$



Problem 19.4 A centrifugal pump has an outer diameter equal to five times the inner diameter and running at 1000 r.p.m. works against a total head of 40 m. The velocity of flow through the impeller is constant and equal to 2.5 m/s. The vanes are set back at an angle of  $40^\circ$  at outlet. If the outer diameter of the impeller is 500 mm and width at outlet is 50 mm, determine :

- (i) Vane angle at inlet, (ii) Work done by impeller on water per second, and  
 (iii) Manometric efficiency.

Solution. Given :

Speed,  $N = 1000$  r.p.m.  
 Head,  $H = 40$  m  
 Velocity of flow,  $V_f = V_{f1} = 2.5$  m/s  
 Vane angle at outlet,  $\phi = 40^\circ$   
 Outer dia. of impeller,  $D = 500$  mm = 0.50 m  
 Inner dia. of impeller,  $D_1 = \frac{D}{5} = \frac{500}{5} = 0.25$  m  
 Width at outlet,  $B_2 = 50$  mm = 0.05 m  
 Tangential velocity of impeller at inlet and outlet are

$$u_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 0.25 \times 1000}{60} = 13.09 \text{ m/s}$$

and

$$u_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times 0.50 \times 1000}{60} = 26.18 \text{ m/s}$$

Discharge is given by,  $Q = \pi D_2 B_2 V_f = \pi \times 0.50 \times 0.05 \times 2.5 = 0.1963 \text{ m}^3/\text{s}$ .

(i) Vane angle at inlet.

From inlet velocity triangle  $\tan \theta = \frac{V_{f1}}{u_1} = \frac{2.5}{13.09} = 0.191$

$$\theta = \tan^{-1} 0.191 = 10.81^\circ \text{ or } 10^\circ 48'' \text{ Ans.}$$

(ii) Work done by impeller on water per second is given by equation (19.2) as

$$= \frac{W}{g} \times V_{w2} u_2 = \frac{\rho \times g \times Q}{g} \times V_{w2} \times u_2$$

$$= \frac{1000 \times 9.81 \times 0.1963}{9.81} \times V_{w2} \times 26.18$$

But from outlet velocity triangle, we have

$$\tan \phi = \frac{V_{f2}}{u_2 - V_{w2}} \Rightarrow \frac{2.5}{26.18 - V_{w2}} = \tan 40^\circ = 0.8391$$

$$26.18 - V_{w2} = \frac{2.5}{0.8391} = 2.979$$

$$V_{w2} = 26.18 - 2.979 = 23.2 \text{ m/s}$$

Substituting this value of  $P_q$  in equation (i), we get the work done by impeller as

$$= \frac{1000 \times 9.81 \times 0.1963}{9.81} \times 23.2 \times 26.18$$

$$= 119227.9 \text{ Nm/s. Ans.}$$

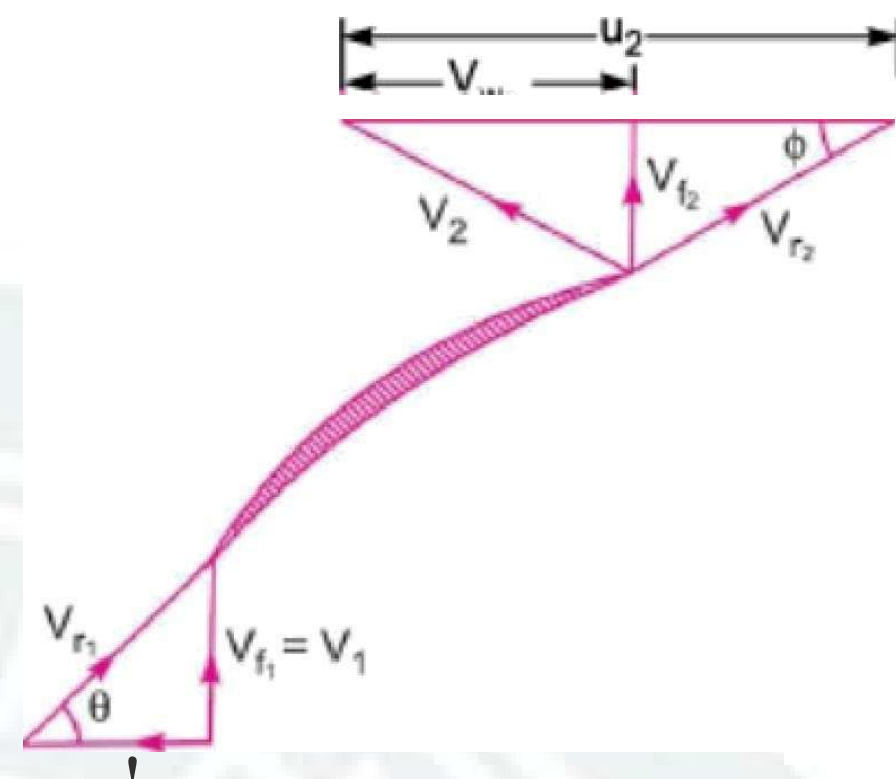


Fig. 19.6

## Chapter 3

Syllabus:-

### 3.0 RECIPROCATING PUMPS

3.1 Describe construction & working of single acting reciprocating pump.

3.2 Describe construction & working of double acting reciprocating pump.

3.3 Derive the formula for power required to drive the pump (Single acting & double acting)

3.5 Define slip.

3.5 State positive & negative slip & establish relation between slip & coefficient of discharge.

3.6 Solve numerical on above

### Reciprocating pump

#### Introduction

- The reciprocating pump is a positive displacement pump.
- Reciprocating pumps are in use where a certain quantity of fluid (mostly slurry) has to be transported from the lowest region to the highest region by the application of pressure.
- Here the mechanical energy is converted into hydraulic energy which is mainly in the form of pressure energy.

- If the mechanical energy is converted into hydraulic energy by sucking the fluid into a cylinder in which a piston is reciprocating, which exerts the thrust on the liquid and increases its hydraulic energy, the pump is known as reciprocating pump.
- It is best suited for relatively small capacities and high head

#### Classification of reciprocating pump

- According to the water being in contact with one side or both the side of piston
  - o Single acting pump
  - o Double acting pump
- According to the number of cylinder provided
  - o Single cylinder pump
  - o Double cylinder pump
  - o Triple cylinder pump

#### Application:

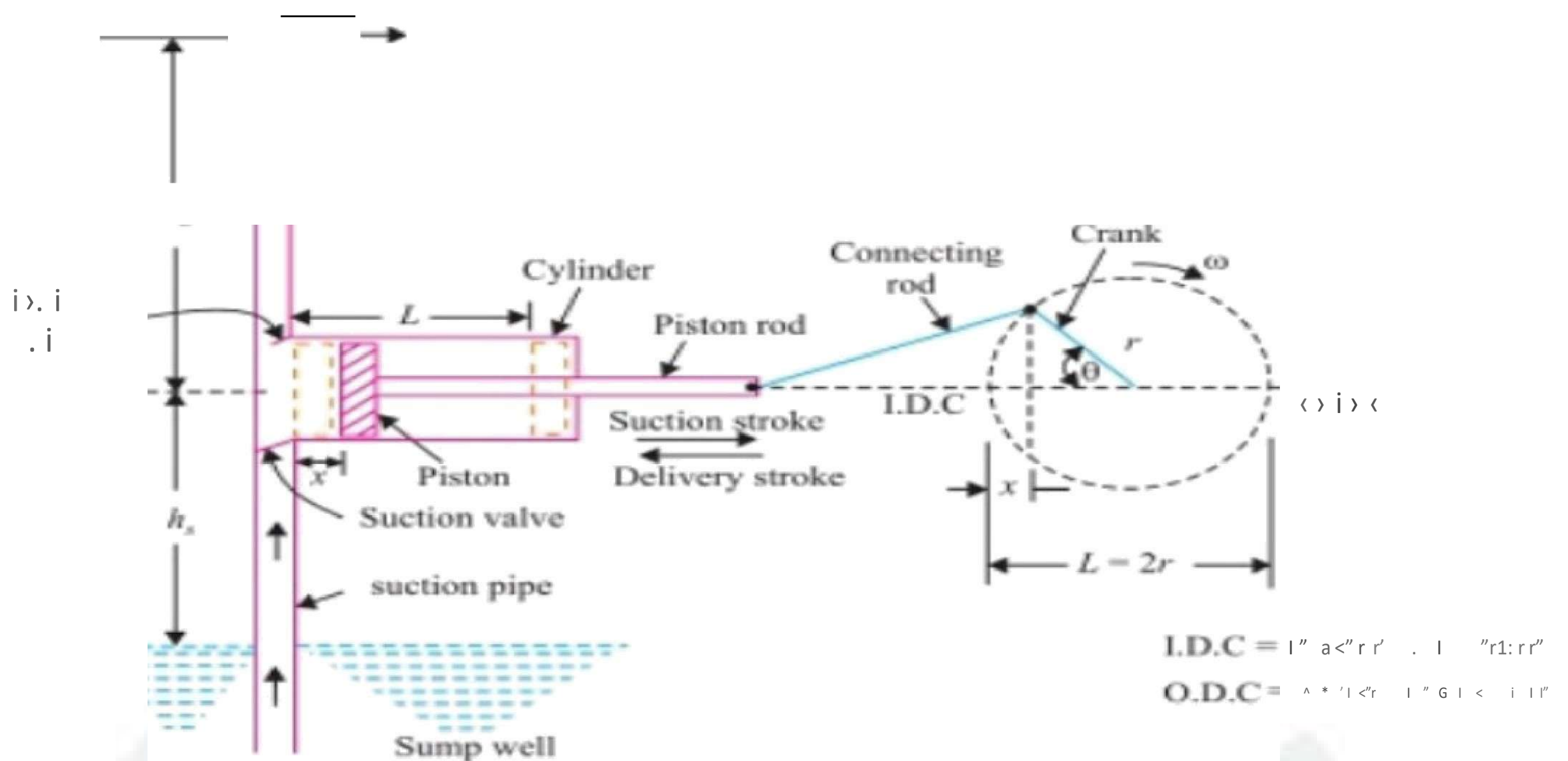
The applications of Reciprocating Pump are as follows.

- o Gas industries
- o Petrochemical industries
- o Oil refineries
- o Vehicle water servicing centers etc.

#### Construction of single acting reciprocating Pump

The main parts are

- Water Sump
- Strainer
- Cylinder
- Piston
- Suction Valve
- Delivery valve
- Suction Pipe
- Delivery Pipe
- Crank and connecting rod mechanism



#### Water Sump:

- It is the source of water. From the sump, water is to be transported to the delivery pipes by the usage of the piston.

#### Strainer:

- It acts as a mesh that can screen all the dirt, dust particles, etc. from the sump. If there is no strainer, then the dirt or dust also enters into the cylinder which can jam the region and affects the working of the pump.

#### Suction Pipe:

- The main function of the suction pipe is to collect the water from the sump and send it to the cylinder via a suction valve. The suction pipe connects the water sump and the cylinder.

#### Suction Valve:

- It is a non-return valve which means it can take the fluid from the suction pipe and send it to the cylinder but cannot reverse the water back to it. In the sense, the flow is unidirectional.
- This valve opens only during the suction of fluid and closes when there is a discharge of fluid to outside.

#### Cylinder:

- It is a hollow cylinder made of cast iron or steel alloy and it consists of the arrangement of piston and piston rod.

#### Piston and Piston rod:



- For suction, the piston moves back inside the cylinder and for discharging of fluid, the piston moves in the forward direction.
- The Piston rod helps the piston to move in a linear direction i.e. either the forward or the backward directions.

#### Crank and Connecting rod:

- For rotation, the crank is connected to the power source like engine, motor, etc. whereas the connecting rod acts as an intermediate between the crank and piston for the conversion of rotary motion into linear motion.

#### Delivery Pipe:

- The function of the delivery pipe is to deliver the water to the desired location from the cylinder.

#### Delivery valve:

- Similar to the suction valve, a delivery valve is also a Non-return valve. During suction, the delivery valve closes because the suction valve is in opening condition and during Discharge, the suction valve is closed and the delivery valve is opened to transfer the fluid.

### Working of single acting reciprocating pump

- Single acting means the water is acting on one side of the piston
- This pump has one suction pipe and one delivery pipe.
- It is usually placed above the liquid level in sump.
- When the crank rotates the piston moves forward and backward inside the cylinder.
- Initially the crank is at inner dead center i.e. at A and crank rotates in the clockwise direction.
- As the crank rotates the piston move towards right and a vacuum is created at left side of the piston.
- The vacuum causes suction valve to open and consequently the liquid is forced from the sump into the left side of the piston
- When the crank is at outer dead center i.e. at C the suction stroke is completed and the left side of the cylinder is full of liquid
- When the crank returns from ODC to IDC the piston moves inward to the left and high pressure is built up in the cylinder.
- The delivery valve opens and the liquid is forced into the delivery pipe.
- The liquid is carried to the discharge tank through the delivery pipe
- At the end of delivery stroke the crank comes to the IDC and the piston is at the extreme left position.

## Heads of Pump:-

There are three types of Head in a reciprocating Pump

### 1. Suction Head:

- It is the height through which water is entering through the Suction pipe to inlet end of Cylinder
- It is the length of Suction Pipe is calculated from the Center of cylinder to the level of liquid in sump
- It is denoted by symbol

### 2. Delivery Head:

- It is the length of Delivery Pipe is calculated from the Center of cylinder to the level of water in Overhead Tank
- It is denoted by symbol

### 3. Static Head:

- It is the total head through which the pump has to work
- It is the Sum of Suction Head and Delivery Head of Pump
- It is denoted by symbol

#### **Heads of Pump:**

where

$V_s$  = Velocity of fluid in the suction pipe.

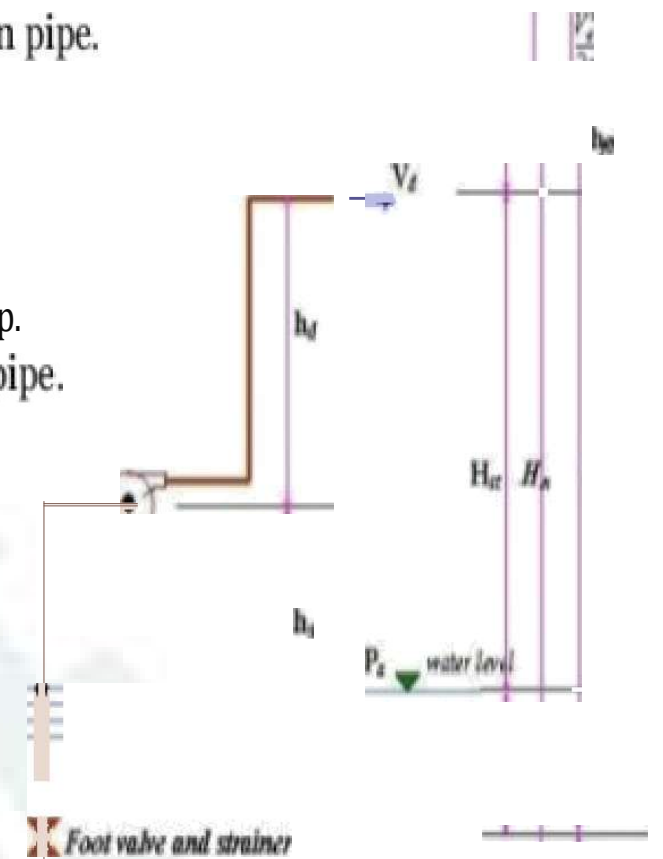
$V_d$  = Velocity of fluid in the delivery pipe.

$h_s$  = Suction head.

$h_d$  = Delivery head.

$h_f$  = head losses in the suction pipe.

$h_{fd}$  = head losses in the delivery pipe.



\*\*\*\*'\*\*\*\*'\*\*\*\*'

$$H_{st} = h_s + h_d$$

## Co-efficient of discharge

In a reciprocating pump the actual discharge ( $Q_a$ ) is always slightly different from theoretical discharge ( $Q_t$ ) due to following reason

- Leakage through the valves and piston packing
- Imperfect operation of the valve
- Partial filling of the liquid

The ratio between actual discharge and theoretical discharge is known as the coefficient of discharge ( $C_d$ ) of the pump.

## Slip

The difference between the theoretical discharge and actual discharge is called slip of the pump.

## Slip

$$\% \text{ Slip} = \frac{Q_t - Q_a}{Q_t} \times 100 = \left(1 - \frac{Q_a}{Q_t}\right) \times 100$$

### Positive slip

In most of the reciprocating pumps is less than , in such a case the value of is less than unity and the slip of the pump is positive.

### Negative slip

If actual discharge is more than the theoretical discharge ; in such a case is more than unity and the slip will be negative.

Negative slip occurs when delivery pipe is short, suction pipe is long and pump is running at high speed.

### Discharge, Work done and Power Required to Drive Single -acting Reciprocating Pump

Let D= diameter of the cylinder

A= cross- sectional area of the piston / cylinder =

r= radius of the crank

N= Speed of the crank in r.p.m

L= length of the stroke = 2r

= Height of the center of the cylinder above the liquid surface

= Height to which the liquid is raised above the center of the liquid.

Vol of liquid sucked in during the suction stroke = AXL

No. of revolution per second =

Discharge of the pump per second = vol of liquid sucked in during suction stroke x No. of revolution per second

Q= AXLx

Weight of water delivered per second, W= wQ= (w= pg)

Work done per second = weight of water lifted /sec x total height through which liquid is lifted

=  $\wedge$  (\*)

Where, (+ is total height through which water is lifted.

We know W=



Work done = (+

Power required to drive the pump= P =

$P = \frac{W}{t}$

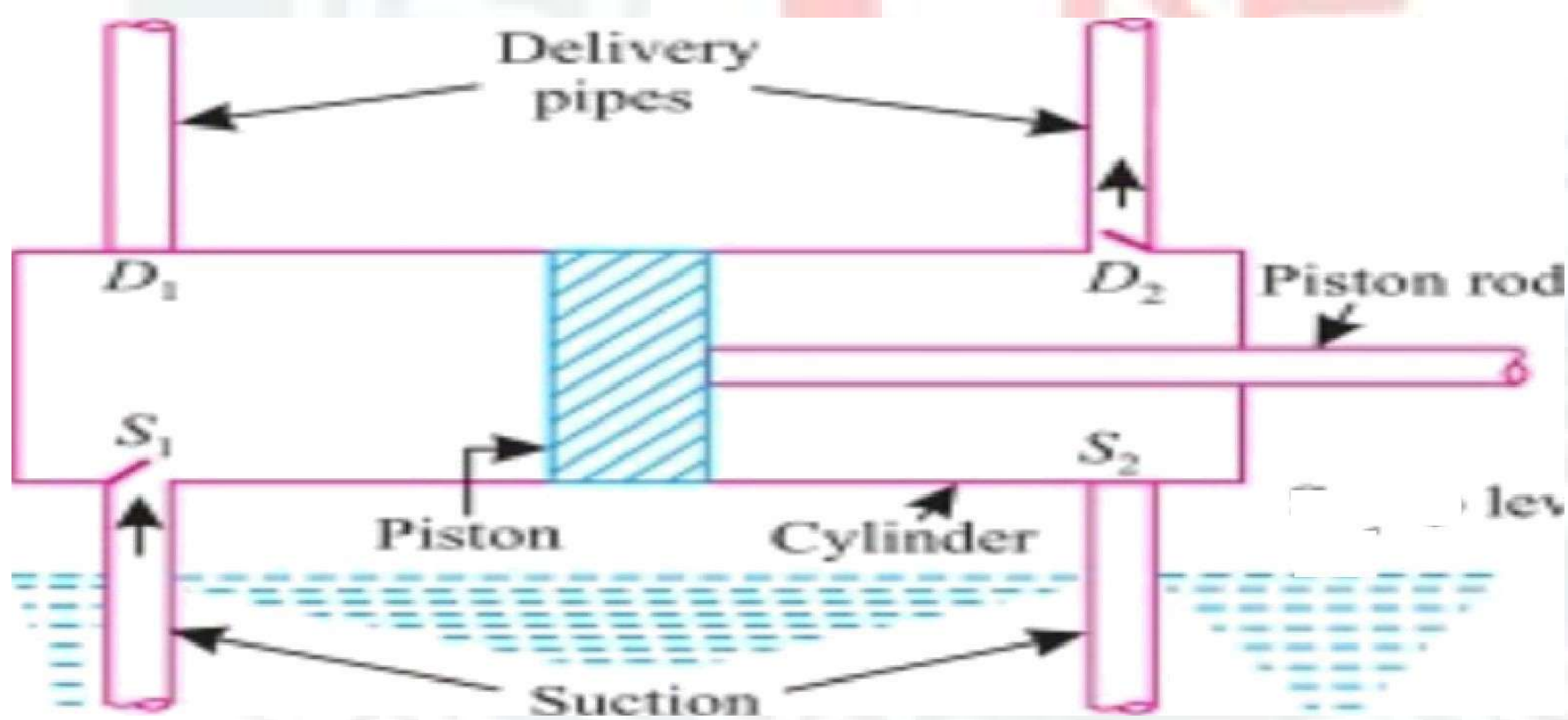
Where  $w$  = weight density of liquid in N/m<sup>3</sup>

### Construction of Double acting Reciprocating Pump

It is the type of reciprocating Pump in which the delivery and Suction of water is taking place twice in a complete revolution of Crank with the help of Mechanical energy from Prime Mover.

The main parts are

- Cylinder
- Piston
- Suction Valve
- Delivery valve
- Suction Pipe
- Delivery Pipe
- Crank and connecting rod mechanism



### Working

- Here we require two suction pipe and two delivery pipe
- Here suction and delivery stroke occurs simultaneously
- When the crank rotates from IDC in the clockwise direction, a vacuum is created on the left side of piston and the liquid is sucked in from the sump through S<sub>1</sub>.
- At the same time, the liquid on the right side of the piston is pressed and a high pressure causes the delivery valve D<sub>2</sub> to open and the liquid is passed on to the discharge tank.



- This operation continues till the crank reaches ODC.
- With further rotation of the crank, the liquid is sucked in from the sump through the suction valve S2 and is delivered to the discharge tank through the delivery valve D1.
- When the crank reaches IDC, the piston is in the extreme left position.
- Due to continuous delivery stroke, a double acting reciprocating pump gives more uniform discharge as compared to single acting pump.
- Advantages
- 1. High pressure is obtained at the outlet.
- 2. Priming process is not needed in this pump.
- 3. It provides high suction lift.
- 4. It is also used for air.

#### Disadvantages

- It requires high maintenance because of more wear and tear of the parts.
- Low flow rate i.e. it discharges low amount of water.
- They are heavy and bulky in size.
- High initial cost

#### **A** ication

- It is used at a place where low discharge rate is required with high pressure. It is mostly used to deliver water at large heights such as in deep well.
- It is used for inflation of tyres of bicycles

#### Discharge, Work done and Power Required to Drive Single-acting Reciprocating Pump

In Case of Double acting reciprocating pump there is two delivery stroke in one revolution of the driving shaft

Let

#### Difference between Centrifugal Pump & Reciprocating Pump

##### Centrifugal Pump

- Flow is Smooth and even
- Weight of Pump is less for a given delivery rate
- It is compact and occupies less floor space for a given delivery rate
- Initial Cost is High

- Installation is easy
- No Air vessel is required
- It can handle viscous liquid as like paper Pulp, muddy water etc.
- It requires priming
- It is suitable for large discharge and small head
- Maintenance cost is less. Periodical checkup is sufficient

#### Reciprocating Pump

- Flow is Intermittent
- Weight of Pump is less for a given delivery rate
- Floor space required is about 6 to 8 times the floor space occupied by the centrifugal pump
- Initial cost is about 4 times of Centrifugal Pump
- Installation is difficult
- Air Vessel is required
- It cannot handle viscous liquid because valves and glands cause trouble when required to handle viscous liquid.
- It does not require priming
- It is suitable for low discharge at high head
- Maintenance cost is high, because valves require constant attention

#### Numerical

**Problem 20.1** A single-acting reciprocating pump, at 50 r.p.m., delivers 0.01 m<sup>3</sup>/s of water. The diameter of the piston is 200 mm and stroke length is 400 mm. Determine :  
 (i) The theoretical discharge of the pump, (ii) Co-efficient of discharge, and (iii) Slip and the slip of the pump.

**Solution.** Given :

Speed of the pump,  $N = 50 \text{ r.p.m.}$

Actual discharge,  $Q_a = 0.01 \text{ m}^3/\text{s}$

Dia. of piston,  $D = 200 \text{ mm} = 0.20 \text{ m}$

$N = 50 \text{ r.p.m.}$

$Q_a = 0.01 \text{ m}^3/\text{s}$

$D = 200 \text{ mm} = 0.20 \text{ m}$

$$A = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.2)^2 = 0.031416 \text{ m}^2$$

Stroke,  $L = 400 \text{ mm} = 0.40 \text{ m}$

(c) Theoretical discharge for single-acting reciprocating pump is given by equation (20.1) as

$$Q_{th} = \frac{A \times L \times N}{60} = \frac{0.031416 \times 0.40 \times 50}{60} = 0.01047 \text{ m}^3/\text{s. Ans.}$$

(i) Co-efficient of discharge is given by

$$C_d = \frac{Q_a}{Q_{th}} = \frac{0.01}{0.01047} = 0.955 \text{ Ans.}$$

(ii) Slip of the pump is given by

$$\text{Slip} = Q_{th} - Q_a = 0.01047 - 0.01 = 0.00047 \text{ m}^3/\text{s}$$

Slip of the pump is

$$\text{Slip} = \frac{Q_{th} - Q_a}{Q_{th}} \times 100 = \frac{0.00047}{0.01047} \times 100 = 4.489\% \text{ Ans.}$$

**Problem 20.2** A double-acting reciprocating pump, running at 40 r.p.m., is discharging 1.0 m<sup>3</sup> of water per minute. The pump has a stroke of 400 mm. The diameter of the piston is 200 mm. The delivery head is 20 m and suction head is 5 m respectively. Find the slip of the pump and power required to drive the pump.

**Solution.** Given:

Speed of pump,  $N = 40 \text{ r.p.m.}$

$N = 40 \text{ r.p.m.}$

Actual discharge,  $Q_a = 1.0 \text{ m}^3/\text{min} = \frac{10}{60} \text{ m}^3/\text{s} = 0.1667 \text{ m}^3/\text{s}$

$Q_a = 1.0 \text{ m}^3/\text{min} = \frac{10}{60} \text{ m}^3/\text{s} = 0.1667 \text{ m}^3/\text{s}$

Stroke,  $L = 400 \text{ mm} = 0.40 \text{ m}$

$L = 400 \text{ mm} = 0.40 \text{ m}$

Diameter of piston,  $D = 200 \text{ mm} = 0.20 \text{ m}$

$D = 200 \text{ mm} = 0.20 \text{ m}$

Area,  $A = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.2)^2 = 0.031416 \text{ m}^2$

$$A = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.2)^2 = 0.031416 \text{ m}^2$$

Suction head,  $h_s = 5 \text{ m}$

$h_s = 5 \text{ m}$

Delivery head,  $h_d = 20 \text{ m}$

$h_d = 20 \text{ m}$

Theoretical discharge for double-acting pump is given by equation (20.5) as,

$$Q_{th} = \frac{2 A L N}{60} = \frac{2 \times 0.031416 \times 0.40 \times 40}{60} = 0.1675 \text{ m}^3/\text{s}$$

Using equation (20.8), Slip =  $Q_{th} - Q_a = 0.1675 - 0.1667 = 0.0008 \text{ m}^3/\text{s}$  Ans.

Power required to drive the double-acting pump is given by equation (20.7) as,

$$P = \frac{2 \times \rho \times g \times A \times L \times N \times (h_s + h_d)}{60} = \frac{2 \times 1000 \times 9.81 \times 0.031416 \times 0.40 \times 40 \times (5 + 20)}{60} = 10000 \text{ W}$$



rn

filled with air.

deals with the study of behavior and applications of compressed air in manufacturing automation in particular.

ns use air as the medium which is abundantly available and can be exhausted after completion of the assigned task.

branch of mechanics that deals with the mechanical properties of gases. study of pressurized gas that produces mechanical motion, and the applications

pneumatics are found in factories that deal with compressed air and

of air

f air

on of compressed air in pressure vessels, containers and in long pipes.

and reproducibility

lity

eristics of medium.

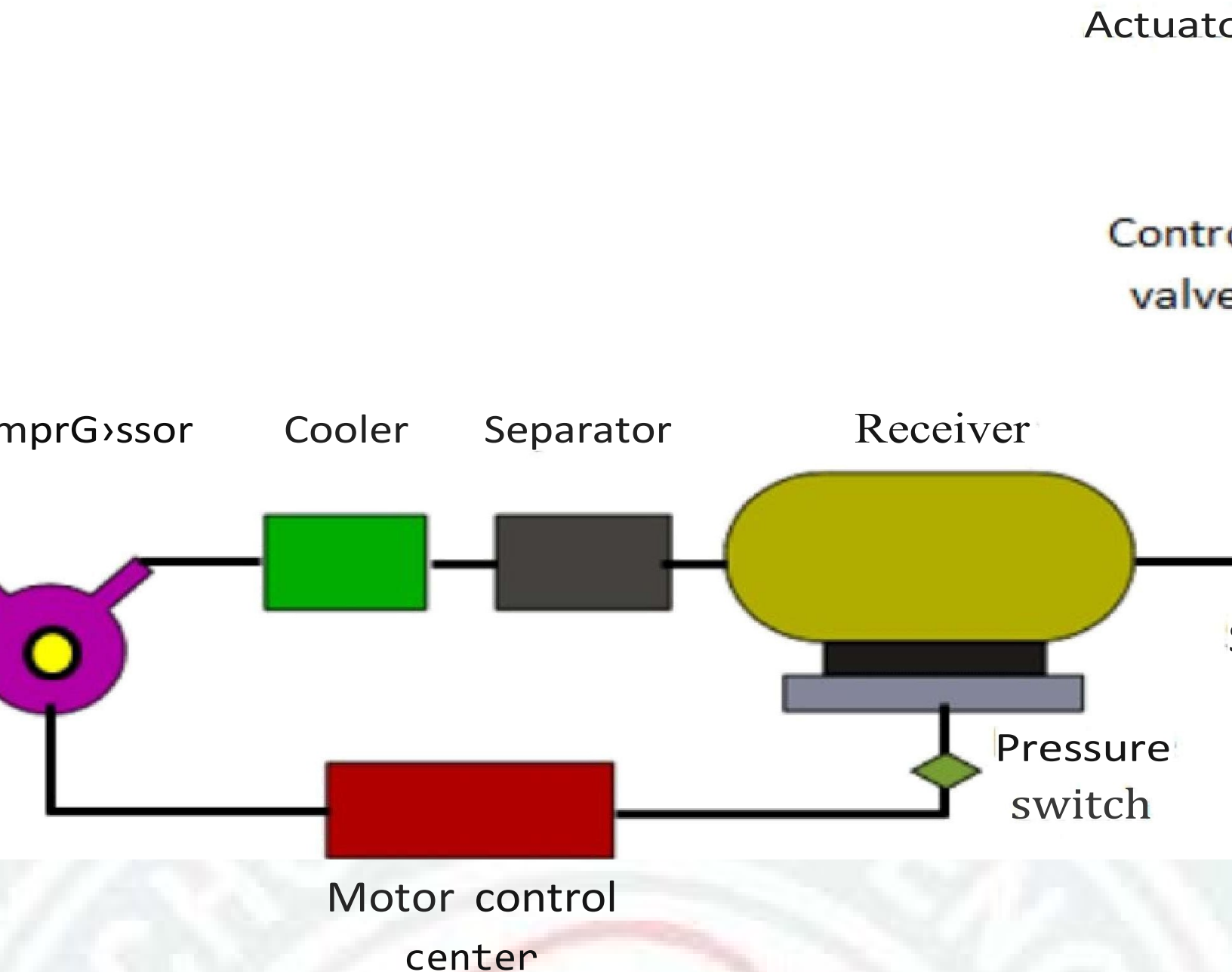
on & easy handling

eaper than other systems.

controllers



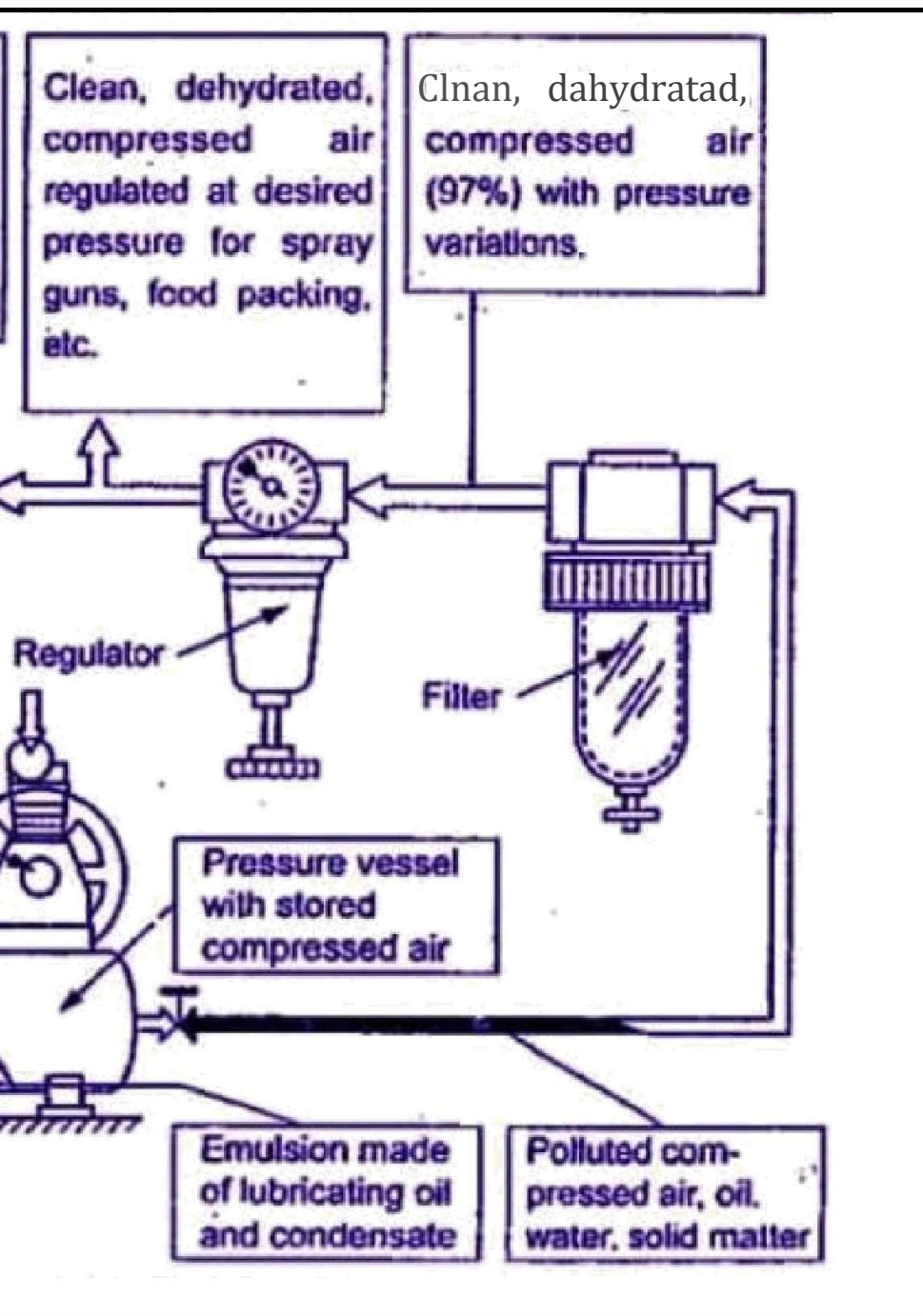
## pneumatic system



are used to filter out the contaminants from the air.

Compressed air is generated by using air compressors. Air compressors are used to generate compressed air. Based on the requirement of compressed air, suitable capacity compressors are selected. During the compression operation, air temperature increases. Therefore coolers are used to cool the compressed air.

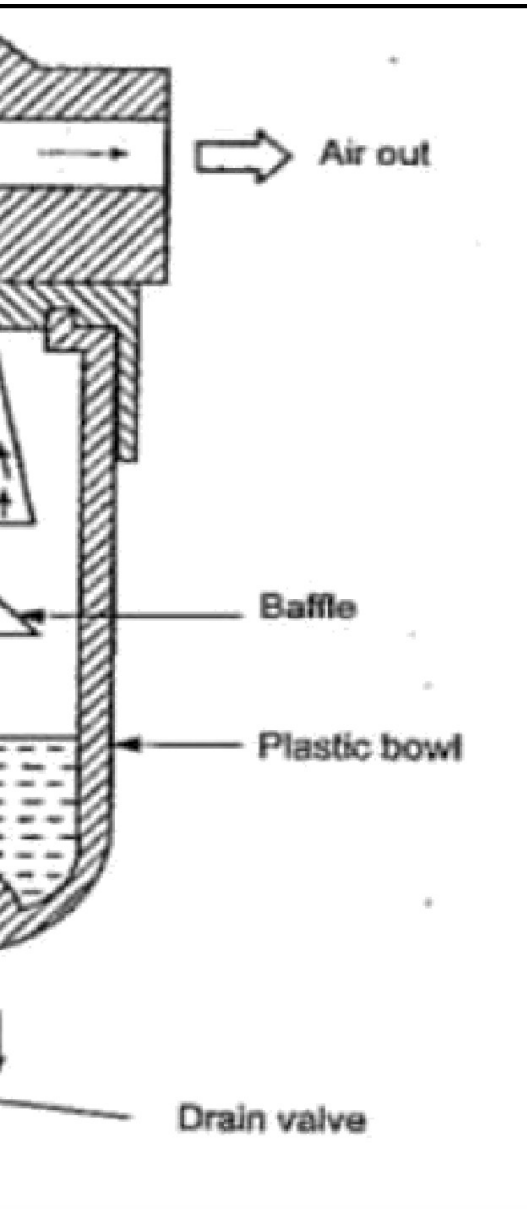
Moisture or vapor in the air is separated from the air by using a dryer.



ce of solid contaminants to the system.

d remove the water vapor that is present in the air.

on particles that may pose a problem in the system components.



- At the bottom of the filter bowl, there is a drain valve which could be manually opened to drain off moisture and solid particle.

One of the main functions of a pressure regulator is to regulate the incoming pressure to the system so that the desired pressure is maintained in a steady condition.

The air leaving the compressor should be properly prepared before it goes to the system. The system should be at its normal operating pressure for the circuit.

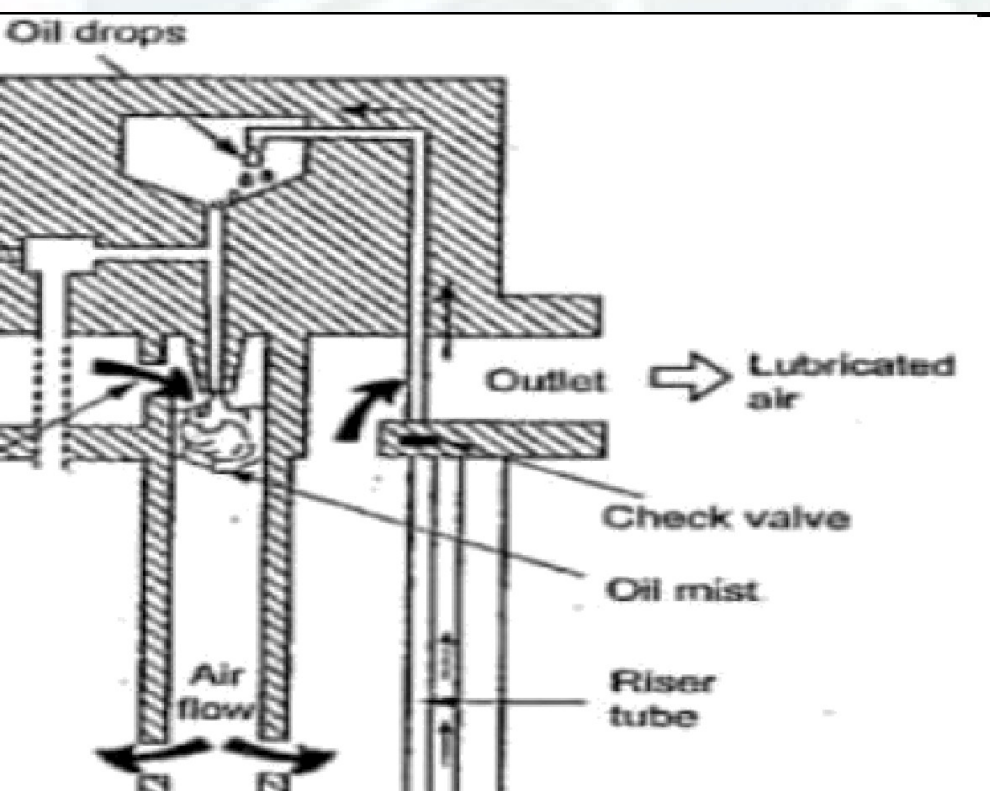
g screw is turned to compress the adjusting and dampening springs, the flow from the inlet port to the outlet port. The pressure of the outlet air is maintained.

d by the compression of the adjustable spring. Higher the spring compression and hence more the pressure and vice versa.

is provided to let out the undesirable excessive outlet pressure. if any, a spring is provided to act as a dampening device needed to stabilize the

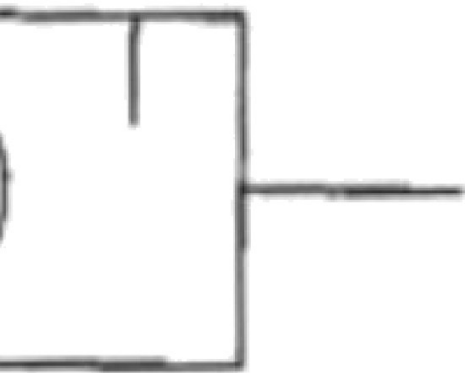
lubricator is to add a controlled amount of oil with air to ensure proper lubrication of pneumatic components.

It adds the lubrication oil in the form of a fine mist to reduce the friction and wear of pneumatic components such as valves, packings used in air cylinders, etc.

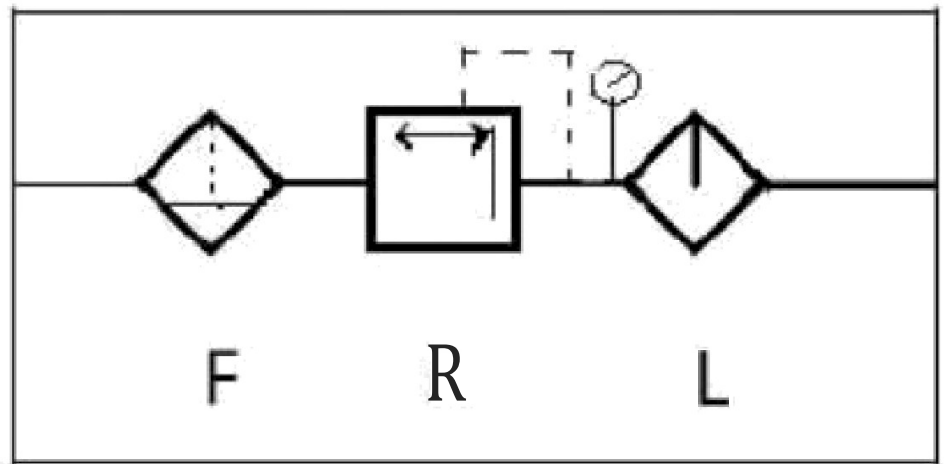




Symbol



## Combined Symbol



to avoid pressure drop or rise so that leakage and parts damages may be avoided. The time may increase.

by.  
and servicing.

placed in the place of heavy vibration then it may damage the Unit.  
without flexibility. such as steel tube piping, are prone to be affected by  
from the piping side. Use flexible tubing in between to avoid such effects.

to control the quantity of pressure and flow rate to generate the desired level of  
a device that conveys energy typically in the form of compressed air into

Pressure is thus relieved to the desired figure, the valve closed again by spring force. The valve is connected to pump and the other to the tank.

The valve has a spring chamber (control chamber) with an adjustable bias spring for closing the valve.

A line connecting the tank is provided in the control chamber to drain the oil to the tank, thereby preventing the failure of valve.

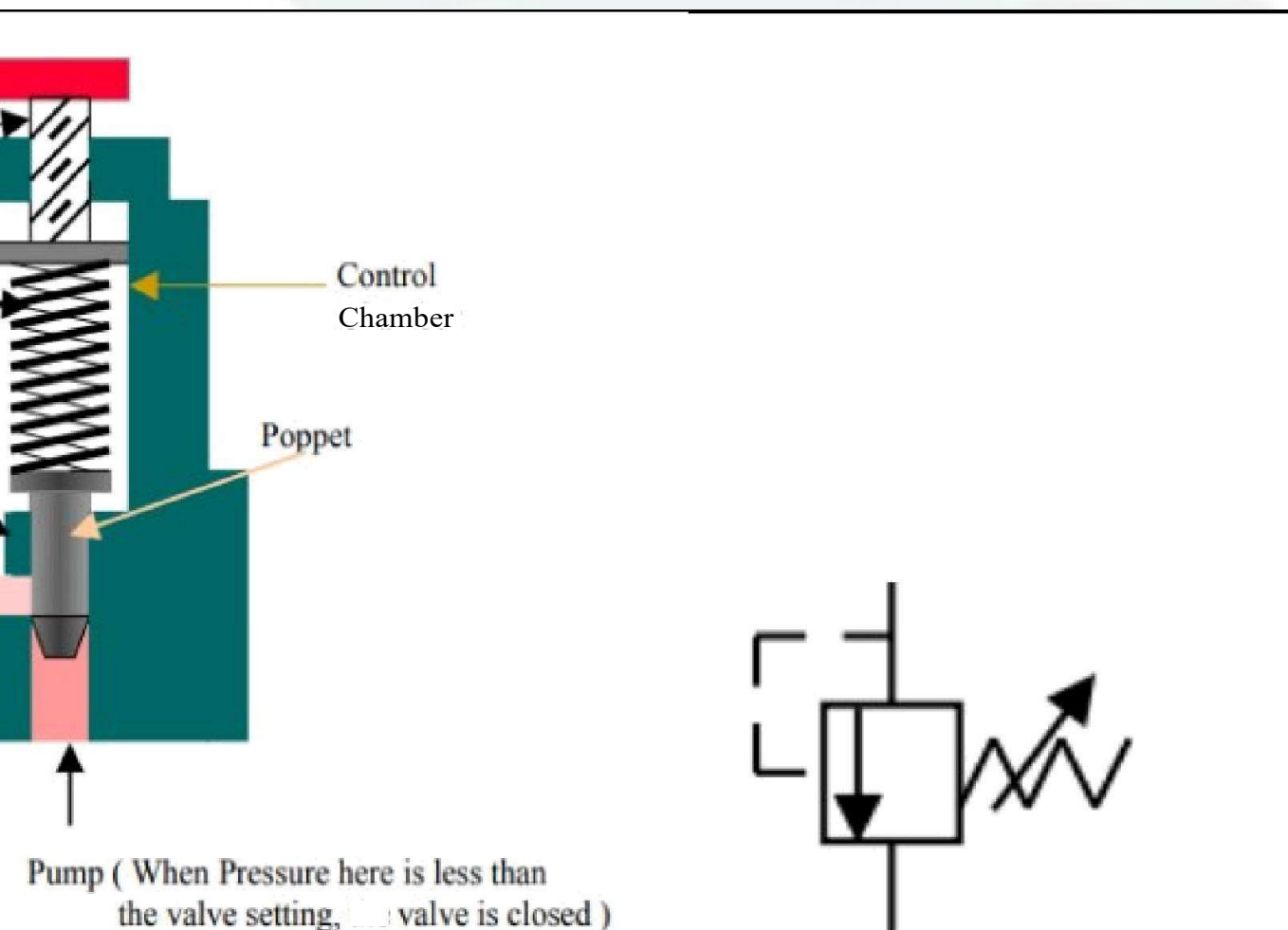
The spring opposes the poppet, which is held on its seat by an adjustable spring.

The pressure is set to limit the maximum pressure that can be attained within the system.

The valve is held in position by spring force plus the dead weight of spool.

When the pressure exceeds this force, the poppet is forced off its seat and excess fluid in the system is drained to the tank.

When the pressure drops to or below established set value, the valve automatically closes.



## Spool Valve —

used in pneumatic system to direct or stop the flow of compressed air. They have two or more ports and fulfill various circuit functions.

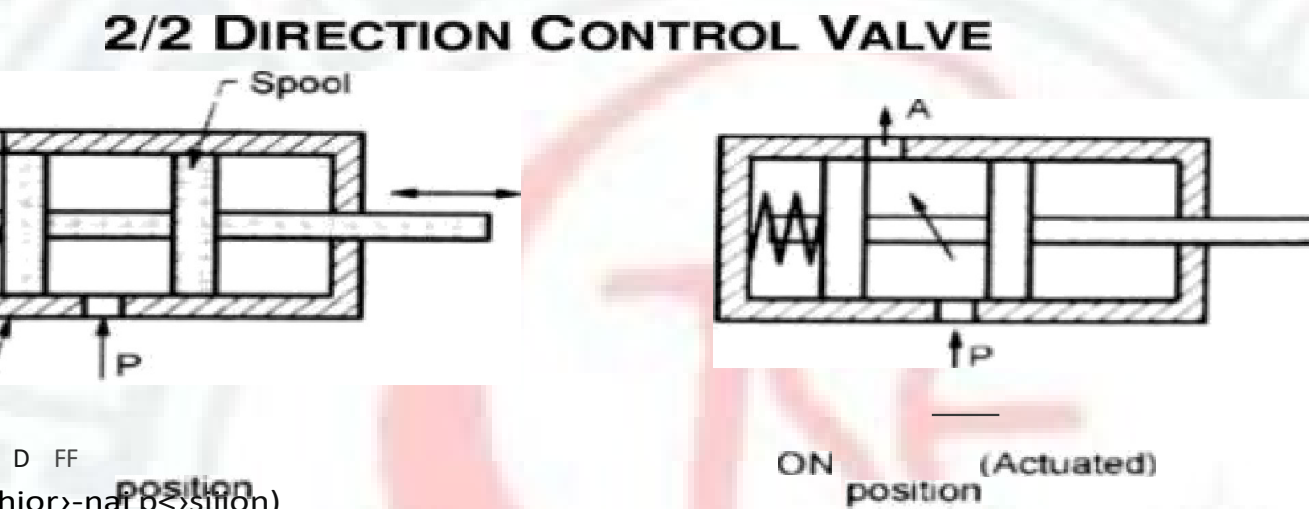
They allow flow to different paths from one or more sources.

They consist of a spool inside a cylinder which is mechanically or electrically actuated. The spool restricts or permits flow, thus it controls the fluid flow.

They are designated with two numbers. The first number shows how many ports they have and the second number shows the amount of states. For example, a 2/2 way valve has two ports (in/out) and two states. A 5/2 way valve has five ports and two states.

The simplest and most simple valve is the 2/2-way valve. It has two ports and two states. It is therefore also called a shut-off valve.

In pneumatic applications where the supply of air must periodically be closed,



s of three ports like 'A', 'R', 'P' as shown in above fig. Port A represents passage of Compressed Air delivered to the Actuator for Reciprocating Action of piston.

It provides the path for return of Compressed air from port A to deliver back to the container. During the delivery of high pressure air from Air Container to the DCV for actuator passage, Port P is open (Neutral Position) the return of compressed air from actuator through Port P is delivered to the air container. Port 'P' is closed. For actuation the electric current is supplied to the spool of spool

Position spools move towards the right position and thereby the passage of compressed air for forward motion of piston in actuator is taking place by the compressed air entering through Port 'A' to the hose connected with the actuator.

Energy in spring attached with the spool Spindle causing the spools to move towards the left position and while Port P is Closed, during this time return stroke of the piston takes place. Compressed air from actuator returns through the Port A and Port R, then enters the container.

e:

It has five ports and two states.

It is used for instance to control double acting cylinders.

Each cylinder requires two outlet ports of the valve.

Ports 'A' & 'B' provided at top of DCV which are allowing the Compressed Air for supply.

During the exhaust of return compressed air from Actuator to Air Container through Port R, the supply of high Pressure Air to be used for reciprocating action of piston is blocked. When the spool is actuated towards outer direction, port P gets connected to B and Port R gets connected to A.



e

a valve that controls the flow of air. Examples include non-return valves.

Valve allows air to flow in one direction only. When air flows in the opposite

valve is formed by a non-return valve and a variable throttle

valves are available in two modes

(control passage is not adjustable)

Control / Throttle valve- Here an adjustable control needle is positioned to regulate the flow as per need of flow quantity.

For valve it is better to lock the needle position by a lock nut in order to maintain that position.

Needle position may change subjecting the valve to allow either less or more flow

type of "electromagnet", the purpose of which is to generate a controlled magnetic field wound into a tightly packed helix.

It is arranged to produce a uniform magnetic field in a volume of space where the flow occurs.

The term may also refer to a variety of transducer devices that convert electrical energy into mechanical work.

It converts electrical energy into mechanical work.

It is often used to refer to a solenoid valve, an integrated device consisting of an electric solenoid which actuates either a pneumatic or hydraulic valve, or a solenoid pump.

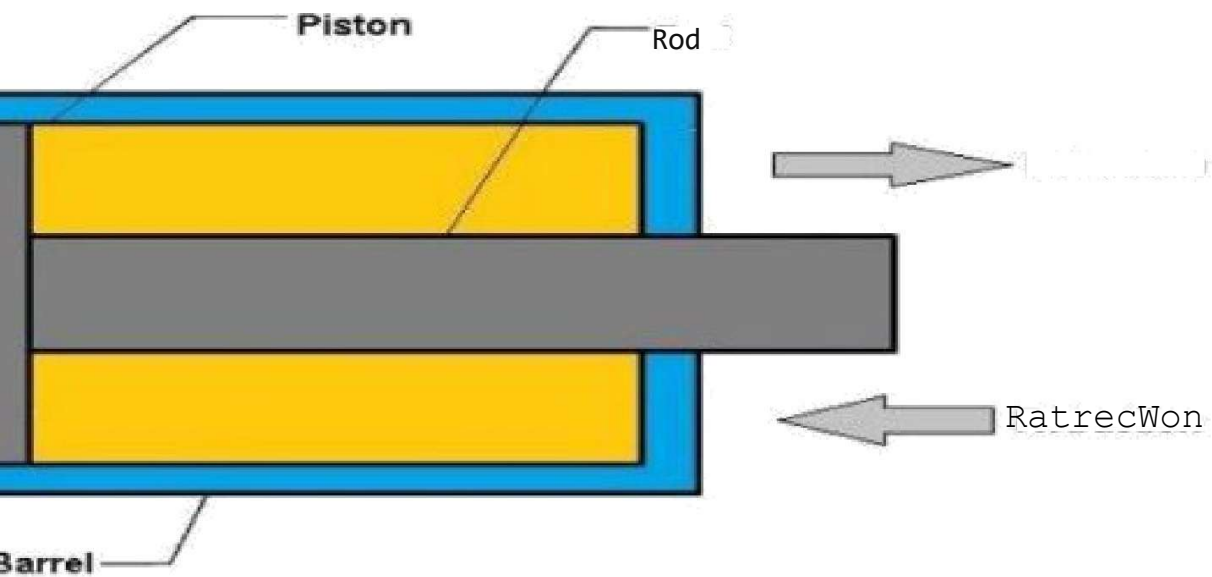
air while being exhausted from the pneumatic system components like  
 creates a lot of noise.

Pneumatic components are to be provided with noise reducing & mufflers  
 to bring the noise level to a tolerable limit and go a long way in reducing health

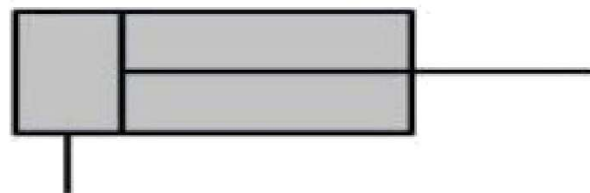
### ISO symbols for fluid circuits

Control valve	
Directional control valve	
	2/2 Directional control valve—normally closed
	2/2 Directional control valve—normally open
	3/2 D.C. valve normally closed
	3/2 D.C. valve normally open
	3/3 D.C. valve—zero position all ports closed
	4/2 D.C. valve

Pressure control valve	
	Pressure relief valve
	Sequence valve
	Pressure regulator
	Pressure regulator with self relieving
Flow valve	
	Flow control general symbol
	Flow control (insignificant influence of viscosity)
	Adjustable flow control
	Flow control valve



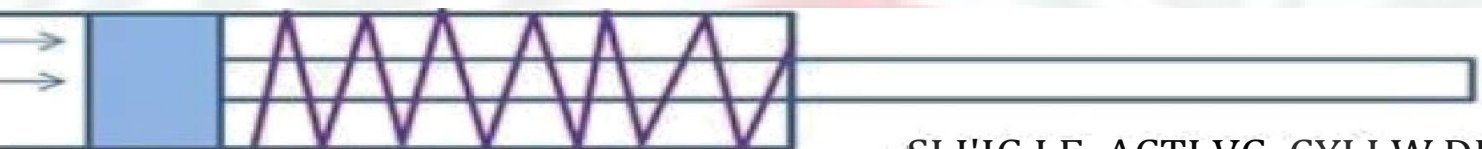
representation



Gywtzollc representatlz>n

acting cylinder

of SII'sIGLE ac€inp c'yli nclelv



SI I'IG LE ACTI VG CYLI W DE R  
SPR I f•IG RETLJ R t'4 E D

---

A port of the valve shifting the valving element and thus SA cylinder

ing force from the push button is released, the valve spring resets the c  
the cylinder.

d to  $p_o < A$  due to resetting of valving element.

open to port R.

the cylinder gets exhausted through the R port of the valve.

force of the spring pushes the piston rod of the cylinder and the cylinder

ing cylinder in which fluid under pressure can be applied to either side  
ment.

acting cylinder

el is made of steel tubing which is seamless.

is perfectly boned.

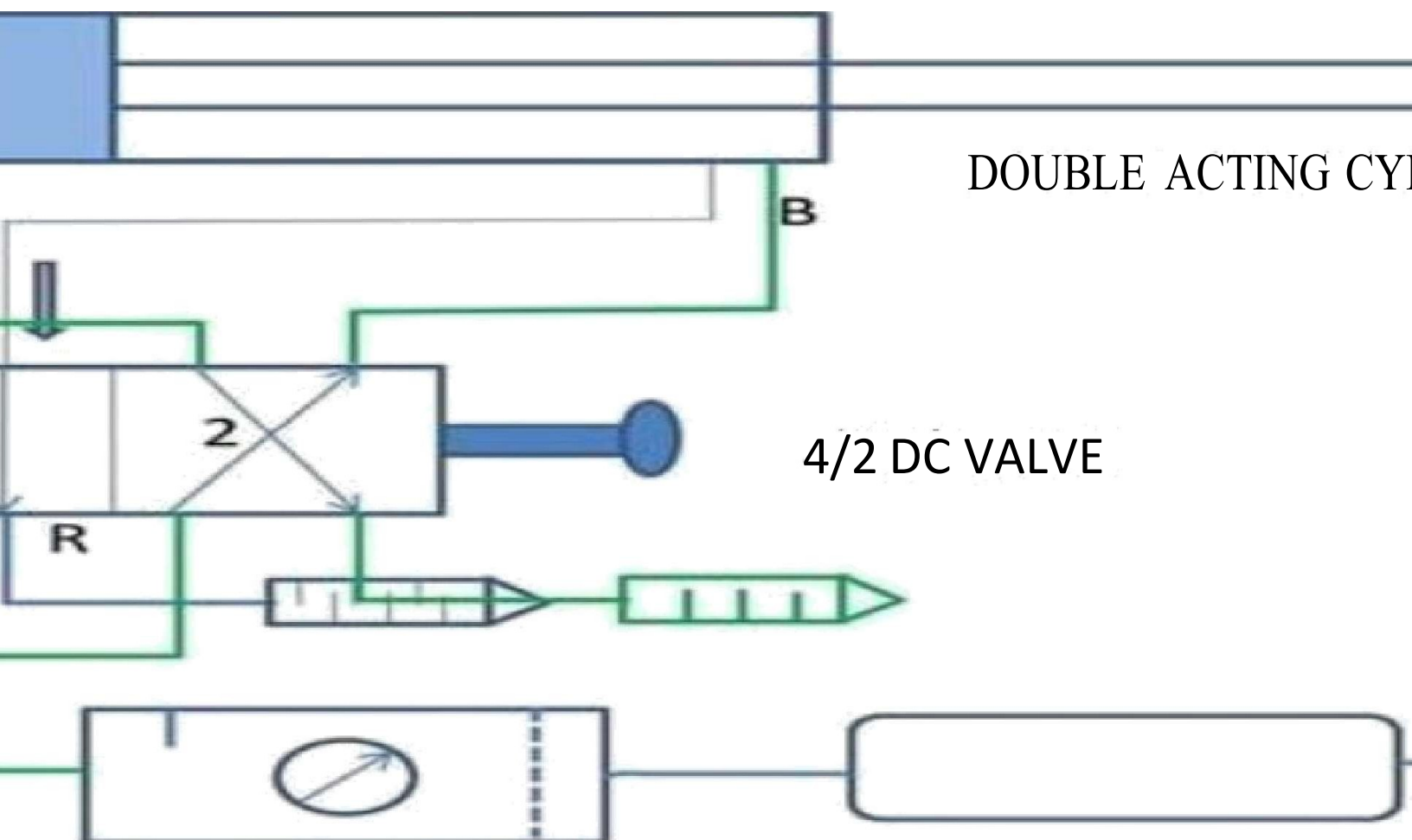
manufactured by ductile iron.

l to prevent leakage between the piston & the barrel.

ends caps.

to the barrel by tie rods.





When the DCV is in its normal position, the compressed air flow from air compressor to air receiver through Port P to A the piston extends in a forward motion mean while the air in the piston side of the cylinder release from A to R Port.

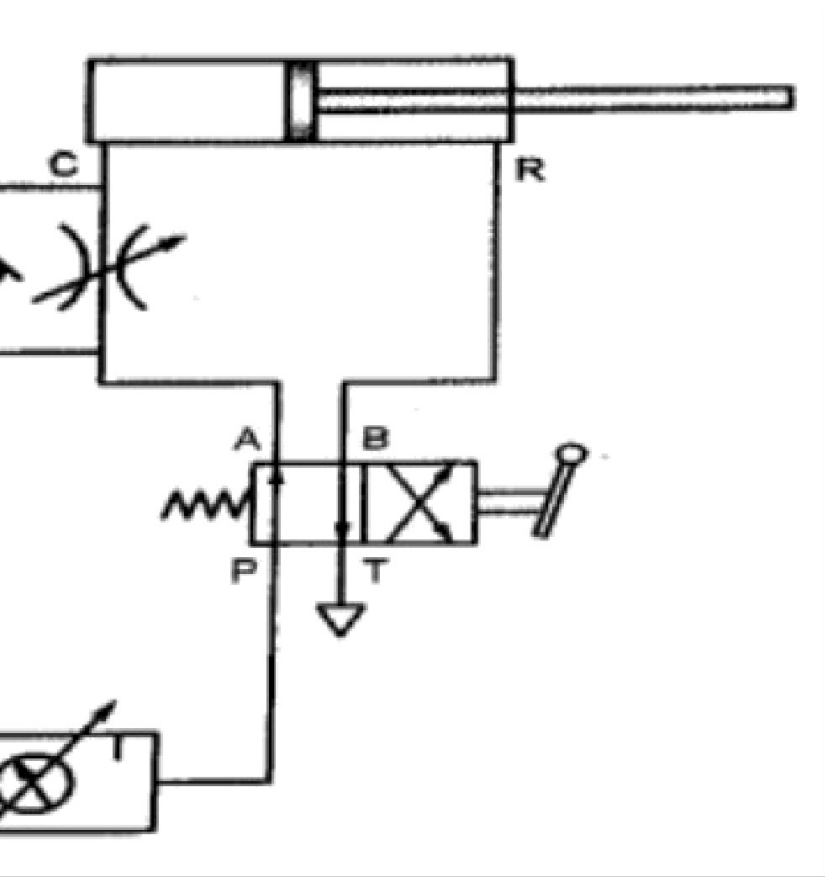
When the DCV is actuated, the compressed air flow from Port P to B and the piston retracts. While the air in the piston side of the cylinder release from A to R port.

Requirement for Double acting flow control actuator:-

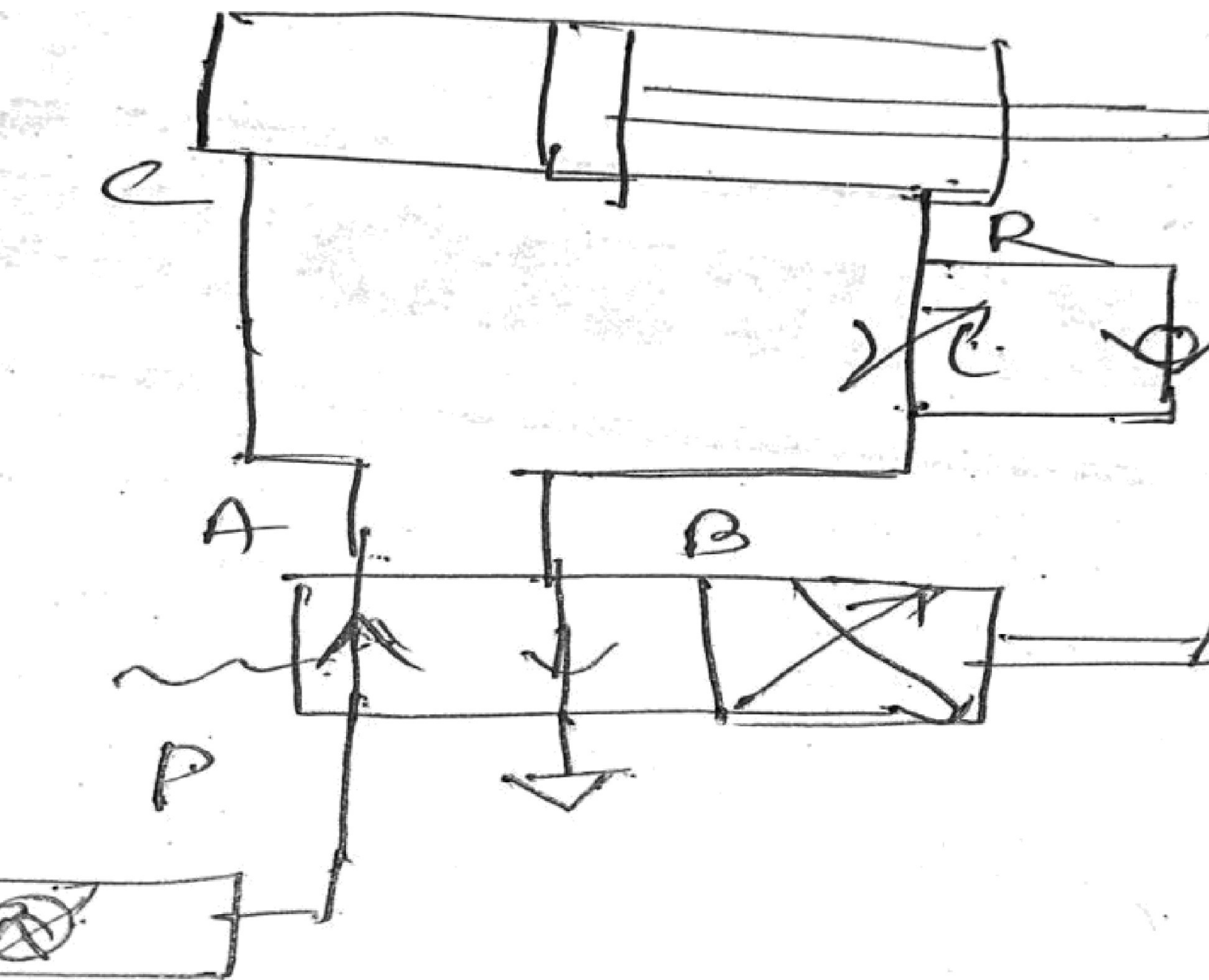
Controlling the actuator speed in a pneumatic system, the flow control valve controls the rate of flow of compressed air. The rate of flow of compressed air will vary the speed of the actuator.

In a pneumatic circuit the rate of flow of compressor air is controlled at inlet of the actuator. The air going in to the actuator is metered.

In a pneumatic circuit flow control valve is fitted between DCV and actuator. For control of actuator during extension stroke, FCV with check valve is fitted in the line for retraction or.



After in circuit fluid enters in to the actuator at a controlled rate. The rate of flow of compressed air in to the cylinder is controlled by FCV. The air is supplied at inlet of the cylinder cap end port 'C' is inlet for extension and retraction.



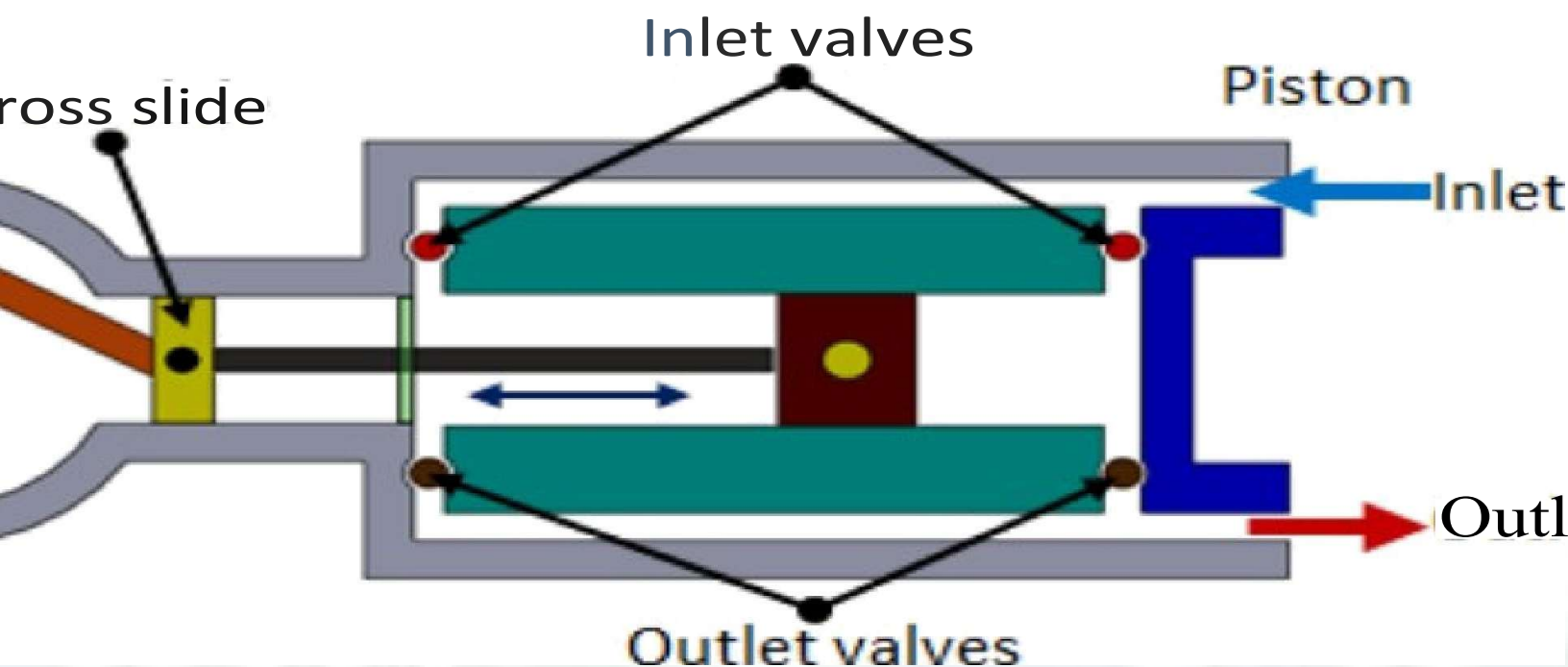
r:

l device which converts mechanical energy into Uuid energy. The con  
pressure by reducing its volume which also increases the temperatur

## Compressor:

Air can be reduced by using double acting compressor as shown in Fig. It has two inlet valves and a crosshead. As the piston moves, the air is compressed on one side of the piston, the air is sucked in.

During the opposite action of the piston, the air is compressed and delivered twice. A pressure higher than 30bar can be produced.



As the air increases, its temperature rises.

To reduce the air temperature to avoid damage of compressor and other mechanical parts, a double-acting compressor with intercooler in-between is shown in Figure.

The intercooler reduces the temperature of compressed air during the compression stages.

The intercooler reduces the volume of air which used to increase due to heat. The compressed air then enters the intercooler where it is cooled.



r

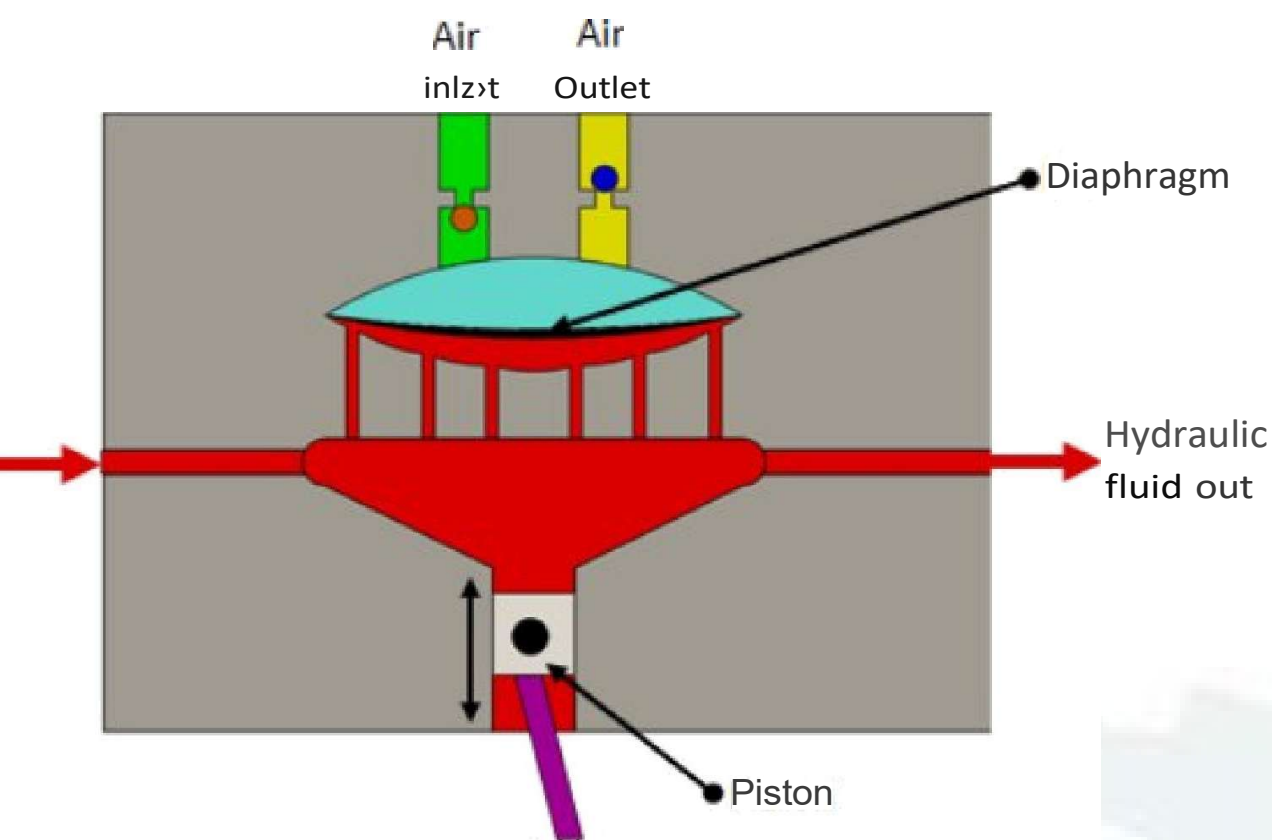


Fig. 6.2.1 Diaphragm compressor

small capacity compressors. In piston compressors the lubricating oil from the cylinder walls may contaminate the compressed air.

Contamination is undesirable in food, pharmaceutical and chemical industries. For such applications diaphragm type compressor can be used.

The following diagram shows the construction of Diaphragm compressor.

The piston reciprocates by a motor driven crankshaft.

When the piston moves down it pulls the hydraulic fluid down causing the diaphragm to move down and the air is sucked in.

When the piston moves up the fluid pushes the diaphragm up causing the ejection of the compressed air.

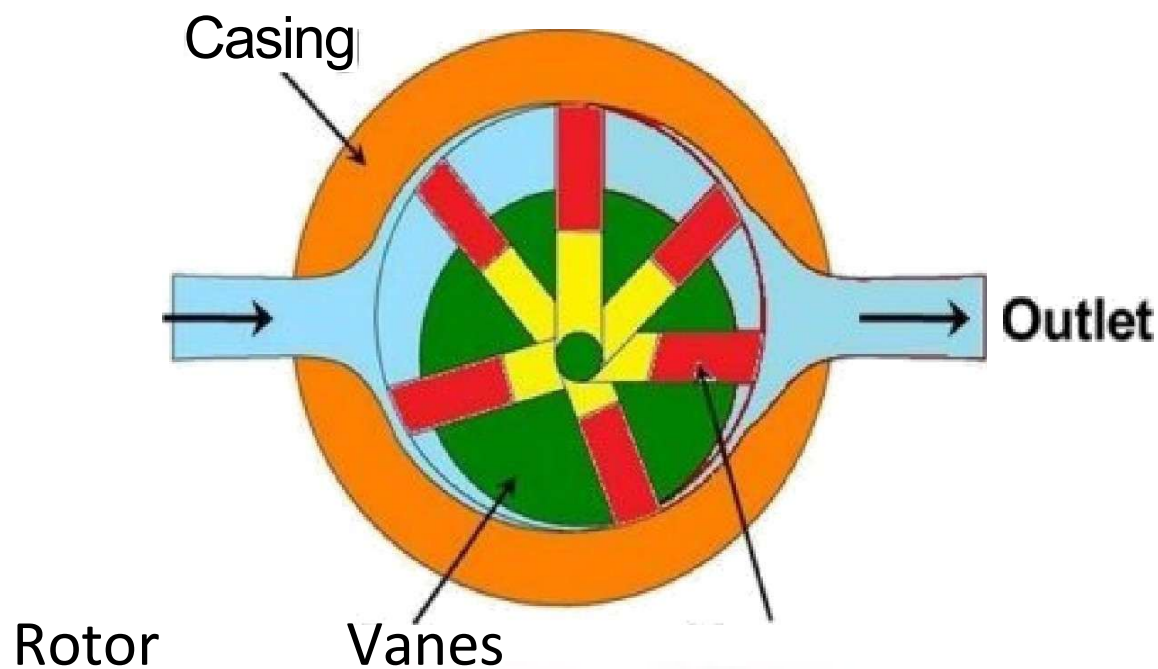


Fig. 6.2.3 Rotary vane compressor

Operation of vane compressor is similar to the hydraulic vane pump. A vane compressor consists of spring loaded vanes seating in the casing. Compression occurs due to movement of the vanes along a cam ring. The volume of the gas trapped in the cam ring. As the rotor rotates, the vanes follow the inner surface of the casing. The volume of the gas decreases near the outlet due to the eccentricity of the rotor. These compressors are free from pulsation and no flow takes place.

### Compressor

A sliding vane compressor is a variation of vane compressors.

# Chapter 5

## SYSTEM

used for transmission of power through the medium of hydraulic oil. It works on the principle of Pascal's law which says that "the pressure is equal in all directions".

The fluid is hydraulic oil, which may be mineral oil or water or combination of these.

## Hydraulic system

connected to the output shaft in an enclosed cylinder

containing hydraulic fluid

on line of pump inside the tank or on tank inlet line.

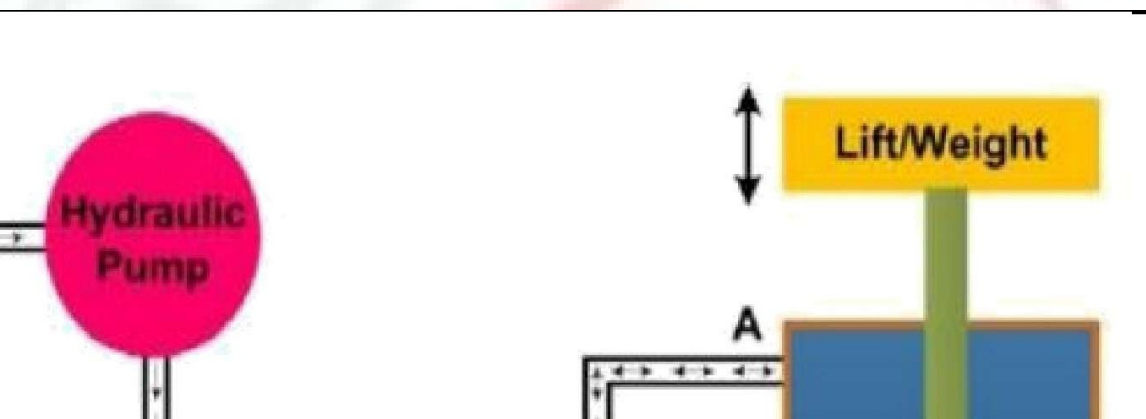
Driven by diesel or petrol engine which is the primary source of power

transmitted by motor or engine

through piping.

A valve which controls the direction of fluid flow so as to change the direction of movement of the actuator.

Used for linear movement or a hydraulic motor for rotary actuation of load.



nk, piping, cylinder and piston can be corroded with the hydraulic fluid. Sealing materials and hydraulic fluid.

size of the system is more which makes it unsuitable for the smaller systems. Hydraulic fluid can permanently damage the complete system. There

fluid is also a critical issue and suitable prevention method and seals must be disposed properly, can be harmful to the Environment.

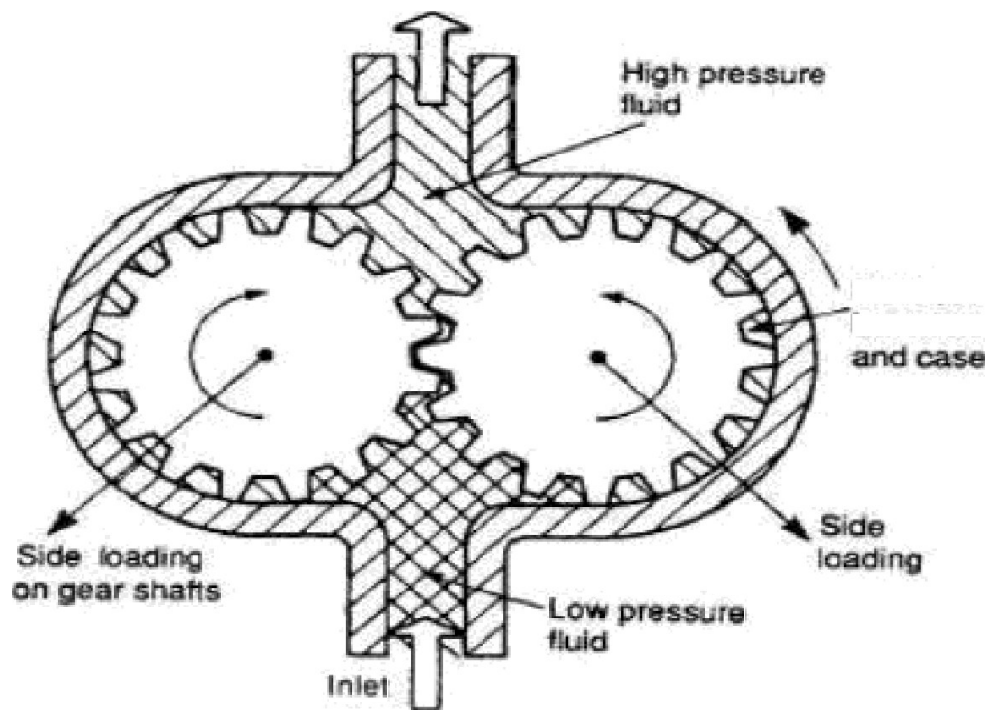
in hot areas it may catch fire  
they can cause serious injuries.  
is required.

Three types of hydraulic pump constructions found in mobile hydraulic systems are gear and vane; however, there are also clutch pumps, dump pumps, and power pumps.

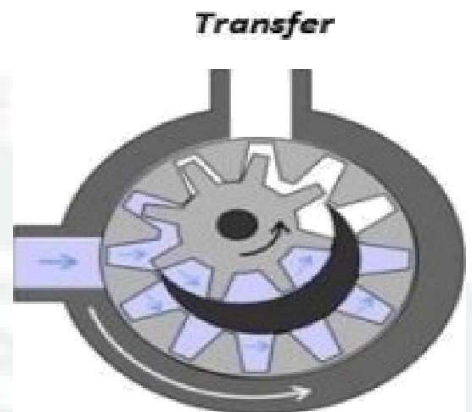
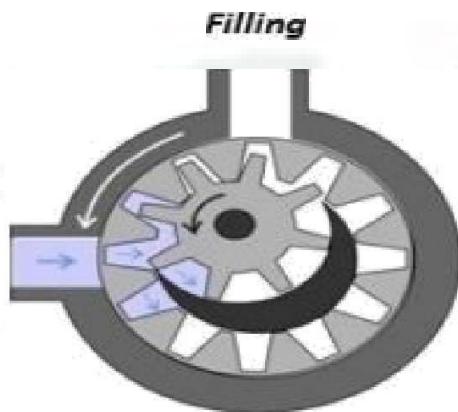
is the component of the hydraulic system that takes mechanical energy and converts it into a flow of oil. This mechanical energy is taken from what is called the prime mover take-off or directly from the truck engine.

ed by the of the propeller and the fluid pressure is proportional to the square of the flow rate.  
sure and high-volume flow  
ment pumps:





the suction port  
r (large exterior  
all interior gear)  
vs indicate the  
p and liquid.



through the pump between the teeth of the "gear-within-a-gear" principle.  
and acts as a seal between the suction and discharge ports.  
now nearly flooded, just prior to forcing the liquid out of the discharge  
and rotor form locked pockets for the liquid which assures volume con  
n mesh completely to form a seal equidistant from the discharge and  
d out of the discharge port.

is illustrated in Figure

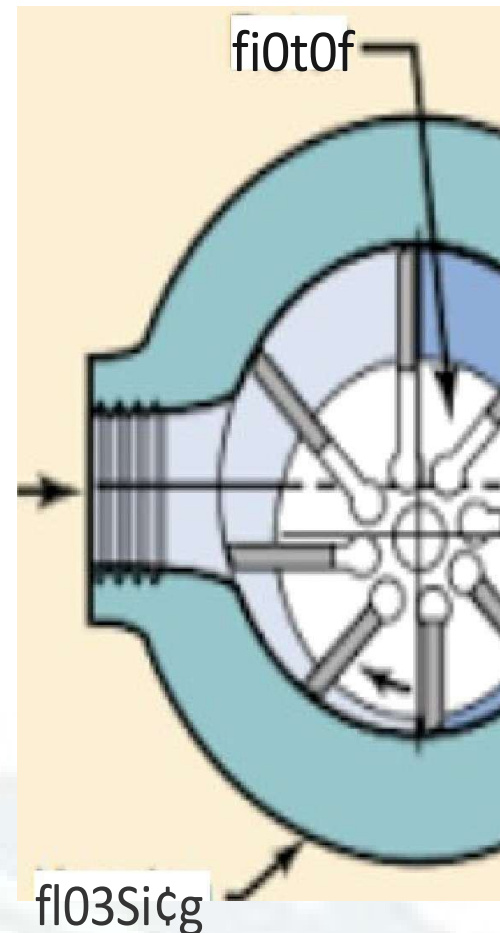
vanes are inserted into a numerous

turns the centrifugal force throws the  
cylindrical wall and creates a chamber  
r and the cylinder. As the rDtor  
the chamber volume between the  
ging due to the rotor positioned  
the inlet to outlet

me becomes bigger and then smaller.

gets bigger a vacuum is produced as  
rotation of the vanes making air  
er from the inlet.

r gets smaller due to the compressed  
duced at the outlet.

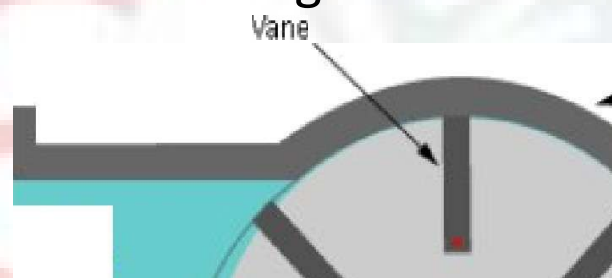


sign combines low cost with high reliability and easy maintenance. The  
rotor is eccentrically supported in a cycloid cam.

close to the wall of the cam so a crescent shaped cavity is formed. Two

as blades, slide in and out of the rotor slots to seal off a volume between  
id enters the crescent shaped pumping chamber through holes in the

the fluid to the opposite side of the  
is squeezed through the discharge,



---

the inner dead center (IDC) with suction process. After a rotation angle, the workspace of the piston is filled with the moved medium.

At the outer dead center (ODC).

the piston displaces the previously sucked medium in the pressure chamber.

Applications for a radial piston pump:

- Displacement of cutting emulsion, supply for hydraulic equipment like cylinders, presses, etc.
- (HPU) (e.g., for overload protection of presses)

- (e.g., automatic transmission, hydraulic suspension control in upper-cylinder engines, etc.)
- for injection molding

Supply additional fluid when main line fluid pump is inadequate to perform a function.  
An energy storage device: a device which accepts energy, stores energy, and releases it when needed.

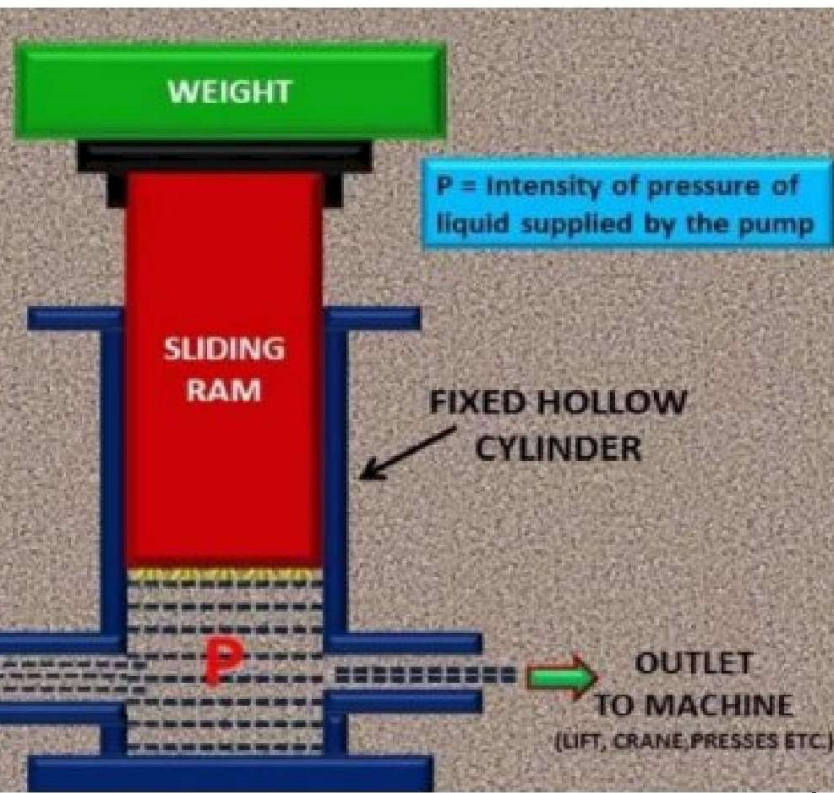
Accumulators accept energy at a low rate (low power) over a long time interval and release it at a high rate (high power) over a short time interval.

Types of accumulators include steam accumulators, mainsprings, flywheel energy storage, rechargeable batteries, capacitors, compensated pulsed alternators (common in hydroelectric plants).

A pressure accumulator is a pressure storage reservoir in which an incompressible hydraulic fluid is stored under pressure, supplied by an external source of mechanical energy.

The energy source can be an engine, a spring, a raised weight, or a compressed gas.

It enables a hydraulic system to cope with extremes of demand using a relatively small pump.



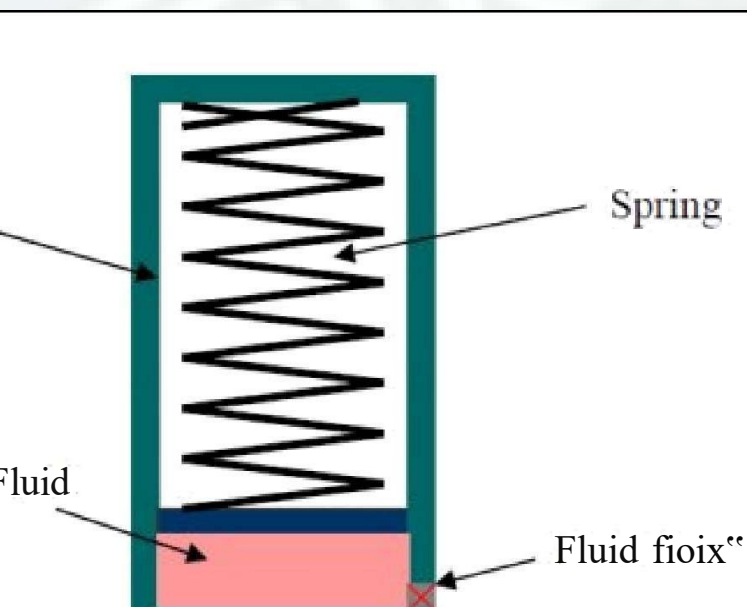
Container

Pressurized Fluid

accumulator:

accumulator is similar to the weight — loaded type except that the piston

source of energy that acts against the piston, forcing the fluid in to the



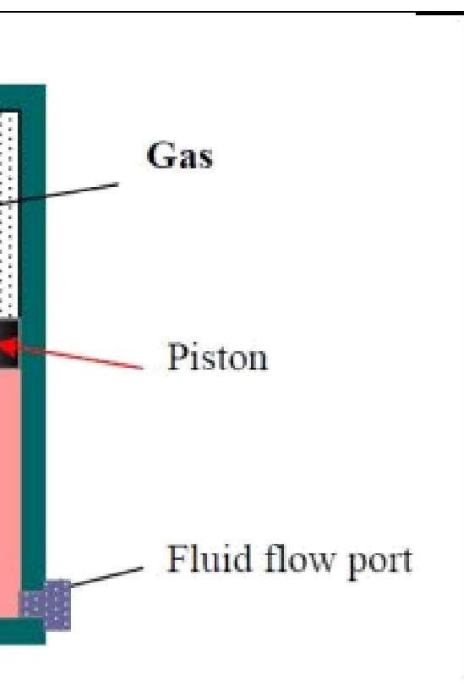


tor

ed design of gas loaded accumulators is the separator type. In this type, gas and the oil.

of separator accumulator are

accumulator consists of a cylinder containing a freely floating piston with



barrier between the gas and oil.

One of the disadvantages of the piston types of accumulator is that they are expensive to manufacture.

Another advantage of the piston accumulator is its ability to handle very high or low temperatures and to be compatible with O-ring seals.

Diaphragm

A diaphragm accumulator consists of a diaphragm, secured in the shell, which serves as a barrier between the gas and the oil.

The diaphragm is secured at the base of the shell, covers the inlet of the line,

---

Valves for controlling pressure include relief, reducing, sequence, counter

Valves are found in virtually every hydraulic system, and they assist in a variety of ways. Pressure-reducing valves maintain system pressures safely below a desired upper limit to maintaining a set pressure.

Pressure-reducing valves

Pressure-reducing

Pressure-reducing valves are designed to operate within a preset pressure range.

The magnitude of the forces the actuators in the system must generate to do the required work depends on these forces, the fluid power components (and expensive equipment) used, and the potential for hazard.

Pressure-reducing valves limit maximum pressure in a system by diverting excess oil to the reservoir.

The pressure at which a relief valve first opens to allow fluid to flow through is known as cracking pressure. Once it has passed its full rated flow, it is in a state of full-flow pressure. The difference between the system pressure and the cracking pressure is sometimes known as pressure differential, also known as pressure drop. The pressure at which a relief valve opens is known as its set pressure.

A relief valve may consist of a poppet or ball, held exposed to system pressure on one side and a spring force on the other.

In a normally closed relief valve (Fig. 1), the force exerted by the compression spring is balanced by the system pressure acting on the ball or poppet.

The ball or poppet is tightly seated. A reservoir port on the spring side of the valve allows the fluid to bypass to the reservoir.

When the system pressure begins to exceed the setting of the valve spring, the fluid unseats the ball or poppet.

The fluid then allows a certain amount of fluid to bypass to the reservoir, maintaining system pressure at the set point.

---

## Relief Valve:

es, the pressure in passage B rises as well, and, when it reaches the set pressure, the valve opens.

the main valve through passage B through the drain port.



the drop across orifice A in the valve opens it and excess oil flows out, preventing any further rise in inlet pressure.

When inlet oil pressure reaches the setting.

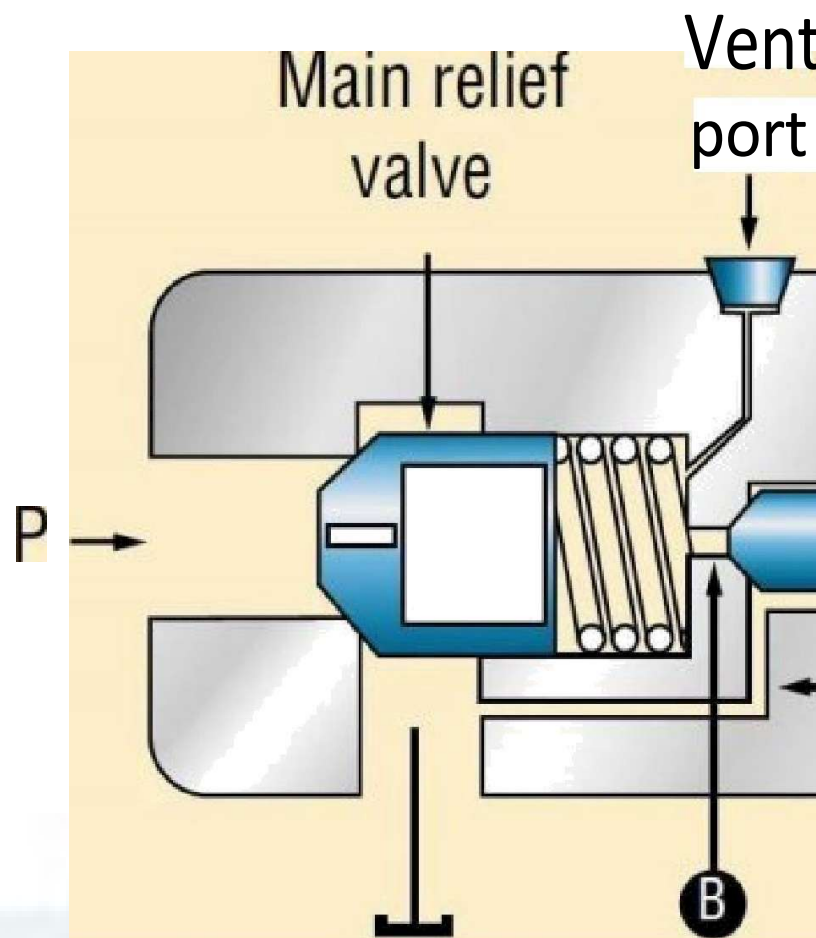
the valve does not start opening until approximately 90% of full pressure, the system is protected because

it is suited for high-pressure applications. Although their pressure setting is less accurate than that of direct-acting valves, they operate at a more constant pressure

valve:

Components for maintaining secondary, lower pressure in a hydraulic system

Pressure-reducing valves are normally open, 2-way valves that close when subjected to sufficient





Valves are essentially used for distribution of energy in a fluid power system through which a fluid traverses in a given circuit.

Valves are used to control the direction of flow in a hydraulic circuit.

Valves are used to control the start, stop and change in direction of flow of pressurized fluid in various lines of a hydraulic circuit.

Control of actuator speeds depends on flow rates. This type of control is achieved by using flow control valves.

Valves can be classified in a number of ways:

Construction.

Working ports:

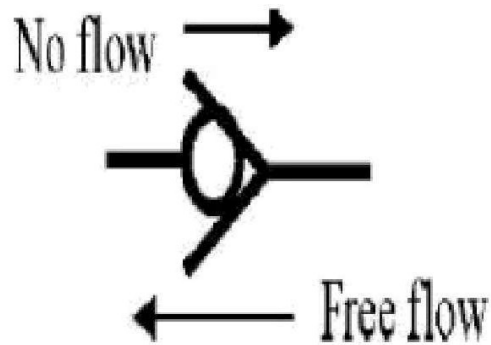
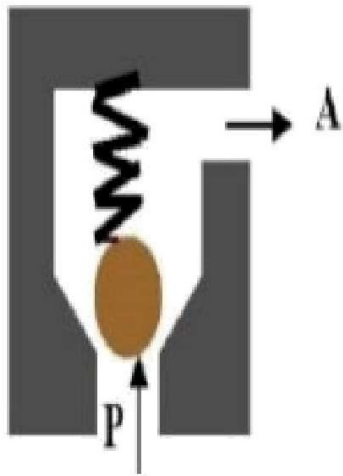
Switching position:

Mechanism:

Application

On

check valve is as shown. It is also called in<sup>□</sup>h-off or Non-return valve.



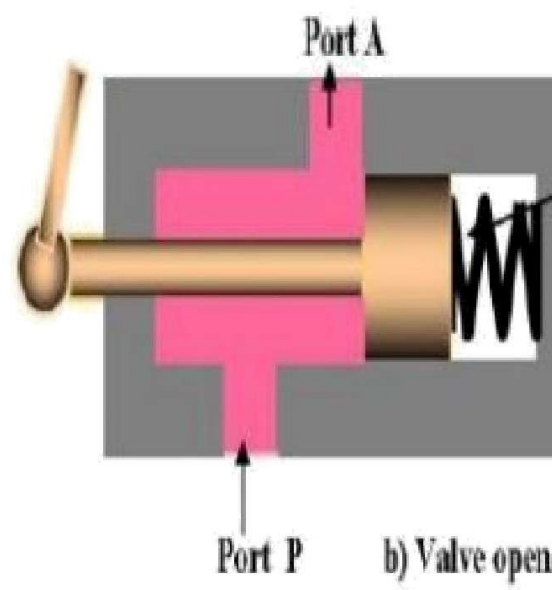
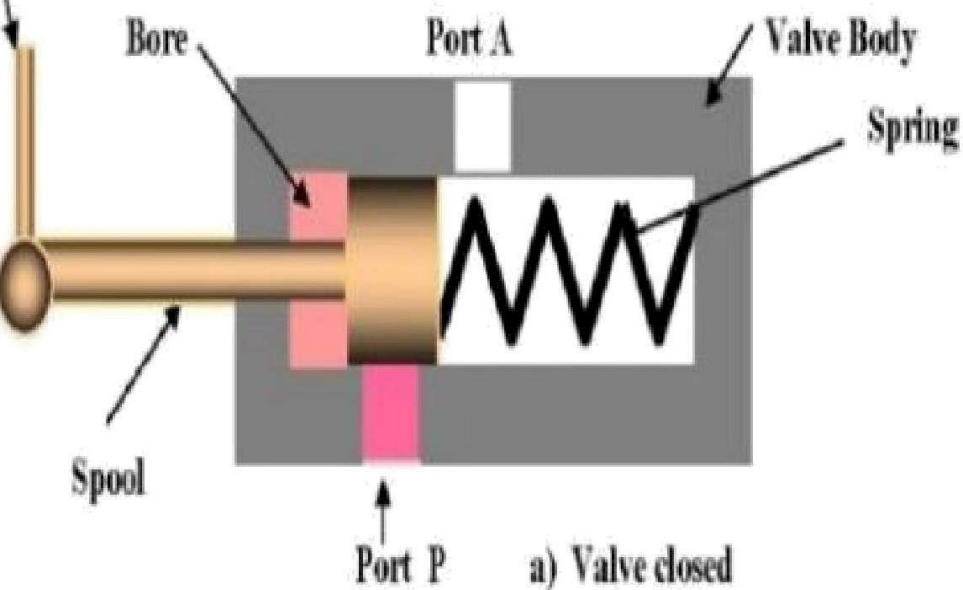
simplest type

l valve is a check valve which is a two way valve because it contains two  
so called as on-off valves because they allow the fluid flow in only in  
closed.

is usually the spool or poppet design with the poppet

off valve

for manual actuation



## control valves

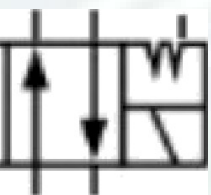
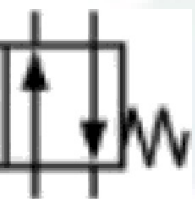
three working ports. These ports are: inlet, outlet, and exhaust (or tank). It is used to connect a valve to an actuator, but allows fluid to return from it as well.

3-way, 3-position valve. A valve of this type connected to a single-acting cylinder could extend, retract, or stop at any place in the stroke.

to select fluid flow paths Use a spool-type valve for this operation. Another type of valve is shown. A diverter valve sends fluid to either of two paths.

capable to control double-acting hydraulic cylinder and it can also control a single-acting cylinder. A DCV valve has four ports in which two of them would be outlet ports to the cylinder, one is the inlet and return to the tank.

## 2 position directional valves



shown are four-way two position valves. The '4 way' means it has 4 pipe connections: Port A, Port B, Port C, and Port D. The 'two position' means that it has two switched positions: Position A and Position B.

is operated by a manual lever and includes spring return.

valve is solenoid operated with two detent positions to hold the valve in its last

## Hydraulic Actuators

work fluid. Like pneumatic actuators, loss of fluid leads to less efficiency and in potential damage to surrounding components and areas. They require many complementary parts, including a fluid reservoir, motor, valves, and exchangers, along with noise reduction equipment.

In actuation, hydraulic actuators are classified as follows:

- Linear actuation (hydraulic cylinders).

- Rotary actuation (hydraulic motor).

- For limited angle of actuation (semi-rotary actuator).

Linear actuators, as their name implies, provide motion in a straight line.

The stroke is a finite amount determined by the construction of the unit.

The primary function of a hydraulic cylinder is to convert hydraulic power into linear mechanical force.

It extends and retracts a piston rod to provide a push or pull force to drive a load.

h.

Types

There are three of the following types:

- Single-acting cylinders.

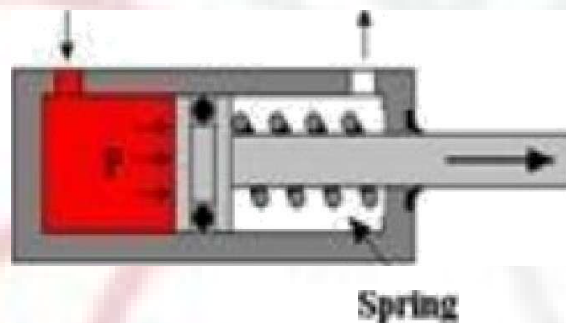
- Double-acting cylinders.

- Telescopic cylinders.

- Hydraulic rams.

Operation inside a

Push Action  
Oil to extend, Spring for retraction





---

specific pressure, the load shifting capacity decreases for each of the suction ports. This cylinder is used in application where a large amount of force is required to move a load. The pressure is applied to both the pistons, resulting in an increased force because of a large area. A disadvantage is that this cylinder must be longer than a standard cylinder to allow the pressure to reach both the pistons simultaneously.

ists of a housing with an eccentric bore, in which runs a rotor with vanes. The torque is created by the unbalanced force of the pressurized fluid on the vanes. On.

n vane motor design is how the vane tips are machined at the contact point. Several types of "lip"™ designs are used, which is to provide a tight seal between the inside of the motor housing and the vanes to minimize wear and metal-to-metal contact.



### Uses of Rotary Actuator

are used for many applications now such as  
drives, wheel motors for military vehicles, self-driven cranes, excavator  
drives,  
drives, roll mills, drum drives for digesters, shredders,  
cutters, high-powered lawn trimmers, and plastic injection machines.



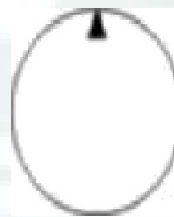
I\Miscellaneous fluids dra



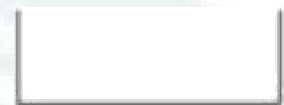
Piping

Riot line

Cra  
lin



J



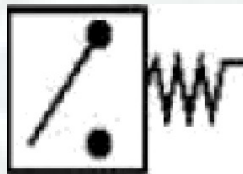
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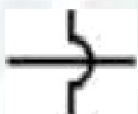
Hydraulic  
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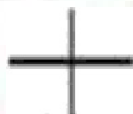
Filter



Accur



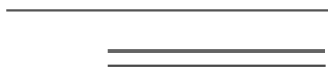
LINE'S  
NOT JOINED



3/2 DCV NO

3/2 DCV NC

4/2 DCV NC



Double-acting cylinder

Pressure Regulator

## nd Analysis

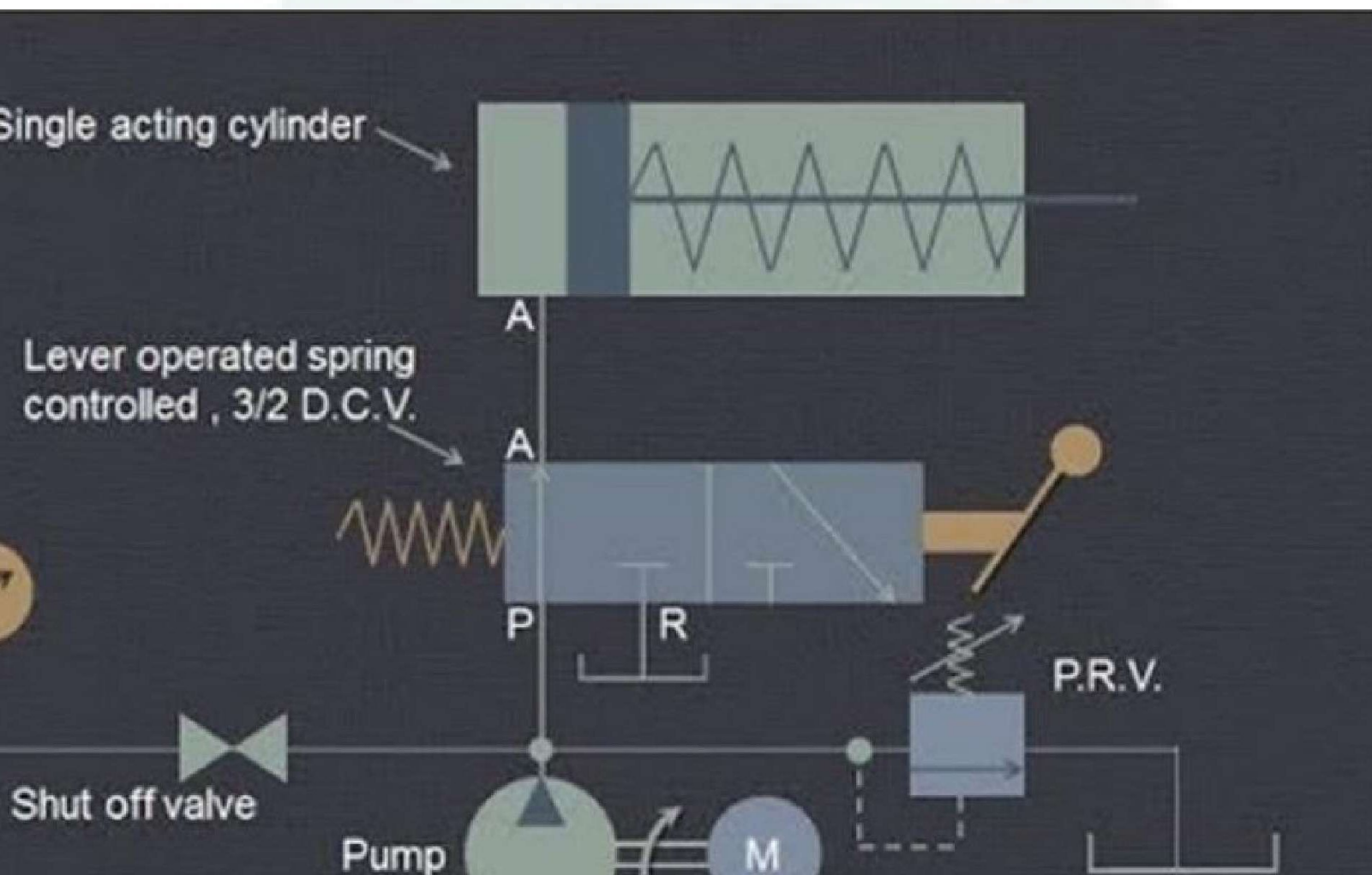
is a group of components such as pumps, actuators, and contrDI valve  
ful task.

designing a hydraulic circuit, the following three important considera

n

sired function

tion It is very important for the fluid power





of valve is used with the pipe line through which high pressurized liquid. If liquid exceeds the limit then it will help in escaping the excess liquid.

gages are fitted with the pipe line to meter the flow of liquid pressure. Pressure for the reciprocating action of piston in cylinder (actuator). It is at outlet of Pumping unit and also helps in measuring the pressure of oil as well as the pressure of liquid during return from single acting actuator. It carries the hydraulic liquid from pumping unit to the inlet of actuator and from actuator to the reservoir.

Actuator is used for transmitting of mechanical force by utilizing liquid pressure. DCV. The Spool type DCV is a handle operated type and handle is a component of Machinery Unit.

Diagram shown above for the representation of various components used in operation.

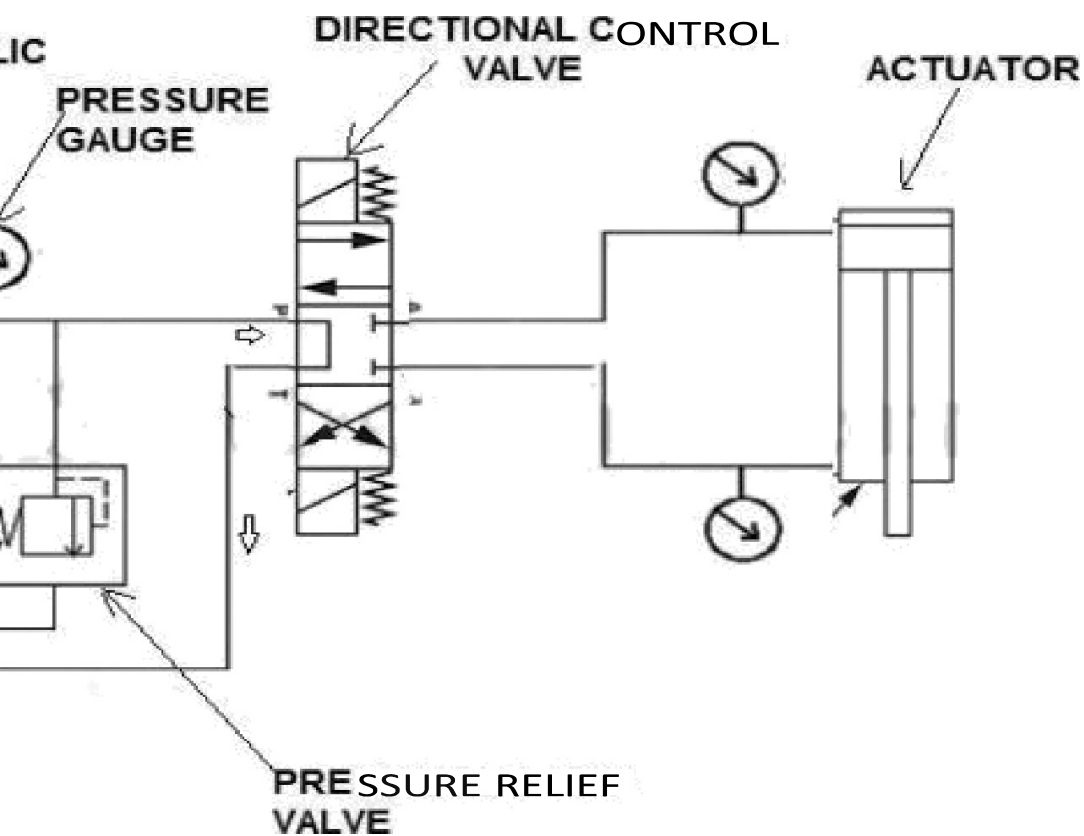
When there is no flow of hydraulic oil taking place through the pipe lines connected to the Actuator. This is also known as the ideal period for actuator operation:

When the system is switched on, the motor transmits the mechanical power to the pump.

The pump draws the oil from sump coming out through filter and converts it into liquid to the required pressure at the actuation point.

The gauge measures the outlet pressure of oil from Pump and if pressure exceeds the working pressure of pipe line to make it working pressure.

The control valve opens its passage from Port P to Port A and delivers the



oil used for the operation of actuator is stored in the reservoir. The oil is at atmospheric pressure.

used to separate the impurities, dusts, small insects floats on oil and purify the oil.

### Pumping Unit

A pump is required to transmit the fluid from reservoir to the direction control valve. The pump must provide the required pressure for the actuation of Double Acting Cylinder. The shaft of the pump is driven by the prime mover as shown in above hydraulic circuit. The inlet pipe connects from sump through filter.

A relief valve is used with the pipe line through which high pressurized liquid flows. When the pressure of liquid exceeds the limit then it will help in escaping the excess pressure to the tank. This helps in maintaining the system pressure.

Pressure gauges are fitted with the pipe line to meter the flow of liquid pressure. The pressure gauge indicates the required level of pressure for the reciprocating action of piston in cylinder. The pressure gauge at the outlet of the pumping unit and also helps in monitoring the system pressure.

at the rod end of piston is return to the tank through PDrt B and pass  
e and port T of DCV to the tank

on:

control valve opens its passage from Port P to Part B and delivers the h  
e connected to the Right side or ODC position of Piston in actuator.

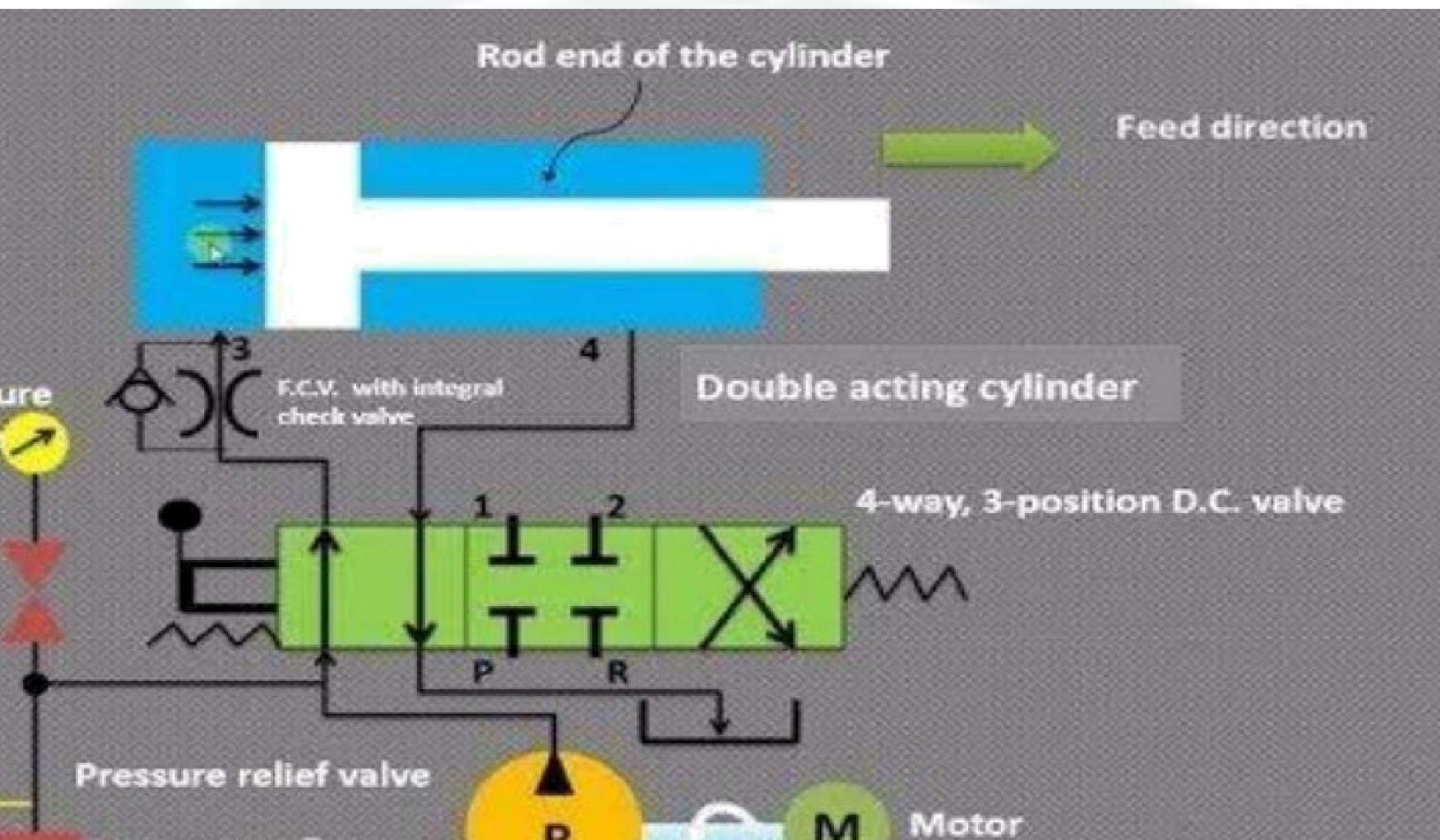
t T are used for return of Oil

l force is exerted by the high pressure Dil to move the piston form ODC  
ce is utilized in moving the parts of machine.

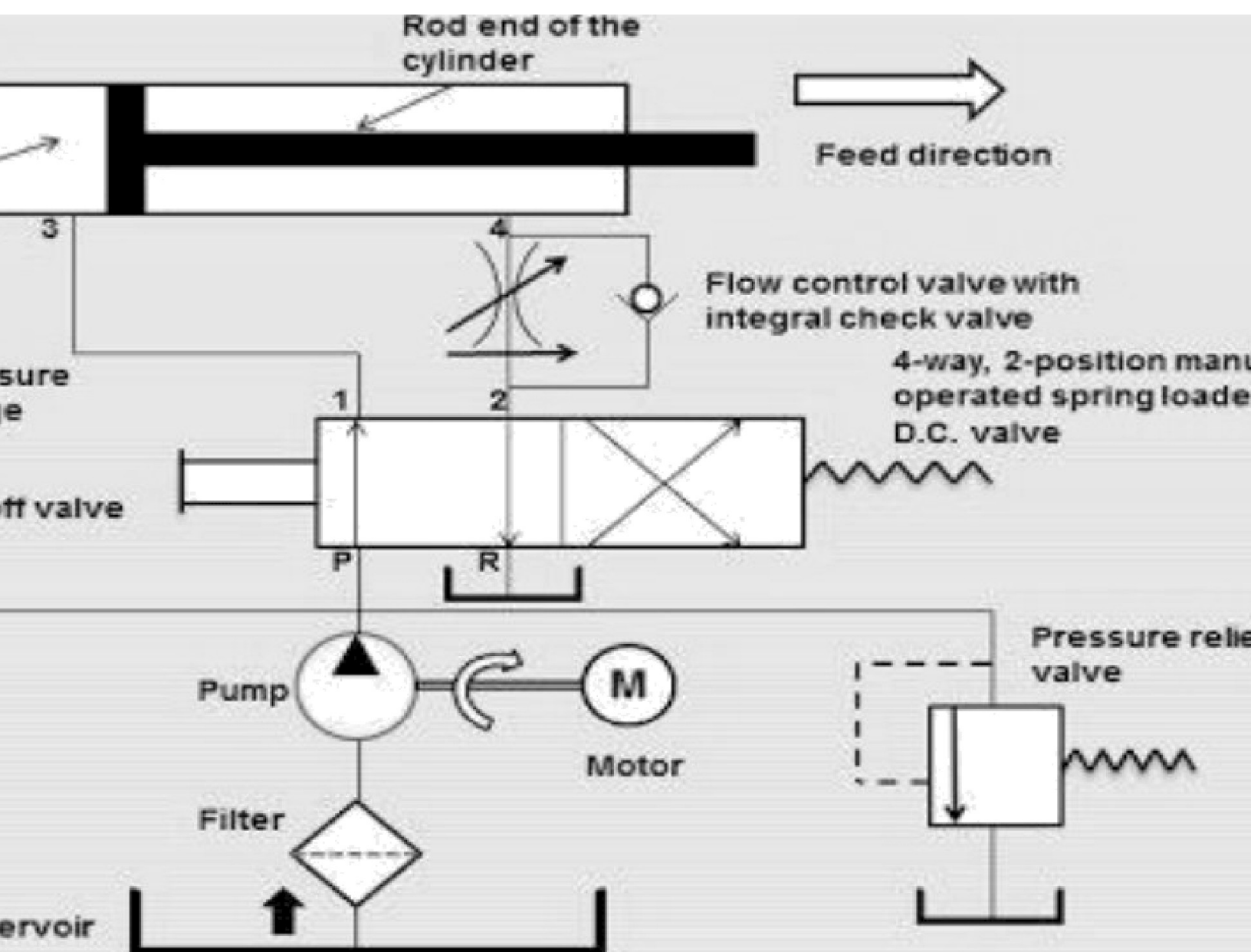
at the rod end of piston is return to the tank through Port A and pass  
e and port T of DCV to the tank

double actine cylinder is operated by the fluid pressure

acting cylinder with metering in control



the flow control valve is on the right side of the piston, the differential area. This increased pressure helps to overcome the pressure drop across the flow control valve. If the pressure required will be relatively low, it makes this circuit marginal. In the first example, initially, the compensatory spool is fully open, and full pump flow goes to the cylinder. As the piston moves forward building up pressure at the flow control valve.





Difference between Hydraulics and pneumatics

### Hydraulic systems

The working fluid is hydraulic oil.

As oil is incompressible, oil can be pressurized to very high pressure. (500 bar or even more)

Since pressure is high, the force developed is also very high (thousands of tonnes).

Since pressure is high, components are very strong, made of steel, and are heavy.

As oil has more viscosity, it cannot flow fast. Hence hydraulic systems are slower in operation.

Due to continuous recirculation, the temperature of oil increases.

Hydraulic oils are petroleum-based oils; they are inflammable and there is every chance of fire hazard if neglected.

Leakage of oil results in dirty and slippery surroundings that may lead to accidents.

The pump used is a positive displacement pump, So a pressure relief valve is necessary

There is no need for a separate lubrication system, because, hydraulic oil itself is a lubricant.

Applications: CNC. Machine tools, earth-moving machines, automobiles, aviation etc





## Pneumatic **systems**

Working fluid is compressed air.

Air is compressible; hence air can be pressurized to lesser pressure. (Only up to 10 bar approx.)

Since pressure is very less, the force developed is very less (up to 1 ton)

Components of the pneumatic system are lighter in weight, are made of aluminum.

Air has very less viscosity, it can flow fast. Hence pneumatic systems are quicker in operation.

The harder it runs, the cooler it works. Free expansion of air in cylinders and motors causes a chilling effect.

No chance of fire hazard. Hence pneumatic tools are preferably used inside mines, where flammable gasses may present.

The very clean and dry surrounding is maintained.

No need for a pressure relief valve. □

A lubricator is necessary. Oil is mixed with the compressed air in the lubricator and then supplied to the system.

Applications: Material handling systems, hand tools mining works, automation, automobiles, etc.



